Design and implementation of a multi-channel space-borne SAR imaging system on Vivado HLS

Zixin Gao, Chen Yang, Yizhuang Xie, Bingyi Li, He Chen, and Yu Xie

Beijing Key Laboratory of Embedded Real-time Information Processing Technology, Beijing Institute of Technology, Beijing 100081, China
a) xyz551_bit@bit.edu.cn

Abstract: New generation space-borne SAR (synthetic aperture radar) systems require high real-time processing performance and have size, weight and power constrains. This paper presents a multi-channel stripmap SAR imaging system implemented on an FPGA platform. In order to reduce FPGA design cost, a high-level synthesis tool Xilinx Vivado HLS is applied to design and implement the SAR imaging system. FFT algorithms in the imaging algorithm use FFT IP cores in FPGA, and the rest is customized on HLS. The modules designed on HLS are optimized and packaged as IP blocks for FPGA implementation of the imaging system. The performance and resource utilization of the whole system are evaluated by processing a two-channel SAR raw data with a granularity of 16384 × 4096. The system can complete imaging in about 4.7 s at 100 MHz operating frequency.

Keywords: multi-channel SAR, FPGA, HLS, implementation

Classification: Integrated circuits

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1 Introduction
Space-borne Synthetic Aperture Radar (SAR) is an active microwave remote
sensing device with all-day, all-weather features in earth observation and has been
widely used in military and civilian areas. Traditional space-borne SAR can not
meet higher and higher index requirements due to azimuth ambiguities and range
ambiguities. Azimuth multi-channel technology is a major technical way to achieve
wide swath with high azimuth resolution, and it is a hot research topic of the new
generation space-borne SAR systems [1]. At present, there are three main types of

 technologies for implementing real-time SAR processing: large-scale Field Pro-

 grammable Gate Array (FPGA) technology, ASIC technology and DSP technology.
 However, in the case of on-orbit processing, an FPGA or an ASIC design is more
 suitable for special environments of satellites due to the harsh constraints of the
 severe size, weight, and power consumptions of the realization platform. FPGA and
 ASIC both have a powerful parallel signal processing capability. However, com-
 pared with an ASIC design, a design on an FPGA has excellent flexibility and cost-
 effective that makes it prominent in space-borne SAR imaging systems. In [2], the
classical Chirp Scaling (CS) imaging algorithm is completed with seven FPGAs.
The system takes about 33 s to complete imaging with a granularity of 16384 ×
16384 at the operating frequency of 100 MHz. Ming-ming Bian [3] uses FPGA to
complete the Range Doppler (RD) imaging algorithm.
At present, the most fundamental method of creating hardware design for
FPGA is by using hardware description languages Verilog or VHDL. And complex
timing state machine design is generally used for development within the FPGA,
which takes a lot of time to analyze and design. In order to get a better timing performance, the simulation and optimization are repeated which take more time. So if there is a tool that can be used to develop FPGA in C or C++ language, it will bring more efficiency to FPGA design. The Xilinx Vivado High-Level Synthesis (HLS) [4] tool can transform a C specification into register transfer level (RTL) implementation, and we can export RTL out as IP which can be used in Xilinx FPGA. C specifications can be written in C, C++, or SystemC language. Since we can develop algorithms at the C-level and verify them at the C-level, it greatly simplifies the design and debugging process, reduces the difficulty of development, and greatly improves the efficiency of FPGA development. The design can be modified according to the requirements and it is with high flexibility. In [5], the effectiveness of state-of-art C-to-FPGA synthesis solutions targeting multiple application domains is demonstrated, and the design productivity is improved. The 3G/4G wireless systems using an HLS methodology is mentioned in [6], which is with significantly improved productivity. In [7], the HLS tool is used to design the relative radiometric correction of remote sensing image, which verifies the high efficiency of developing FPGA based on HLS.

Considering the complexity of SAR imaging algorithm and the difficulty of developing FPGA with hardware description languages, a Vivado HLS tool is applied to design and implement a multi-channel stripmap SAR imaging system on an FPGA platform in this paper. And the imaging system is evaluated from aspects of image quality, system performance and resource utilization.

