NUMERICAL STUDY ON SHEAR BEHAVIOR OF REINFORCED CONCRETE SIMPLE BEAMS WITH DIFFERENT SHEAR-SPAN RATIOS

異なるせん断スパン比を持つ鉄筋コンクリート単純梁のせん断挙動に関する数値解析的研究

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The objective of this paper is to examine the performance of constitutive models for describing the cracking behavior and the load-displacement characteristics of shear failure of concrete structures. Concrete simple deep beams in different shear-span ratios (0.5 to 2.0) were analyzed. In addition, in order to expand the comprehension on the effect of constitutive model parameters in the deep beams to slender beams, the beams in the shear-span ratio of 4.0 were numerically simulated. The structural analysis was carried out by means of nonlinear finite element method. A smeared crack approach using rotating crack model without shear strain on the crack plane was employed. Based on this analytical work, the effect of the compressive strength reduction after cracking and the post-peak ductility in the constitutive law on shear fracture behavior for different shear-span ratios was discussed.

Keywords: Shear failure of concrete structures, Shear-span ratio, Nonlinear FEM analysis, Strength reduction after cracking, Post-peak ductility

1. INTRODUCTION

The mechanism of shear fracture in concrete structures has been the subject of heated debates in past decades. Yet, it has not been sufficiently clarified. On the other hand, several crack approaches as well as constitutive models for concrete under both uniaxial tension and compression loading have been proposed in many researches 1). However, reliable predictions for the extreme complex shear failure in concrete structures have not been achieved. The complexity of the shear failure depends considerably on how much the failure mode is governed by crushing behavior.

There are two representative numerical approaches to implement a crack model based on the Fracture Mechanics: discrete crack approach and smeared crack approach 2). The discrete crack approach is a direct application of crack models. Crack growth is analyzed on the assumption that cohesive forces are acting in the process zone. The complexity of the finite element analysis depends very much on whether the crack path is assumed in advance or not. If the crack path is not known in advance, the problem is much complicated. In the smeared crack approach, a cracked solid is assumed to be a continuum with the notion of stress and strain 3). The behavior of cracked concrete can then be described in terms of stress-strain relations and it is sufficient to switch from the initial isotropic stress-strain relation to an orthotropy stress-strain relation upon cracking. As a consequence, the topology of the original finite element mesh remains preserved which is computationally convenient. The two approaches presently seem to achieve better performance in different types of applications. In general, the smeared approach is better suited for engineering analyses of distributed fracture, while the discrete approach has its strength in detailed analyses of localized fracture. Thus, the smeared crack approach may be employed for a rough estimation of the load-displacement relation of shear failure of concrete structures in the practical design.

In this paper, the performance of constitutive models for describing the cracking behavior and the load-displacement characteristics of shear failure of concrete structures was examined. The problem on shear failure of RC beams in different shear-span ratios was employed as a practical application of the numerical modeling. The shear failure mode of RC beams changes complexly according to the shear span-ratio. Specifically, the shear failure mode of RC beams in relatively small shear span-ratio is governed by the interaction between the cracking behavior and the crushing behavior, while

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the shear failure mode of RC beams in relatively large shear-span-ratio is mainly governed by the cracking behavior. The intent of the present analysis is to investigate the practical approach to achieve the reliable prediction of the complex phenomena. In addition, the clarification on the performance of constitutive models for the complex failure could be useful in the material research.

The numerical simulations were carried out in the two-step procedure. Firstly, the appropriate parameters are determined in both compressive and tensile constitutive models so as to approximate the peak load and load-displacement relation obtained in the experiments, and to describe the cracking behavior observed in the experiments. This analysis is considered as the benchmark analysis. Thereafter, the sensitivity of the numerical results to the compression and tension softening parameters is examined. This analysis is considered as the parametric analysis. Based on this analytical work, the performance of the constitutive model parameters for different shear-span ratios was addressed.

2. BENCHMARK ANALYSIS

2.1 Review of Experiments

The simple deep beam tests were numerically simulated in practice. The experimental work was conducted by Niwa [1] to confirm the shear strength and formulate the design method of deep beams. The specimen and loading system for the test are shown in Fig. 1. Roller supports were provided at both the supporting and the loading points. The yield strength of main steel bar and transverse web reinforcement is 375.3 MPa and 400.8 MPa, respectively. The details of specimens, the material properties and the failure modes in the test are shown in Table 1. For the concrete, a water-cement ratio of 44% and the maximum aggregate size of 10 mm were adopted.

