Preliminary Design of an Augmented Railgun
Influence of the Dimensions of the Outer Rails on the Forces Acting on the Projectile and the Rails

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Keywords : rail launchers, electromagnetic forces, ANSYS

Railguns are electromagnetic launch systems which have the potential to accelerate projectiles to velocities higher than 2 km/s. The acceleration of the projectile is the result of the interaction of the current through the brush armature with the magnetic field induced by the current in the rails. For a conventional railgun, raising the current is the best way to increase the electromagnetic force on the projectile. The current density however is limited: the heating of the sliding contacts between the rails and the brush armatures due to the Joule-effect and to the friction can cause the melting of these contacts. One way to increase the acceleration without raising the current through the projectile is by adding an extra pair of rails in order to establish an additional magnetic field. The EM force on the projectile for an augmented railgun is described by the force-equation:

\[ F_{\text{EM}} = \frac{1}{2} L'R h^2 + M'I A \]  

(1)

The first term represents the influence of the magnetic field induced by the current in the inner rails and is proportional to the self-inductance gradient \( L'_R \). The second term describes the influence of an additional magnetic field and is proportional to the mutual inductance gradient \( M' \). \( I_R \) and \( I_A \) are respectively the currents in the inner and outer rail.

The objectives of this preliminary study are to design an augmented railgun capable of accelerating projectiles with a mass of 100 to 200 g to a velocity of 1 to 2 km/s, with the condition that the EM forces on the rails must be limited to 8 MN/m.

The finite element code ANSYS was used for the simulation of the magnetic fields. Three current ratios were used for the simulations. The forces acting on the rails are determined with a 2D transient analysis. The EM force on the projectile is analytically calculated with the force-equation. Therefore values of \( L'_R \) and \( M' \) are determined with a 3D AC-analysis at frequencies of 10 Hz and 1 kHz. For each geometry and frequency the EM force for the three current ratios were determined. The force-equation (1) is then used to determine \( L'_R \) and \( M' \) for each geometry at both frequencies by fitting (1). The EM force on the projectile calculated with a 3D transient analysis was then compared with the analytically determined results for the same geometry and currents (Fig. 1). The results of the transient analysis are first in good agreement with the results calculated for 1 kHz, then decrease to converge with the results for 10 Hz. The fitted curve calculated with the values of the inductances linearly decreasing from the values calculated for 1 kHz at 0.3ms to the values for 10 Hz at 2.0 ms, shows a good overall agreement. This method is used to calculate the EM forces for the different geometries.

The EM forces on the rails and on the projectile are increasing with decreasing distance between the rails \( a \) and height \( h \). The force on the projectile is decreasing faster for increasing \( a \) and \( h \) then the force on the rails. The best ratio of the EM force on the projectile and the EM forces on the rails is found at \( a = 2 \text{ mm} \) and \( h = 2 \text{ mm} \). The optimal width \( b \) is not so easy to find. The maximal EM force on the projectile for \( a = 2 \text{ mm} \) and \( h = 2 \text{ mm} \) is found at 8 mm for all current ratios. The maximum of the EM force on the rails depends on the current ratio. Another point of interest is the EM forces on the inner rails. If \( b \) is chosen too small, we will need a high current in the inner rails to avoid EM forces on the inner rails that point forwards. We have chosen \( b = 8 \text{ mm} \) to optimize the EM force on the projectile.

To obtain a muzzle velocity of 1 km/s for a projectile of 200 g or a muzzle velocity of 2 km/s for a projectile of 100 g, the impulse on the projectile must be 200 Ns. Therefore the current ratios needed to obtain this impulse for the best theoretical geometry were determined. The inner current was varied between 300 and 600 kA and the corresponding outer current was calculated (Table 1). The EM forces on the rails decrease with an increasing current in the inner rails. We choose the current ratio with the lowest inner current wherefore the EM force on the rails is smaller than 8 MN/m. But for the current ratio 400 kA/1030 kA, the EM force on the inner rails points inwards. Therefore the current ratio 450 kA/857 kA is chosen as solution.

The obtained solution for an impulse of 200 Ns is a theoretical solution based upon the EM forces on the rails and on the projectile. Other criteria have to be considered for the final construction.

