Source process of the 1923 Kanto earthquake inferred from historical geodetic, teleseismic, and strong motion data

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The historical geodetic and teleseismic data are jointly inverted for the rupture process of the 1923 Kanto earthquake together with the strong motion data recently discovered. The resultant slip distribution shows two asperities (areas of large slips) on the fault plane with a total seismic moment of $1.1 \times 10^{21}$ Nm ($M_w$ 8.0). The asperity in the shallow central portion of the fault is larger with maximum slip of approximately 10 m than the one in the hypocentral region. The recovered slip functions indicate that the initial slip was abrupt in the hypocentral asperity, though it was gradual in the larger asperity. The major discrepancies between the observations and synthetics are attributed to volcanic activities and the 3-D structure of the Kanto Basin. We compare the slip and aftershock distributions and also discuss the relation of the asperities to silent earthquakes.

Key words: The 1923 Kanto earthquake, source process, asperity.

1. Introduction

The September 1, 1923, Kanto earthquake is one of the most devastating earthquakes in history, causing severe damage and more than 100,000 fatalities in the Tokyo metropolitan area. This earthquake is an interplate event along the Sagami trough where the Philippine Sea plate is subducting beneath a continental plate (Fig. 1). Geomorphological studies suggested that similar great earthquakes have recurred along the Sagami trough during at least the last 6000 years (e.g., Sugimura and Naruse, 1954; Matsuda et al., 1978). Therefore, it is important to understand the detailed source process of the 1923 Kanto earthquake even for the prediction of the strong ground motions from a great future earthquake.

Many seismological and geodetical studies have been carried out for this earthquake. Kanamori and Miyamura (1970) located its hypocenter around the base of the Izu Peninsula from $P$-wave arrival times. Kanamori (1971) determined the focal mechanism to be right-lateral reverse faulting on a fault plane striking N70° W from $P$-wave polarity data and the seismic moment to be $7.6 \times 10^{20}$ Nm ($M_w$ 7.9) from surface wave amplitudes. Matsu’ura et al. (1980) and Matsu’ura and Iwasaki (1983) applied an inversion method to the geodetic data to obtain the fault parameters. Their models are consistent with the above focal mechanism by Kanamori (1971). The geodetic and teleseismic data were simultaneously inverted by Wald and Somerville (1995). Their solution shows two asperities (areas of large slips), one near the hypocenter and another shallower in the southeast of the first.

Recently, engineering seismologists (e.g., Yokota et al., 1989; Takemura et al., 1994) have retrieved some regional seismograms from all over Japan, or restored clipped strong motion records observed at Tokyo. We combined these strong motion data with the teleseismic and geodetic data, and applied a joint inversion method to them for a detailed image of the source process.

2. Data

The geodetic and teleseismic datasets are the almost same as those of Wald and Somerville (1995). The Military Land Survey (1930) conducted leveling and triangulation for preseismic (1884–1898, 1884–1899) and postseismic periods (1923–1927, 1924–1925). The horizontal and vertical geodetic displacements caused by the 1923 Kanto earthquake were obtained from comparisons of the preseismic and postseismic measurements. The horizontal displacements were revised by Sato and Ichihara (1971), so we use their revised displacements. The vertical displacements and station coordinates were read from a map of the Military Land Survey (1930). These horizontal and vertical displacements are shown in Fig. 2, where we can find two zones of large vertical displacements and relate them with the asperities by Wald and Somerville (1995).

Teleseismic data recorded in USA, Europe, and Australia were collected by Kanamori (1971) and digitized by Wald and Somerville (1995). Figure 3(a) shows the location and azimuthal coverage of the teleseismic stations where useful records were observed. The records were bandpass-filtered between 0.02 and 0.4 Hz, and resampled at a rate of 1.0 Hz. The instrumental responses were deconvolved and a common instrumental response convolved in as was done by Wald and Somerville (1995). We will convolve the Green’s functions with the common response in our procedure of a joint inversion.

Strong motion data recorded at observatories of the Japan Meteorological Agency (JMA) and Tohoku Imperial Uni-
University (predecessor of the present Tohoku University) at Sendai were collected by Takemura and his colleagues (Takemura, 1994; Takemura et al., 1994, 1995; Takemura and Nozawa, 1996a, b, 1998). They are available on the web site (Kajima Corporation, 2003). We chose the data observed by the Imamura-type strong motion seismographs, whose stations are plotted in Fig. 3(b). The data are bandpass-filtered between 0.05 and 0.5 Hz and resampled at a rate of 2 Hz. The instrumental responses were also investigated by Takemura and his colleagues, but we do not deconvolve the instrumental response from the data, so that we will calculate their Green’s functions including the response. Note that the later part of the NS component at the Gifu station was clipped off.