The shear tests were carried out in a displacement-control-testing machine. The vertical relative displacement measured between the loading point and the supporting point was considered as the shear displacement. The observed failure modes in all tests are classified in Table 1. DC stands for the shear failure accompanied with obvious crushing at the web concrete, and SL stands for the shear failure without obvious crushing at the web concrete. In the case of the shear-span ratio \(a/d\) lower than or equal to 1.0, a diagonal crack initiated at the web concrete and the shear load further increased. At the load level close to the peak, another crack propagated downward from the bottom edge of upper bearing plate and the concrete between cracks was crushed, finally leading to a slip-off along the connected cracks. In the case of \(a/d\) higher than or equal to 1.5, the shear load further increased after the initiation of a diagonal crack. The diagonal crack propagated upward without obvious crushing at the web concrete, and thrust against the bottom edge of upper bearing plate, finally leading to a brittle failure.

![Fig. 1: Specimen and Loading System](image)

<table>
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<th>TABLE 1: Detail of Specimens, Material Properties and Failure Modes</th>
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\(p_c\): ratio of main steel bar; \(p_r\): ratio of transverse web reinforcement 
\(f_c\): compressive strength of concrete

2.2 Finite Element Analysis

The structural analysis was carried out using SBETA [2] Finite Element Program developed by V. Cervenka et al. A smeared crack approach using a rotating crack model was employed. In addition, the following effects of concrete behavior were considered: nonlinear behavior in compression including hardening and softening; fracture of concrete in tension based on nonlinear fracture mechanics; biaxial stress failure criterion [3] by means of equivalent uniaxial stress-strain relationship [4]; reduction of compressive strength after cracking [5]. The details of the numerical formulation are given in SBETA [2].

The present study focuses mainly on the softening parameters of the constitutive models. Regarding the compressive constitutive models, the reduction of the compressive strength after cracking in the direction parallel to the cracks was applied, and several stress reduction rates were considered. A linearly descending softening law in compression was adopted and the influence of the end-point of the softening curve on the predicted load-displacement relations was also examined. Regarding the tensile constitutive models, an exponential crack opening model, a linear crack opening model and a tension cut-off model were alternatively employed. In the rotating crack model [6,7], the direction of the principal stress coincides with the direction of the principal strain. No shear strain occurs on the crack plane and only two normal stress components must be defined. If the principal strain axes rotate during loading, the direction of cracks also rotates.

Behavior of concrete in tension without crack was assumed linearly elastic. After cracking, three types of models were alternatively used in this analysis for the crack opening as shown in Fig. 2. The function of the exponential crack opening model was empirically derived by Hordijk [8] as follows:
\[
\frac{\sigma}{f'_{c,ef}} = \left[1 + \left(\frac{c_1 w_t}{w_t^c}\right)^3\right] e^{-(c_2 w_t^c)^3} - \frac{w_t^c}{w_t^c} \left(1 + c_2\right) e^{-(c_2 w_t^c)^3} 
\]
(1a)

\[
w_t^c = 5.14 \frac{G_F}{f'_{c,ef}} 
\]
(1b)

where \(w_t\) is the crack opening displacement, \(w_t^c\) is the crack opening displacement at the complete release of stress, \(\sigma\) is the normal stress in the crack and \(f'_{c,ef}\) is the effective tensile strength associated with the biaxial stress failure criterion according to Kupfer \(^6\). Values of the constants are \(c_1 = 3.0\) and \(c_2 = 6.93\). \(G_F\) is the fracture energy needed to create a unit area of stress-free crack. The crack opening displacement \(w_t\) is derived from strains based on the Crack Band Theory. The linear crack opening model gives the relation of \(w_t^c = 2G_F/\pi f'_{c,ef}\) and the tension cut-off model has no softening regime and abrupt stress-drop after cracking.