2 Multi-channel stripmap SAR algorithm

Multi-channel SAR imaging is based on a single transmitter for transmitting beam, and multiple receivers for receiving the beam. The multi-receiver beam reception mechanism enables wide swath with high azimuth resolution [8], and multi-channel mode has also become an important trend in the development of SAR imaging. However, the multi-receiver mode will result in azimuth non-uniform sampling which will lead to range cell migration and focus error, and it is a key problem in the imaging algorithm. Therefore, solving the azimuth non-uniform sampling is very crucial.

Before the standard imaging process, we need to overcome the azimuth non-uniform sampling problem. The inverse-filter method presented in [9] can perfectly recover the azimuth spectrum, effectively solving the problem of azimuth non-uniform sampling. And the inverse-filter method is also proposed in [10]. In this paper, we adopt inverse-filter method to realize the azimuth spectrum reconstruction. Combined with the classical CS algorithm [11], the multi-channel stripmap SAR imaging algorithm is completed and the corresponding imaging system is constructed. Fig. 1 shows the process of multi-channel stripmap imaging algorithms.
As can be seen from Fig. 1, multi-channel SAR imaging includes data preprocessing and standard imaging processing two parts. First, perform the data preprocessing and it consists of the following steps:

- Subtract direct current (DC) component of the SAR raw data;
- Transfer the multiple channel data to the Range-Doppler domain via FFTs in the azimuth direction and calculate channel phase error parameter;
- Calculate inverse-filter coefficient using the phase error parameter;
- Complete azimuth spectrum reconstruction by inverse-filter method.

Then it enters the standard CS imaging process. The standard CS imaging process consists of the following six process steps:

- In the Range-Doppler domain, the reconstruction data are multiplied by the Chirp Scaling factor, which is the 1st phase function in the CS algorithm. The 1st phase function is expressed as:

\[
\phi_1(\tau, f; r_{\text{ref}}) = \exp \left\{ -j \pi K_s(f; r_{\text{ref}}) C_s(f) \left[ \tau - \frac{2}{c} r_{\text{ref}} \left( 1 + C_s(f) \right) \right]^2 \right\} 
\]  

(1)

where \( f \) is the azimuth frequency, \( \tau \) is the range time, \( r_{\text{ref}} \) is the reference distance, \( K_s(f; r_{\text{ref}}) \) is the modulating frequency in the range direction, and \( C_s(f) \) is the curvature factor;

- The data are transformed to the two-dimensional frequency domain via a FFT in the range direction;

- Then the data are multiplied by the range compensation factor, which is the 2nd phase function in the CS algorithm. The 2nd phase function is expressed as:
\[
\phi_2(f, f; r_{ref}) = \exp \left\{ -j\pi \frac{f^2}{K_s(f; r_{ref})[1 + C_s(f)]} \right\} \cdot \exp \left\{ \frac{4\pi}{c} f r_{ref} C_s(f) \right\}
\]

where \( f \) is the range frequency. The first term of the expression completed the range compression, including the secondary range compression (SRC), and the second completed the range cell migration correction (SCRC);

- The data are transformed to Range-Doppler domain via an inverse FFT in the range direction;
- Then the data are multiplied by the azimuth compensation factor to complete the azimuth processing and phase correction. The azimuth compensation factor is the 3rd phase function in the CS algorithm. The 3rd phase function is expressed as:

\[
\phi_3(\tau, f; r_{ref}) = \exp \left\{ -\frac{2\pi}{\lambda} c t \left\{ 1 - \left[ 1 - \left( \frac{\lambda f}{2V(r = \tau c/2)} \right)^2 \right]^{1/2} \right\} \right\} + j\theta_{\Delta}(f; r)
\]

where \( \theta_{\Delta}(f; r) = \frac{4\pi}{\lambda} K_s(f; r_{ref})[1 + C_s(f)]C_s(f)(r - r_{ref})^2 \);
- An inverse FFT in the azimuth direction is executed, and focussed data are obtained.