In the Tokyo Imperial University (predecessor of the University of Tokyo) at Hongo, Tokyo, the strong motion data were recorded by Omori-, Imamura-, and Ewing-type seismographs. The Ewing seismogram, and the EW component of the Imamura seismogram were restored to ground motions by Morioka (1976, 1980) and Yokota et al. (1989), respectively. However, these restored seismograms have significant differences. The previous study of forward modeling (Sato et al., 1999) showed that the Ewing seismogram, which is dominated by long-period oscillations with a period of 13 s, cannot be explained by the strong motion simulation. On the other hand, the Imamura seismogram is consistent with the simulation results, so we use only the Imamura seismogram for the Hongo station.

Since Yokota et al. (1989) also found the accurate direction of the EW component to be E 13° N, we will calculate the Green’s function in this direction. In addition, Yokota et al. (1989) showed that the seismogram was adequately restored but its amplitude could be underestimated by 15%, and so we scale it up by 15% for the inversion.
3. Method

For the fault geometry we adopt the model of Wald and Somerville (1995), which was constructed based on Kanamori (1971) and Matsu’ura et al. (1980). The fault parameters of the model are listed in Table 1. The length in the strike direction is 130 km, and the width in the dip direction is 70 km. We divided the fault into seventy 13 km subfaults and made the slip direction at each subfault variable using a combination of 90° and 180° slips.

The Green’s functions for the geodetic data were calculated by the method of Yabuki and Matsu’ura (1992) in a halfspace medium with a Poisson’s ratio of 1/4. We assume that the halfspace medium has a rigidity of 30 GPa when we estimate seismic moments. The Green’s functions for the teleseismic data were calculated by a ray theory with a layer-averated isotropic PREM and the attenuation time constants (τ)** of 1 s (for P-waves) and 4 s (for SH-waves). For strong motion data we used the reflectivity method of Kohketsu et al. (1985) with the 1-D layered structures of Sato et al. (1998a).

We then apply the joint inversion method developed by Yoshida and Koketsu (1990) and Yoshida et al. (1996) to the geodetic, teleseismic and strong motion data. The k-th component of the waveforms $F_k$ at station $x_j$ and at time $t_l$ is represented by

$$F_k(t_l, x_j) = \sum_{mn} X_{mn} f_{mnk}(t_l - (l - 1)\tau - T_{mn}, x_j) + \sum_{mn} Y_{mn} g_{mnk}(t_l - (l - 1)\tau - T_{mn}, x_j),$$

where $f_{mnk}$ and $g_{mnk}$ are the k-th components of the seismic Green’s functions for the mn-th subfault with unit slip in the directions of 90° and 180°, respectively. $X_{mn}$ and $Y_{mn}$ are the slip components in the mn-th subfault. The rupture front reaches the mn-th subfault at $T_{mn}$. The source time function of a point source is composed of sequential ramp functions with a rise time $\tau$, so that the l-th ramp function arises at $T_{mn} + (l - 1)\tau$. The k-th component of the static displacement $U_k$ at station $x_j$ is independent of time, and so it is represented by

$$U_k(x_j) = \sum_{mn} \left( \sum_l X_{mn} \right) u_{mnk}(x_j) + \sum_{mn} \left( \sum_l Y_{mn} \right) v_{mnk}(x_j),$$

where $u_{mnk}$ and $v_{mnk}$ are the k-th components of the geodetic Green’s functions for the mn-th subfault with unit slip in the directions of 90° and 180°, respectively. For the calculation of $u_{mnk}$ and $v_{mnk}$, we distributed 8 x 8 virtual sources and average their displacements for the central point source on each subfault.

We incorporate the positivity and smoothing constrains into the inversion for suppressing numerical instability. The positivity constraint is realized by the penalty functions $1/\sqrt{X_{mn}}$ and $1/\sqrt{Y_{mn}}$, which can grow rapidly if $X_{mn}$ and $Y_{mn}$ approach to zero. The discrete Laplacian operator defined as

$$\nabla^2 X_{mn} = X_{m+1,n,l} + X_{m,n+1,l} + X_{m,n,l+1} + X_{m,n,l} - 6X_{m,n,l}$$

is introduced for the smoothing constraint. We determine the relative weights of the geodetic and seismic datasets and the constraints in the inversion following Wald and Somerville (1995) with some considerations mentioned later.