For the ascending branch of concrete stress-strain curve in compression, the formula recommended by CEB-FIP Model Code 90 \(^{12}\) was adopted (see Fig. 3a).

\[
\sigma_c = f'_{c,ef} \frac{kx - x^2}{1 + (k - 2)x}, \quad x = \frac{\epsilon_c \epsilon_0}{\epsilon_c}, \quad k = \frac{E_0}{E_c} 
\]
(2)

where \(\sigma_c\) is the compressive stress, \(\sigma\) is the compressive stress, \(f'_{c,ef}\) is the effective compressive strength associated with the biaxial stress failure criterion according to Kupfer \(^6\), \(\epsilon_c\) is the strain at the peak stress, \(k\) is a shape parameter and the value of 2.0 was used in this analysis for parabola, \(E_c\) is the initial elastic modulus, \(E_0\) is the secant elastic modulus at the peak stress.

For the descending branch of concrete constitutive curve in compression, a fictitious compression plane model is used in SBETA based on the assumption that a compression failure is localized in a plane normal to the direction of compressive principal stress. All post-peak compressive displacements and energy dissipation are localized in this plane. It is assumed that the displacements are independent of the size of the structure and such hypothesis is supported by experiments conducted by van Mier \(^{13}\). Softening law in compression is linearly descending. The end point of the softening curve is defined as a limit displacement \(w_t^c\) at the complete release of stress (see Fig. 3b).

The reduction of the compressive strength after cracking in the direction parallel to the cracks is considered in a similar way as found in the experiments of Vecchio and Collins \(^9\). The reduction function was empirically developed by Kolleger et al. \(^9\) as follows:

\[
f'_{c,ef} = r_c f_c, \quad r_c = c + (1-c)e^{-(128\epsilon_c)} 
\]
(3)

where \(r_c\) is the compressive strength reduction rate, \(\epsilon_c\) is the transverse strain (crack opening strain) and \(f_c\) is the concrete compressive strength. For zero transverse strain, there is no strength reduction and for large strains the strength asymptotically approaches the minimum value \(f'_{c,ef} = f_c\), (see Fig. 4). The constant \(c\) is the maximum strength reduction rate under a large transverse strain.

In the constitutive models, the initial elastic modulus \(E_0\) and the tensile strength \(f_t\) of concrete are estimated using the following equations \(^{14, 15}\).

\[
E_0 = 4733\sqrt{f_c} \quad \text{(MPa)} 
\]
(4)

\[
f_t = 0.332\sqrt{f_c} \quad \text{(MPa)} 
\]
(5)

The fracture energy \(G_F\) was assumed as 0.1 N/mm except the tension.
cut-off model (\(G_d=0.0\)), a value often used by many researchers \(^3\). In addition, Balakrishnan and Murray \(^6\) suggested values between 0.05 N/mm and 0.25 N/mm, with 0.1 N/mm being the most effective.

2.3 Comparison between Experiments and Benchmark Analysis

The FEM model employed here was chosen to describe the test configuration of Niwa \(^4\). After some trials in preliminary numerical studies, the geometric and loading configuration as well as mesh profile were adopted in the FEM model. The configuration of the FEM model for S1 beam (see Table 1) is shown in Fig.5. Considering the symmetry of the specimen, only half of the structure is analyzed. It should be noted that the strength of the hatched elements in the figure is increased in 80% to consider three-dimensional compression state due to the restraint of the bearing plates based on the numerical study by Niwa \(^4\). The specimen is assumed to be in a state of plane stress. Finite plane stress elements consist of quadrilaterals composed of two four-node sub-triangles. The stress-strain relation in reinforcement is assumed as a perfectly elastoplasticity. The main steel bar (thick line) at the bottom of the beam is modeled by a discrete bar finite element which is embedded and passing through quadrilateral elements as shown in Fig. 5. The bar element has only axial stiffness and is in the uniaxial stress-state. It should be noted that on a macro-level, a relative slip distance of reinforcement with respect to concrete over a certain distance arise, if concrete is cracked or crushed. The transverse web reinforcement is modeled by a smeared reinforcement which stress and stiffness are considered in the quadrilateral element. While the vertical displacement of the support of the specimen is restrained, a vertical prescribed displacement is applied at the loading point.