3 Implementation of SAR imaging system

3.1 System architecture design

Through the analysis of the imaging flow, it is clear that FFT/IFFT operations account for the most of the system. Since the real-time requirements of FFT/IFFT operations are very high, we use Xilinx FFT IP cores to complete FFT operations. IFFT operation can be realized by exchanging the real and imaginary parts of the input and output data of FFT operation, so FFT IP core is also used to do IFFT operation. The other operations in the system are very complicated to design by using hardware description languages, so HLS tool is used to design and optimize them. And then, package them as HLS IP blocks and import them into Vivado Design Suite. Next, in the Vivado Design Suite, combine these HLS IP blocks with Xilinx FFT IP cores using the hardware description language to complete FPGA implementation. Fig. 2 shows block diagram of a two-channel stripmap SAR imaging system.

As can be seen from Fig. 2, the system includes HLS designs and Xilinx FFT IP cores. To accelerate the DC removal operation of two-channel raw data, we design two identical subtracting DC component modules for parallel processing. Phase error estimation 1 and phase error estimation 2 are designed to calculate phase error parameter among channels. Phase error estimation 1 is designed for the calculation of intermediate parameter and phase error estimation 2 is designed for the calculation of final phase error using the intermediate parameter. Because some intermediate parameters which are used to calculate 1st phase function, 2nd phase function, and 3rd phase function are the same, we design the parameter calculation module to get these parameters in advance. Two IEEE standard single precision floating-point Xilinx FFT IP cores are used to perform the parallel acceleration for the SAR imaging system and the FFT IP cores are set as pipeline mode.
3.2 Design and optimization of models on HLS

The design process of HLS can be divided into three main steps. Firstly, perform C simulation to verify the function of modules. And the C/C++ testbench is designed to ensure the correctness of the modules. In the case of ensuring the correctness of the modules function, C synthesis can be performed directly which can convert C/C++ model into RTL description. Finally, verify the RTL code with C/RTL co-simulation by using the optimized C/C++ code and the original test stimulus. Another step is exporting RTL as IP Catalog for system integration. HLS design flow is roughly shown as Fig. 3.

Because HLS supports the operation of C/C++/SystemC language, we propose C++ language to directly program the modules that designed on HLS, and optimize each module by modifying the directives until it meets the demand, and converts all the modules into RTL description. Finally package the RTLs output as IP blocks for SAR imaging system implementation.
Vivado HLS has different directives for optimizing the integrated process of the code to achieve different architectures, so the design has different running delays and resource consumption. According to different requirements, we can quickly reconfigure the function modules by modifying the related optimization directives or parameters, and regenerate the RTL code which is with great flexibility. Since the SAR imaging system requires high real-time, the PIPELINE, LOOP_MERGE, and ARRAY_PARTITION directives are mainly used to optimize the data throughput rate, reduce the delay and improve the performance of the modules. The target device XC7VX690T is selected in the design of modules and the clock period is 10 ns.

In the following, the main optimization directives used in the modules are described and the performance of some modules before and after the optimization is shown. It should be explained that the optimization results of each module are mostly the effect of multiple optimization directives.

(a) PIPELINE directive
Pipeline design is an important factor affecting the performance of a design. In C/C++ based design of HLS, multiple executions of a task are performed sequentially without the PIPELINE directive. Instruct a task to execute in a pipeline, allowing the next execution of the task to begin before the current execution is completed. It reduces the initiation interval by allowing the concurrent execution of operations within a loop or function. This directive is used in loops or functions in the modules designed on HLS and is optimized by setting the processing latency of the pipeline sub-steps. Take phase function generation calculation module as an example to illustrate the effect of PIPELINE directive. Table I and Table II respectively show the performance and resource utilization of 1st phase function, 2nd phase function and 3rd phase function generation calculation modules before and after optimization.