4. Inversion Results

4.1 Inversion of geodetic data alone

We first inverted the geodetic data alone. Figure 4 shows the resultant slip distribution and compares the observed and calculated displacements. This solution indicates two asperities, one near the hypocenter around the base of the
Izu Peninsula and another on the shallow, eastern part of the fault plane around the Uruga Strait between the Miura and Boso Peninsulas. Their maximum slips are 8.6 m and 8.5 m, respectively. The slip direction changes from predominantly right-lateral strike slip around the hypocentral region to near dip slip in the eastern asperity. These features of the slip distribution are consistent with the result of Wald and Somerville (1995). The calculated displacements are in good agreement with the observed ones as shown in Fig. 4. The two peaks of uplifts have been inverted into the asperities mentioned above. The small descents in the Kanto Basin and along the northern coast of the Tokyo Bay constrain the extents of the asperities.

We note significant discrepancies between the observed and calculated horizontal displacements at the Izu-Oshima station. They cannot be reduced, even if we apply a heavier weight to this 1.8 m displacement during the inversion. Since only this station and another in the Izu Peninsula are located on the Philippine Sea plate and the postseismic survey was carried out about 25 years after the preseismic one, it is plausible that the discrepancies may be caused by the plate motion. However, the relative motion of the Philippine
Sea plate to the continental plate is 2–3 cm/yr to the north-west (Sagiya, 1999; Heki and Miyazaki, 2001), so that the total movement during the period amounts to 50–75 cm, which is only a third of the observed horizontal displacement. We have to find other causes for the remaining two thirds. Izu-Oshima is a volcanic island, which erupted in 1910 (volume of erupted solid material $1 \times 10^5$ m$^3$), 1912–1914 ($3.3 \times 10^7$ m$^3$), and 1921–1922 ($1 \times 10^5$ m$^3$), according to Nakamura (1964). These volcanic activities may have resulted in these two thirds.

4.2 Joint inversions

We next inverted the geodetic and teleseismic data simultaneously (Fig. 5). The temporal feature of the source process was introduced by the source time function consisting
of seven ramp functions with a rise time of 1.5 s. We carried out the inversion with the rupture front velocities between 2.5 and 4.0 km/s, and chose a velocity of 2.6 km/s which minimizes the variance.

Since we cannot expect exact information on timing and instrumental responses of historical seismograms, we chose a heavier weight for the geodetic data than that for the seismograms to obtain a stable solution. In spite of this lower weight, the seismograms are well recovered as shown in Fig. 5(b). The resultant slip distribution in Fig. 5(a) is mostly similar to that of the geodetic inversion, though the western asperity near the hypocenter is somewhat weakened. The eastern asperity with a maximum slip of 9.2 m becomes larger than the western one, and the total seismic
The moment is $1.0 \times 10^{21}$ Nm ($M_w$ 7.9). The slip velocity functions in Fig. 5(c) indicate that the seismic moment in the first (western) asperity was released more rapidly than those in the second (eastern) asperity. This feature was also found by Wald and Somerville (1995).

We finally inverted the geodetic, teleseismic and strong motion data all together (Fig. 6). In this case, we increased the number of ramp functions from seven to ten, because a preliminary inversion with seven functions showed that slips in the eastern asperity were still large at the seventh function. The best rupture front velocity was not changed after the strong motion dataset were added.

Compared with the results of the two-fold joint inversion without the strong motion dataset or the results of Wald and Somerville (1995), the asperities have been intensified and the area of the eastern asperity has been expanded to
the north in this final model of the slip distribution. The maximum slip and total moment increase from 9.2 m and \(1.0 \times 10^{21}\) Nm (\(M_w 7.9\)) to 10.0 m and \(1.1 \times 10^{21}\) Nm (\(M_w 8.0\)), respectively. In other words, the larger slips are required for recovering the amplitudes of the strong motions. The synthetic teleseismic waveforms keep good agreement with the observed ones.

In the resultant slip velocity functions (Fig. 6(c)), the above feature (abrupt rise of the moment release in the first asperity, and gradual rise in the second one) appears less distinct than in those from the geodetic and teleseismic data. However, we can still say that the initial rises in the first asperity are more rapid than those in the second one.

Although most of the seismic data are well recovered, the coda part of the synthetic seismogram at Hongo is not in good agreement with the observed one. The large coda wave train cannot be reproduced by using a 1-D structure, even if the structure contains soft, thick sediments (e.g., Sato et al., 1998b). Forward modeling with a 3-D structure (Sato et al., 1999) showed that surface waves excited along the boundary between the Kanto Mountains and Kanto Basin (Fig. 1) can explain the large coda at Hongo.