In the benchmark analysis, an exponential crack opening model is used (see Fig. 2a). The adopted quantities of the maximum strength reduction rate \(c\) are shown in Fig. 6, and the adopted limit displacement \(w_c\) is 1.0 mm (see Fig. 3b). Particularly to approximate the peak load, \(c=0.0\) was assumed for \(a/d=0.5\) or lower, and no strength reduction \(c=1.0\) for \(a/d=2.0\) or higher. In the case of the shear-span ratios between 0.5 and 2.0, the interpolating values of \(c\) between 0.0 and 1.0 are adopted, as shown in Fig. 6. Here, it should be noted that the relation between \(c\) and shear span-ratio in the figure is consistent with the experimental observation such that the smaller is the shear span-ratio, the stronger is the interaction between cracking and crushing. However, to formulate the constitutive model on the shear span-ratio, further experimental and numerical study is necessary.

First, the cracking behavior predicted by the FEM analysis is examined. The cracking patterns at the peak load for S1 and S4 beams are shown in Figs. 7a and 7b. In the figures, the hatched area indicates the crushed concrete and the thicker crack line indicates the larger crack width. In the shear-span ratio of \(a/d=1.0\) or lower, the shear failure accompanied with heavy crushing at the web concrete was observed. Flexural cracks initiate at the bottom of the beam and subsequently diagonal cracks initiate at the web concrete. At the load level close to the peak, the crushed concrete zone associated with widely opened diagonal cracks at the bottom edge of upper bearing plate grows downward, leading to a slip-off failure. In the shear-span ratio of \(a/d=1.5\) or higher, the shear failure without obvious crushing at the web concrete is observed. Flexural cracks initiate at the bottom of the beam and propagate to the mid-depth of the beam. Subsequently, diagonal cracks initiate at the web concrete and continue to propagate along the line between the loading point and the support, and
grow excessively wide. Nearly at the peak load level, the compression failure is observed at the extreme compression fiber, and the diagonal cracks thrust against the bottom edge of upper bearing plate, leading to a brittle failure. In the shear-span ratio of \(a/d=0.5\), no yield of reinforcement is observed. However, in the shear-span ratio of \(a/d=1.0\) or higher, the transverse reinforcement is partially yielded. Based on the comparisons of cracking behavior between the FEM analysis and the experiment, it may be concluded that the FEM model in the benchmark analysis approximates the cracking behavior and the failure mode of test results.

Fig. 8a shows the comparison between the results of shear load-displacement relations obtained in the experiment and in the FEM analysis. The numerical simulation approximates the overall test results. A more precise prediction may be obtained with modified parameters of constitutive models as well as modified geometric configuration and mesh profile. However, the current results already show that both the cracking behavior and the load-displacement characteristics were captured overall by the adopted FEM model. Therefore, the current FEM model can be used as the benchmark analysis to examine the effect of constitutive model parameters for shear failure of concrete beams, discussed next.

### 3. PARAMETRIC ANALYSIS ON CONSTITUTIVE PARAMETERS

#### 3.1 Influence of Softening Parameters in Compression

The sensitivity of the results from the numerical simulation to each of the maximum strength reduction rate \(c\) and the limit displacement \(w_{cr}\) was examined. Fig. 8b shows the comparison between the results of shear load-displacement relations in the benchmark analysis and in the parametric analysis with the maximum strength reduction rate \(c\) of 0.0 or 1.0. In this parametric analysis, the tensile constitutive model and the value of the limit displacement \(w_{cr}\) are identical to that in the benchmark analysis. The difference between the predicted load-displacement curves with \(c=0.0\) and \(c=1.0\) is considerably large in the case of \(a/d=0.5\). The difference is however reduced in the larger shear-span ratio. The predicted failure mode with \(c=1.0\) for S1 beam is different from that observed in the benchmark analysis as shown in Fig. 7a. The peak load is associated with the bearing compression failure just above the lower bearing plate, instead of the crushing of compression strut at the web concrete. It may be explained by the fact that the condition of no compressive strength reduction after cracking \((c=1.0)\) gives a large crushing resistance to the compression strut at the web concrete, resulting in the further increase of the shear load, and allowing the bearing compression failure. The larger is the value of \(c\), the higher is the crushing resistance of the compression strut at the web concrete. The condition of \(c=0.0\) gives crushing behavior at the web concrete for S3 and S4 beams, which was not observed in both the experiment and the benchmark analysis. Thus, the predicted failure modes and load-displacement curves are strongly influenced by the value of \(c\).