<table>
<thead>
<tr>
<th>Modules</th>
<th>Latency</th>
<th>Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Before</td>
<td>After</td>
</tr>
<tr>
<td>1st phase function</td>
<td>86017</td>
<td>4117</td>
</tr>
<tr>
<td>2nd phase function</td>
<td>507939</td>
<td>16449</td>
</tr>
<tr>
<td>3rd phase function</td>
<td>758083</td>
<td>8534</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Modules</th>
<th>Optimization</th>
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<th>DSP48E</th>
<th>FF</th>
<th>LUT</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st phase function</td>
<td>Before</td>
<td>0</td>
<td>16</td>
<td>1231</td>
<td>1204</td>
</tr>
<tr>
<td>function</td>
<td>After</td>
<td>0</td>
<td>35</td>
<td>2295</td>
<td>1769</td>
</tr>
<tr>
<td>2nd phase function</td>
<td>Before</td>
<td>0</td>
<td>41</td>
<td>6693</td>
<td>10182</td>
</tr>
<tr>
<td>function</td>
<td>After</td>
<td>0</td>
<td>58</td>
<td>8339</td>
<td>12124</td>
</tr>
<tr>
<td>3rd phase function</td>
<td>Before</td>
<td>16</td>
<td>44</td>
<td>11253</td>
<td>16442</td>
</tr>
<tr>
<td>function</td>
<td>After</td>
<td>16</td>
<td>207</td>
<td>29140</td>
<td>42853</td>
</tr>
</tbody>
</table>
(b) LOOP MERGE directive

By default, HLS performs multiple consecutive loops sequentially. With LOOP MERGE directive, multiple loops can be implemented in parallel which can reduce overall latency, increase sharing and improve logic optimization. The directive can’t be used if there is data dependency among loops. Besides, loops cannot be merged when they contain FIFO reads. Merging changes the order of the reads, however reads from a FIFO or FIFO interface must always be in sequence. Take phase error estimation 1 module as an example to illustrate the effect of LOOP MERGE directive. Its performance and resource utilization before and after optimization of LOOP MERGE directive are shown in Table III and Table IV.

<table>
<thead>
<tr>
<th>Modules</th>
<th>Latency</th>
<th>Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Before</td>
<td>After</td>
</tr>
<tr>
<td>Phase error estimation 1</td>
<td>16415</td>
<td>8211</td>
</tr>
</tbody>
</table>

Table IV. Resource utilization comparison of phase error estimation 1 module before and after optimization

<table>
<thead>
<tr>
<th>BRAM</th>
<th>DSP48E</th>
<th>FF</th>
<th>LUT</th>
</tr>
</thead>
<tbody>
<tr>
<td>Before</td>
<td>0</td>
<td>20</td>
<td>4551</td>
</tr>
<tr>
<td>After</td>
<td>0</td>
<td>23</td>
<td>4505</td>
</tr>
</tbody>
</table>

(c) ARRAY PARTITION directive

In the optimization of algorithms, PIPELINE directive which is commonly used to improve performance is often limited because of the inability to satisfy multiple accesses to an array at the same time, and the optimization effect is affected. ARRAY PARTITION directive can partition large arrays into multiple smaller arrays or into individual registers, improving access to data and remove block RAM bottlenecks. HLS provides three types of array partitioning: block, cyclic and complete. According to different rules and needs of algorithms, select an appropriate array partitioning type. ARRAY PARTITION directive is usually applied with other directives, and it helps in reducing latency.

Subtracting DC data module, parameter calculation module, phase error estimation 2 module and inverse-filter coefficient calculation module use one or two or three directives shown above. Specific optimization is no longer shown one by one and Table V shows the usage of directives on modules.

<table>
<thead>
<tr>
<th>Modules</th>
<th>PIPELINE</th>
<th>LOOP MERGE</th>
<th>ARRAY PARTITION</th>
</tr>
</thead>
<tbody>
<tr>
<td>Subtracting DC data</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1st phase function</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2nd phase function</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3rd phase function</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Parameter calculation</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>Phase error estimation 1</td>
<td>✓</td>
<td>✓</td>
<td></td>
</tr>
<tr>
<td>Phase error estimation 2</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Inverse-filter coefficient</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
As can be seen from the performance and resource utilization of each module before and after the optimization, the latency and throughput of each module has greatly improved, and resource utilization has increased a little. Considering the high real-time requirements of real-time imaging system, it is paramount to meet the performance requirements in the optimization process and the increment in resource utilization is allowed as long as it is within acceptable limits. Therefore, the modules designed with HLS meets the requirements.