Figure 7 represents the growth of the rupture by showing the slip-rate distributions every 4 s. If we compare the distribution from the three-fold joint inversion with the strong motion dataset with the one from the two-fold joint inversion without the strong motion dataset, we can find details of the source process in the former including the shorter-length features. This implies that the strong motion data provided us with much more information on the source time function than the teleseismic data, and we inferred a clearer image of the rupture process from them.

5. Discussion

Hamada et al. (2001) precisely relocated the hypocenters of aftershocks of the 1923 Kanto earthquake. Figure 8(a) shows the epicenters of the aftershocks with horizontal errors less than 10 km in three years after the main shock. The comparison between the aftershock and the present slip distributions suggests few aftershocks around the larger eastern asperity as expected from the established theory on aftershock patterns and main shock faulting (e.g., Mendoza and Harzell, 1988). However, many small aftershocks occurred in and around the western asperity. A possible reason for this contradiction may be that the rupture in the western asperity was not completed during the main shock. Ito et al. (2004) and Yagi (2004) found that the aftershocks of the 2003 Tokachi-oki earthquake did not occur on the surface of the Pacific slab in the asperity regions, but within the plates above and below the asperity regions. Thus it might also be possible that the aftershocks in the western asperity of the 1923 Kanto earthquake were intraplate events, but we cannot show any evidence because the focal depths of the aftershocks were not well determined. Figure 8(b) represents the recent seismicity in 2000–2003, showing events shallower than 50 km with magnitudes larger than 2.0. We still find null seismicity in the eastern asperity. The seismicity in the western asperity becomes lower, suggesting that the coupling between the slab and continental plate is getting recovered there.

Silent earthquakes (aseismic slip events) have recently been detected thanks to the development of the continuous crustal tilts observation and Global Positioning System (GPS) network. In the Kanto region, Hirose et al. (2000), Ozawa et al. (2003), and Sagiya (2004) found such events in 1989, 1996, and 2002. Their source regions are located in the middle part of the Tokyo Bay or in the east of the
Fig. 9. Results from inversions of the geodetic data using the Green's functions for a 1-D layered structure. (a) Slip distribution. (b) Observed (up: red, down: blue) and calculated (black) vertical displacements. (c) Observed (green) and calculated (black) horizontal displacements. The variance reduction for geodetic data is 0.96.

Boso Peninsula neighboring the eastern asperity as shown in Fig. 8(b). Similar silent earthquakes adjacent to asperities of large earthquakes have also been found in other regions (Yagi and Kikuchi, 2003), and so it may imply an important process during earthquake cycles.

We assessed the effect of Green's functions calculated for a 1-D layered structure on the inversion of geodetic data alone. We used the same structure model as that used for the strong motion data at Hongo (Sato et al., 1998a). The frequency-wavenumber method of Zhu and Rivera (2002) is used to calculate the Green's functions for the geodetic data. Figure 9 shows the result with the 1-D Green's functions. The soft sedimentary layer in the 1-D structure increases the displacements, so that the 1-D Green's functions reduced the slip amounts. The maximum slips in the western and eastern asperities decreased from 8.6 m and 8.5 m to 6.9 m and 7.5 m, respectively. The total seismic moment, however, increased from $9.2 \times 10^{20}$ Nm to $9.7 \times 10^{20}$ Nm, because the rigidities at depths of 12–34 km are 39–46 GPa, which are higher than that of 30 GPa for the halfspace model (the rigidity at depths of 3–12 km is 29 GPa, which differs little from that for the halfspace model). The variance reduction was not changed. These effects may be applicable to the results of the joint inversions. We used a 1-D model in this assessment, the real structure in the Kanto region should be three-dimensionally complex as suggested by the geographical setting in Fig. 1. The Green's functions for this 3-D structure are necessary in the next stage of our study.

6. Conclusion
We carried out a joint inversion of geodetic, teleseismic and strong motion data for the source process of the 1923 Kanto earthquake. There are two asperities (areas of large slips) in the resultant slip distribution. The new strong motion data improved the resolution, so that the asperities were intensified with longer rupture duration and the eastern asperity was recovered with a larger area than in the result of the two-fold joint inversion of the geodetic and teleseismic data or the result of Wald and Somerville (1995). The maximum slip is 10.0 m and the total seismic moment is $1.1 \times 10^{21}$ Nm ($M_w$ 8.0), while the two-fold joint inversion recovered the maximum slip of 9.2 m and the moment of $1.0 \times 10^{21}$ Nm ($M_w$ 7.9). The recovered slip functions
indicate that the initial rise was abrupt in the western asperity, while it was gradual in the eastern asperity. There are very few aftershocks in the eastern asperities, though many small aftershocks occurred in and around the western asperity. The source regions of the 1989, 1996, and 2002 silent earthquakes are located in the zones neighboring the eastern asperity.

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