Fig. 8c shows the comparison between the results of shear load-displacement relations in the benchmark analysis and in the parametric analysis with the limit displacement \(w_{cr}\) of 0.5 mm. In this parametric analysis, the tensile constitutive model and the value of the maximum strength reduction rate \(c\) are identical to those in the benchmark analysis. There is no obvious difference of the predicted failure modes between the parametric analysis and the benchmark analysis with respect to cracking behavior. The limit displacement \(w_{cr}\) considerably influences the entire load-displacement relation as well as the peak load in the case of \(a/d=1.0\) or higher. The larger is the limit displacement, the higher is the peak load. However, in the case of \(a/d=0.5\), this parameter does not influence the entire load-displacement relation and neither the peak load. It may be

![FIG. 8: Comparison of Shear Load-Displacement Relations (a) between Experiment and Benchmark Analysis; (b) in terms of Maximum Strength Reduction Rate \(c\); (c) in terms of Limit Displacement \(w_{cr}\); (d) in terms of Tension Softening Models](image-url)
caused by the fact that in the case of $a/d=0.5$, the abrupt load drop after the peak load is associated with the crushed concrete zone along the shear plane, which rapidly distributed. The stress redistribution is therefore not allowed. In the case of $a/d=1.0$ or higher, the large limit displacement $w_r$ allows the stress to be redistributed, resulting in the increase of the peak load. Thus, the post-peak ductility in the compressive constitutive model allows the increase of the load-carrying capability of concrete beams in the case of $a/d=1.0$ or higher. Based on this observation, another aspect on the effect of fiber reinforcement in concrete structures can be identified, which may be significant in the material development. This is because so far the ductility improvement of fiber reinforcement in both tension and compression is mainly recognized.

3.2 Influence of Softening Parameters in Tension

The sensitivity of the results from the numerical simulation to the tension-softening model was examined. In this parametric analysis, the linear crack opening model and the tension cut-off model ($G_r=0.0$) are employed.

Fig. 8d shows the comparison between the results of shear load-displacement relations in the benchmark analysis and in the parametric analysis with different crack opening models. In this parametric analysis, the quantities of the maximum strength reduction rate $c$ and the limit displacement $w_r$ are identical to those in the benchmark analysis. There is no obvious difference of the predicted failure modes between the parametric analysis and the benchmark analysis with respect to cracking behavior. The influence of the tensile constitutive model on the numerical results in the case of $a/d=2.0$ is relatively higher than that in the case of $a/d=0.5$. There is no significant difference in the numerical results between the linear crack opening model and the exponential crack opening model. However, in the parametric analysis with the tension cut-off model, the load-carrying capability was partially lost at the early load level in the case of $a/d=1.5$ or higher. Thus, the predicted shear load-displacement relation is not sensitive to the shape of tension-softening model. However, in comparison with no sensitivity to the shape of tension-softening model, the consideration of the tension-softening behavior influences slightly the load-displacement relations as well as the peak load.

4. ANALYSIS FOR SLENDER BEAMS

In the previous analysis, the sensitivity of numerical simulations to the softening parameters in constitutive models was examined based on the experimental observations in the deep beam tests. To expand the comprehension on the effect of softening parameters in the deep beams to slender beams, the beams in the shear-span ratio of 4.0 were numerically simulated. Two models were considered to examine the different failure modes (see Table 2). One is Slender Beam 1, which is identical to S4 beam except for the shear-span ratio. The other is Slender Beam 2, which is identical to Slender Beam 1 except for the reduced ratio of main steel bar ($p_r=0.744\%$). Slender Beam 2 is expected to have a flexural failure, while Slender Beam 1 a shear failure.

| TABLE 2: Parameters in Benchmark Analysis for Slender Beams |
|-----------------|---|---|---|---|---|---|---|---|
| $a$ (cm) | $a/d$ | $l$ (cm) | $p_r$ (%) | $p_c$ (%) | $f_r$ (MPa) | $c$ | $w_r$ (mm) |
| Beam 1 | 128.0 | 4.0 | 270.0 | 310.0 | 3.72 | 0.45 | 54.43 | 1.0 |
| Beam 2 | 128.0 | 4.0 | 270.0 | 310.0 | 0.744 | 0.45 | 54.43 | 1.0 |