Table 1. Current ratios calculated to determine an impulse on the projectile of 200 Ns for the theoretically best geometry and the corresponding maximum total EM forces on the rails

<table>
<thead>
<tr>
<th>IR (kA)</th>
<th>300</th>
<th>350</th>
<th>400</th>
<th>450</th>
<th>500</th>
<th>550</th>
<th>600</th>
</tr>
</thead>
<tbody>
<tr>
<td>IA (kA)</td>
<td>1518</td>
<td>1243</td>
<td>1030</td>
<td>937</td>
<td>857</td>
<td>773</td>
<td>699</td>
</tr>
<tr>
<td>F (MN/m)</td>
<td>11.9</td>
<td>9.2</td>
<td>7.5</td>
<td>6.3</td>
<td>5.5</td>
<td>4.9</td>
<td>4.5</td>
</tr>
</tbody>
</table>

Fig. 1. EM force on the projectile: Fitting of the analytically calculated results to the EM force determined with a 3D transient analysis

References

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Influence of the Dimensions of the Outer Rails on the Forces Acting on the Projectile and the Rails

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For the preliminary design of an augmented railgun, the electromagnetic repulsive forces on the rails and the self and mutual inductance gradients were determined by simulation. This design is meant for the realization of an augmented railgun at the French-German Research Institute in Saint-Louis, France. The simulated railgun has a 25 mm × 25 mm square calibre and both the inner and outer rails have a rectangular cross-section. In our study the geometry of the inner rails is fixed while the dimensions of the outer rails were altered. A 2D transient analysis for the determination of the magnetic forces on the rails was carried out with the finite element method program ANSYS. The EM force on the projectile is analytically calculated with the force-equation based on values of the inductance gradients determined with 3D AC-analyses. The influence of the ratio between the currents in the inner and outer rails on the electromagnetic forces has also been investigated. We have shown that the EM force acting on the projectile increases when the height of the outer rails and the distance between the inner and outer rails decrease. However this also leads to higher repulsive forces between the rails. For the theoretically best geometry, based on the electromagnetic forces, a 3D transient analysis was carried out. The electromagnetic force determined directly with the 3D transient analysis is then compared with the one obtained with the analytical method. A good agreement was found.

Keywords: rail launchers, electromagnetic forces, ANSYS

1. Introduction

Compared with conventional guns, electromagnetic guns have a high muzzle velocity. Another advantage is the decrease in vulnerability due to the absence of powder. Throughout the years many different types of EM guns and energy storage have been developed. An overview can be found in Ref. (1) and (2).

Railguns are electromagnetic launch systems which have the potential to accelerate projectiles to velocities higher than 2 km/s. The acceleration of the projectile is the result of the interaction of the current through the brush armature with the magnetic field induced by the current in the rails. For a conventional railgun, raising the current is the only way to increase the electromagnetic force on the projectile. The current density however is limited: the heating of the sliding contacts between the rails and the brush armatures due to the Joule-effect and to the friction can cause the melting of these contacts. Current transition results in an increase of the armature resistance and the deterioration of the rails (3).

One way to increase the acceleration without raising the current through the projectile is by adding an extra pair of rails in order to establish an additional magnetic field. The electromagnetic force on the projectile for an augmented railgun is described by the force-equation:

\[ F_{EM} = \frac{1}{2} L'_{IR} I_R^2 + M'I_R I_A \]

The first term represents the magnetic field induced by the current in the inner rails and is proportional to the self inductance gradient \( L'_{IR} \). The second term describes the influence of an additional magnetic field and is proportional to the mutual inductance gradient \( M' \). \( I_R \) and \( I_A \) are respectively the currents in the inner and outer rail.

The current in the outer rail, and thus the magnetic field, is limited by the electromagnetic forces on the rails. In this paper we investigate the influence of the dimensions of the outer rail on the electromagnetic forces on the projectile and on the rails for an augmented railgun.
augmented railgun. A similar preliminary study is described in Ref. (4).

The objectives of this preliminary study are to design an augmented rail gun capable of accelerating projectiles with a mass of 100 to 200 g to a velocity of 1 to 2 km/s, with the condition that the electromagnetic forces on the rails must be limited to 8 MN/m.

2. Simulations

The finite element code program ANSYS was used for the simulation of the magnetic fields. Three different material types are simulated. The air is simulated as a material with relative magnetic permeability of 1. The rails have an electrical resistivity of 2e-8 Ω.m and a relative magnetic permeability of 1. The projectile has an electrical resistivity of 2.6667e-8 Ω.m and again a relative magnetic permeability of 1.