3.3 Real-time performance analysis

The architecture of the imaging system mentioned in section 3.1 is based on a combination of HLS-design IP blocks and FFT IP cores. If the entire system is divided on a time scale, it can be divided into three large modules. As shown in Fig. 4, the three modules are azimuth spectrum reconstruction, range data processing and azimuth data processing, which belong to a serial operation in time. That is, all data of the current module is processed before the data processing of the next module can be performed.

The real-time performance analysis of a two-channel SAR imaging system by processing SAR raw data with a granularity of \( \frac{16384}{4096} \) is shown below. As we know, the data available to a SAR processor are an ensemble of two-dimensional dispersed signals. We assume that \( N_A \) represents sampling points in azimuth direction of raw data, \( N_A \) represents sampling points in azimuth direction of data after spectrum reconstruction, and \( N_R \) represents sampling points in range direction. Based on the assumption, \( N_A \) is equal to 2048, \( N_A \) is equal to 4096 and \( N_R \) is equal to 16384. The device model used in this paper is Xilinx XC7VX690T, instantiating two FFT IP cores in the device for parallel processing.

(a) Analysis of stage ①

Firstly, subtract the DC component from SAR raw data, and we design and package

Fig. 4. Real-time imaging system analysis process
two IP blocks to ensure that two-channel data can be processed in parallel, which consumes nearly 1.5 s. Then the processing of the data is partitioned into two parallel branches. One branch, calculate phase error parameter between the two channels using all the data. The other branch, execute NR times azimuth NA-point FFT individually with two FFT IP cores. The speed of the FFT operation is faster, so the delay of this part depends on the calculation of phase error parameter. When the two-channel phase error parameters are obtained, the calculation of inverse-filter coefficients are begun to be executed. This section is executed sequentially, with a total delay of approximately 1.5 s. After that, the filtering operation is performed. Two pieces of NA-point data execute filtering operation at the same time to get a piece of NA-point data, and then the data are multiplied by the 1st phase function. The filtering operation can be parallelized with the calculation of the 1st phase function. Since the speed of the calculation of 1st phase function is slower, the delay depends on the 1st phase function part. The partial delay is about 0.5 s, and the azimuth processing completes.

(b) Analysis of stage ②

After the azimuth data processing is finished, the range operation is performed. This section is a part of the flow of the classical CS imaging algorithm. The FFT operation in the range direction is executed and then the data are multiplied by the 2nd phase function, and finally the inverse FFT is executed in the range direction. This part we uses two FFT IP cores with the pipeline structure. In this case, for NR-point FFT processing, it takes approximately NR clock cycles to receive data, NR clock cycles to process data and NR clock cycles to release Data. And multiple pieces of data can be pipelined with the pipeline structure. Considering that the computational delay of one piece of 2nd phase function is about 16449 clock cycles, it is obviously not enough to update one piece of 2nd phase function per piece of data. In order to make the computational speed of 2nd phase function match with FFT operation, we propose a method that every four pieces of data share one piece of the 2nd phase function and adopt the ping/pong memory group as caches for the 2nd phase function. Since two FFT IP cores are used to process two pieces of data in parallel, it means that we update one piece of the 2nd phase function every two pieces of data for one FFT IP core. This method has been verified to have little effect on imaging quality, and the 2nd phase function computational speed can match with the FFT operation. In this case, the total delay depends on the FFT operation, and the total processing time of NA pieces of data takes about 0.35 s. After that, the inverse FFT operation in the range direction is executed with the latency of about 0.35 s.

(c) Analysis of stage ③

The data are multiplied by the 3rd phase function, and then the inverse FFT in the azimuth direction is executed. The time schedule of this part is similar to the range operation. The difference is that the inverse FFT operation in the azimuth direction can be executed only after the data have been multiplied by the 3rd phase function. In order to match the speed of the calculation of the 3rd phase function to the inverse FFT operation, we propose a method that every six pieces of data share one piece of the 3rd phase function, which means that one piece of the 3rd phase function is updated for every three pieces of data for one FFT IP core, and it has no
effect on imaging quality. The partial delay is the sum of the latency of the first piece of the 3rd phase function calculation and the inverse FFT operation, which is about 0.35 s.