4.1 Benchmark Analysis for Slender Beams

In the benchmark analysis for the slender beams, an exponential crack opening model, the maximum strength reduction rate $c=1.0$ (no strength reduction), and the limit displacement $w_r=1.0$ mm were adopted (see Table 2). The cracking patterns at the peak load for both slender beams are shown in Figs. 9a and 9b. Flexural cracks initiate at the bottom of the beam and propagate to the mid-depth of the beam in both beams. In the case of Slender Beam 1, subsequently diagonal cracks initiate at the web concrete and continue to propagate in a diagonal direction, growing excessively wide. At the load level close to the peak, the compression failure is observed at the extreme compressive fiber and the both the main reinforcement and the transverse reinforcement are yielded. In the case of Slender Beam 2, neither obvious diagonal crack nor compression failure is observed, resulting in the propagation of the flexural cracks to the upper-depth of the beam. The failure load is associated with the yield of the main reinforcement, and the transverse reinforcement is not yielded at this stage.

4.2 Influence of Softening Parameters in Compression

The sensitivity of the results from the numerical simulation to each of the maximum strength reduction rate $c$ and the limit displacement $w_r$ was examined. Fig. 9c shows the comparison between the results of shear load-displacement relations in the benchmark analysis and in the parametric analysis with $c=0.0$ and $w_r=1.0$ mm, or $c=1.0$ and $w_r=0.5$ mm. In this parametric analysis, the tensile constitutive model is identical to that in the benchmark analysis. There is no obvious difference in the predicted failure modes between the parametric analysis and the benchmark analysis with respect to cracking behavior. Particularly, the condition of $c=0.0$ does not give the crushing behavior at the web concrete for Slender Beam 1. As shown in the figure, the numerical results are sensitive to the value of $w_r$ in Slender Beam 1 as observed in the deep beams. However, the numerical results are not sensitive to the value of $c$. It may be explained by the fact that the peak load in Slender Beam 1 with $c=0.0$ is associated with the compression failure without diagonal crack in the element at the extreme compressive fiber of the beam, and no crushing at the web concrete is observed. Therefore, the maximum strength reduction rate $c$ does not influence the compression strength. On the other hand, in Slender Beam 2, the numerical results are sensitive to the value of neither $c$ nor $w_r$. Thus, the comprehension on the effect of compressive softening parameters in the deep beams can be also applied to the slender beams, if the shear failure mode is dominant and governed by the crushing at the web concrete. However, there is little effect of compressive softening parameters for the beams when the flexural failure mode is dominant.
4.3 Influence of Softening Parameters in Tension

The sensitivity of the results from the numerical simulation to the tension-softening model was examined. In this parametric analysis, the linear crack opening model and the tension cut-off model ($G_c=0.0$) are employed. Fig. 9d shows the comparison between the results of shear load-displacement relations in the benchmark analysis and in the parametric analysis with the different crack opening models. In this parametric analysis, the values of the maximum strength reduction rate $c$ and the limit displacement $w_0$ are identical to those in the benchmark analysis. There is no obvious difference in the predicted failure modes between the parametric analysis and the benchmark analysis with respect to cracking behavior. As shown in the figure, the predicted shear load-displacement relation is not sensitive to the shape of tension-softening model. However, the consideration of the tension-softening behavior highly influences the numerical results in both beams, especially the significant influence in Slender Beam 2. Thus, comprehension on the effect of tension softening parameters in deep beams can be also applied to the slender beams, especially when the flexural failure mode is dominant.

5. CONCLUSIONS

In this paper, numerical simulations were carried out to examine the performance of constitutive models for describing the cracking behavior and the load-displacement characteristics of shear failure of reinforced concrete simple beams. Based on the structural analysis for the shear-span ratio of 0.5 to 4.0, the following conclusions can be drawn.

The compressive strength reduction rate after cracking considerably influences the prediction of shear failure of concrete simple beams. Particularly, a large compressive strength reduction rate is necessary to approximate the shear behavior of the beams with a small shear-span ratio.