2.1 Currents

For the simulations three current ratios are used. The amplitudes for the inner rails are chosen. The currents in the outer rails are determined in order to have the same impulse on the projectile for each current ratio. The calculations were made so that a muzzle velocity of 2 km/s is reached for a projectile with a mass of 200 g. For dc-currents in the inner rail with amplitudes of 400 kA, 500 kA and 600 kA the corresponding amplitudes for the outer rails, with \( L'_R = 0.4 \) µH/m and \( M' = 0.2 \) µH/m, are respectively 1267 kA, 833 kA and 511 kA.

The simulated railgun is a parallel augmented railgun. The inner and outer rails have a separate Pulse Forming Network. The currents for the transient analysis are a LabView simulation of these Pulse Forming Networks. Each PFN consists of five capacitor banks. A description of these capacitor banks can be found in Ref. (5). The results are represented in Fig. 2. These currents are multiplied with a factor to correspond with the analytical calculated results to the electromagnetic force determined with a 3D transient analysis.

2.2 Electromagnetic Forces on the Rails

The forces acting on the rails are determined with a 2D transient analysis. In a 2D analysis only the rails are simulated. The dimensions of the inner rail are fixed at 25 mm × 20 mm. The width of the outer rails is altered from 2 to 40 mm and the height from 2 to 30 mm with steps of 2 mm. The distance between the rails is varied between 1 mm to 15 mm in steps of 1 mm. The rails are surrounded by a cylinder of air. Only a quarter of the total geometry is simulated. Since the electromagnetic force on the elements is a direct outcome from the simulations with the finite element code ANSYS, no further calculations have to be made.

2.3 Electromagnetic Force on the Projectile: \( L'_R, M' \)

It is possible to determine the force on the projectile directly with a 3D-simulation of the rails and the projectile in the same way as the forces on the rails in a 2D-simulation. But a 3D transient analysis for all geometries is time-consuming and is only carried out for the most promising geometry. Instead the results for 10 Hz at 2.0 ms are used to calculate the electromagnetic force on the projectile at each step for the current ratio 400 kA/1267 kA and for both frequencies. The results are represented in Fig. 3. The results of the transient analysis are in good agreement with the results calculated for 1 kHz until 0.3 ms, then decrease to converge with the results for 10 Hz at 2.0 ms.

The fourth curve represents the results calculated with the values of the inductances linearly decreasing from the values calculated for 1 kHz at 0.3 ms to the values for 10 Hz at 2.0 ms and shows a good agreement. This method is used to calculate the electromagnetic forces for the different geometries and allows us to make an estimation of the maximal force and the impulse on the projectile.

3. Results

3.1 Electromagnetic Forces on the Rails

The EM forces on the inner and outer rails calculated with ANSYS refer to the force on one inner or outer rail. The inner and outer rail at one
side of the projectile are imbedded in a housing.

The results of our calculations with ANSYS point out that the total electromagnetic force on the rails is decreasing with increasing current ratio. When we take a look at the results for a large outer rail for the different current ratios, we see that the difference in the total electromagnetic force is mainly due to the large outer rail for the different current ratios. When we take a look at the results for a small outer rail the induced electromagnetic force on the rails is decreasing with increasing current ratio. When we take a look at the results for an outer rail of 24 mm × 20 mm and a current is concentrated at the middle of the upper surface of the rail. For a small outer rail the induced current concentrated in the corners at the side of the projectile. Since the magnetic field is inversely proportional to the square of the distance, this explains why the magnetic force on the inner rails is negative (inwards). For construction reasons, negative forces on the inner rails have to be avoided.

To compare the forces on the rails we determined the maximum total force for each geometry and current ratio. The total electromagnetic force on the rails is decreasing with increasing height h and distance between the rails a. For the current ratio 600 kA/511 kA the maximal total force in function of the width is found at b = 2 mm. For the two other current ratios the force curve in function of the width goes through a maximum. This is a result of the negative electromagnetic forces on the inner rail. The overall maxima of the total magnetic force are listed in Table 1. The lowest maximum 4.85 MN/m is found for the highest current ratio 600 kA/511 kA. The maximum 6.76 MN/m found for 500 kA/833 kA is about 40 % higher and the maximum 10.4 MN/m for 400 kA/1267 kA is more then two times higher then the one found for the highest current ratio.