4 Results

The two-channel stripmap SAR imaging system is validated by processing SAR raw data with a granularity of $16384 \times 4096$. The raw data are represented in a single precision floating point complex form with 64 bit (32 bit for the real part and for the imaginary part, respectively) for each sample data point. The Xilinx XC7VX690T FPGA is used as the platform of the imaging node, and two FFT IP cores are adopted for parallel processing. The imaging system is evaluated from three aspects: image quality, performance and resource utilization. Fig. 5 is a point target image, which is imaged by the two-channel stripmap SAR imaging system. And the horizontal direction is the range direction and the vertical direction is the azimuth direction.

![Point target image](image)

Fig. 5. Point target image

Peak side-lobe ratio (PSLR), integrated side-lobe ratio (ISLR) and spatial resolution (RES) are used to evaluate the point target. R represents the range direction and A represents the azimuth direction. During the imaging process, a two-dimensional windowing process was performed with a $-30$ dB Taylor window. As can be seen from Table VI, the comparison between the two cases does not differ widely, which validates that the proposed imaging system is able to provide sufficient accuracy for point target imaging.

<table>
<thead>
<tr>
<th>Platform</th>
<th>R PSLR (dB)</th>
<th>R ISLR (dB)</th>
<th>R RES (m)</th>
<th>A PSLR (dB)</th>
<th>A ISLR (dB)</th>
<th>A RES (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FPGA</td>
<td>$-29.69$</td>
<td>$-24.86$</td>
<td>1.52</td>
<td>$-28.95$</td>
<td>$-24.37$</td>
<td>1.05</td>
</tr>
<tr>
<td>Matlab</td>
<td>$-29.72$</td>
<td>$-24.89$</td>
<td>1.50</td>
<td>$-29.02$</td>
<td>$-24.46$</td>
<td>1.03</td>
</tr>
</tbody>
</table>

Through recording the numbers of clock cycles, it takes 4.7 s for the system to process SAR raw data with $16384 \times 4096$ data granularity at the operating frequency of 100 MHz. Table VII shows the resource utilization of $16384 \times 4096$ sample points processed by the proposed imaging system.

Table VIII shows a comparison with previous works. Compared with [13, 14], taking into account the data granularity processed, the proposed system shows advantages in processing time. Reference [12] describes a stripmap SAR system...
and it takes 12.1 s to process stripmap SAR raw data with a granularity of 16384 \times 16384. Since the system we designed is a two-channel stripmap SAR imaging system, the inverse-filter method is executed to complete data preprocessing which consumes more time than that of stripmap SAR imaging system. Taking into account the data granularity and the complexity of the algorithm, the processing time of reference [12] is comparable to ours. And the resource utilization of our design is acceptable.

In summary, the proposed design achieves a good tradeoff between real-time performance and resource utilization. The entire design takes 12 weeks from initial software code simulation to the final imaging, and it demonstrates that HLS can improve the design productivity.

5 Conclusion

Vivado HLS tool is applied to design and implement a multi-channel stripmap SAR imaging system on an FPGA platform. And a two-channel imaging system is implemented on Xilinx XC7VX690T FPGA platform by combining HLS designs and FFT IP cores. The modules designed on HLS are optimized and packaged as IP blocks for FPGA implementation. The proposed system takes 4.7 s to process SAR raw data with 16384 \times 4096 data granularity. And the image quality and resource utilization of the system is acceptable. Designing on the basis of existing reliable software codes on HLS reduces the difficulty of FPGA development and accelerates the implementation of a multi-channel stripmap SAR imaging system. The evaluation of the SAR imaging system illustrates the effectiveness of HLS as a flexible design tool for FPGA implementation.

Acknowledgments

This work was supported by the National Natural Science Foundation of China under Grant 91438203, the Chang Jiang Scholars Program under Grant T2012122 and the Hundred Leading Talent Project of Beijing Science and Technology under Grant Z141101001514005.