The compression-softening curve does not influence the entire load-displacement relation and neither the peak load in the case of small shear-span ratio ($a/d=0.5$). However, in the case of large shear-span ratio ($a/d=1.0$ or higher), the post-peak ductility in the compressive constitutive law allows the increase of the shear load-carrying capability of beams when the shear failure mode is dominant. Therefore, the methodology such as fiber reinforcement to increase the compressive post-peak ductility may become significant in the material development.

The shape of tension-softening model does not significantly differentiate the predicted shear load-displacement relation. However, the consideration of the tension-softening behavior highly influences the load-displacement relation as well as the peak load, especially when the flexural failure mode is dominant.

In the present numerical study, a particular numerical approach and particular constitutive models are employed. However, the above mentioned conclusions are qualitatively applicable to the practical analysis and also significant in the material research field.

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REFERENCES

和文要約

1. 序
コンクリートのせん断破壊メカニズムは、これまでにも数多く議論されてきたが、まだ十分には解明されていない。これまでにさまざまなせん断破壊実験の可能性が提案されてきたが、複雑なコンクリートのせん断破壊挙動を数値解析的に十分に評価するまでには至っていない。本研究では、回転分岐及び割れを用いて、コンクリート構造物のせん断破壊現象評価に与える構成要素パラメータの影響について数値解析をおこなった結果を報告した。これらの結果をもとに、構成要素を取りくみせん断破壊挙動の理解を深めた。

2. ベンチマーク解析

2.1 ディープビューせん断実験
図2に示す既存のディープビューせん断実験において、数値解析を行った。結果を表3と図3の詳細を示す。実験では、せん断スパン比1.0を下げる場合、試験体ウェップ部にせん断破壊が観察され、せん断スパン比が1.5以上の場合は、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

2.2 有限要素法解析
有限要素法解析は、Cenverka等により開発されたSBETA有限要素法プログラムにより、回転分岐及び割れを用いて行った。引張破壊解析では、ひび割れ発生後のせん断破壊実験において、引張破壊モードは観察され、せん断スパン比が1.5以上の場合は、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

2.3 せん断実験結果とベンチマーク解析の比較
解析モデルの、図5に示すように、せん断スパン比とせん断破壊モードを評価した。実験では、せん断スパン比が1.0以下の場合は、せん断破壊モードが観察され、せん断スパン比が1.5以上の場合は、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

3. バラメータ解析
3.1 圧縮軟化パラメータの影響
図6にベンチマーク解析結果とせん断強度低下率とせん断破壊モードを評価した。図7に示すように、せん断破壊モードが観察され、せん断スパン比が1.0の場合、破壊モードがウェップ部のせん断破壊を伴わせん断破壊モードが観察された。

3.2 引張軟化パラメータの影響
図8にベンチマーク解析結果とせん断破壊モードを評価した。図9に示すように、せん断破壊モードが観察され、せん断スパン比が1.0の場合、破壊モードがウェップ部のせん断破壊を伴わせん断破壊モードが観察された。

4. 線形パラメータの影響
4.1 ベンチマーク解析
ディープビューせん断実験における数値解析により得られた結果を示す。実験では、せん断スパン比が1.0の場合は、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

4.2 圧縮軟化パラメータの影響
図9にベンチマーク解析結果と、せん断強度低下率とせん断破壊モードを評価した。図7に示すように、せん断破壊モードが観察され、せん断スパン比が1.0の場合、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

4.3 引張軟化パラメータの影響
図9にベンチマーク解析結果と、せん断強度低下率とせん断破壊モードを評価した。図7に示すように、せん断破壊モードが観察され、せん断スパン比が1.0の場合、試験体ウェップ部にせん断破壊を伴わせん断破壊モードが観察された。

5. 結論
本研究では、コンクリート構造のせん断破壊におけるひび割れ挙動及びせん断強度を数値解析的に評価するための構成要素パラメータの影響を検討した。せん断スパン比が1.0の場合、破壊モードがせん断破壊を伴わせん断破壊モードが観察された。この結果をもとに、せん断スパン比が1.0の場合、破壊モードがせん断破壊を伴わせん断破壊モードが観察された。