### 3.2 L’R and M’

First we discuss the values of the inductance gradients found with the AC-analyses at 10 Hz and 1 kHz. The inductance gradients L’R found for 10 Hz fluctuate around 0.43 µH/m and do not show much variation in function of the width b, the height h and the distance a. The values for L’R at 1 kHz decrease slightly with increasing width b and height h and decreasing distance a and vary between 0.40-0.44 µH/m.

The mutual inductance gradient M’ decreases with increasing height h and distance a for both frequencies. At 10 Hz M’ is slightly decreasing with increasing width b. At 1 kHz the values for M’ go through a maximum in function of the width b. The mutual inductances vary between 0.16-0.26 µH/m at 10 Hz and between 0.25-0.38 µH/m at 1 kHz.

### 3.3 Electromagnetic Force on the Projectile

Once the inductance gradients are determined we can calculate analytically the electromagnetic force on the projectile. The fitted values for M’ and L’R and the currents for the transient analyses are used. To compare the results we determine the maximum electromagnetic force on the projectile for each geometry and at each current ratio. Notice that we can calculate the electromagnetic force on the projectile for any current ratio we want.

The maximum electromagnetic force on the projectile is decreasing with increasing height h and distance a for all current ratios. The values in function of the width b go through a maximum and show a dip at b = 14 mm like the values for M’ at 1 kHz.

The overall maxima are presented in Table 2. The lowest maximum is found for 600 kA/511 kA. The maxima found for 400 kA/1267 kA and 500 kA/833 kA are respectively 13 % and 6 % higher.

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**Table 1. Values and positions of the overall maxima for the total electromagnetic force on the rails**

<table>
<thead>
<tr>
<th>Current Ratio</th>
<th>Maximum</th>
<th>b</th>
<th>h</th>
<th>a</th>
</tr>
</thead>
<tbody>
<tr>
<td>IR = 400 kA, IA = 1267 kA</td>
<td>10.4 MN/m</td>
<td>14 mm</td>
<td>2 mm</td>
<td>1 mm</td>
</tr>
<tr>
<td>IR = 500 kA, IA = 833 kA</td>
<td>6.76 MN/m</td>
<td>12 mm</td>
<td>2 mm</td>
<td>1 mm</td>
</tr>
<tr>
<td>IR = 600 kA, IA = 511 kA</td>
<td>4.85 MN/m</td>
<td>2 mm</td>
<td>2 mm</td>
<td>1 mm</td>
</tr>
</tbody>
</table>

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**Table 2. Values and positions of the overall maxima for the total electromagnetic force on the projectile**

<table>
<thead>
<tr>
<th>Current Ratio</th>
<th>Maximum</th>
</tr>
</thead>
<tbody>
<tr>
<td>IR = 400 kA, IA = 1267 kA</td>
<td>10.4 MN/m</td>
</tr>
<tr>
<td>IR = 500 kA, IA = 833 kA</td>
<td>6.76 MN/m</td>
</tr>
<tr>
<td>IR = 600 kA, IA = 511 kA</td>
<td>4.85 MN/m</td>
</tr>
</tbody>
</table>
3.4 Impulse

The impulse can be calculated by integration of the analytically determined force curve. To obtain a muzzle velocity of 1 km/s for a projectile with a mass of 200 g or a muzzle velocity of 2 km/s for a projectile of 100 g the impulse on the projectile must be 200 Ns. A muzzle velocity of 2 km/s for a projectile with a mass of 200 g requires an impulse of 400 Ns.

For a chosen impulse, the outer rail current can be calculated if the inner rail current is fixed.

4. Determination of the Theoretically Best Geometry

With the theoretically best geometry we mean the best geometry found based upon the electromagnetic forces on the rails and on the projectile. To obtain the impulses mentioned above we have to maximize the force on the projectile. But high electromagnetic forces on the projectile mean also high electromagnetic forces on the rails. We fix the limit for the electromagnetic force on the rails at 8 MN/m for construction reasons. Therefore we have to find a balance between the electromagnetic forces on the rails and the electromagnetic force on the projectile.

The electromagnetic forces on the rails just as the electromagnetic force on the projectile are increasing with decreasing distance between the rails a and height h. The force on the projectile is decreasing faster for a and h than the force on the rails. The best ratio of the force on the projectile and the forces on the rails is found at a distance between the rails of a = 2 mm and a height of h = 2 mm.

The optimal width b is not so easy to find. The maximal electromagnetic forces on the projectile for a = 2 mm and h = 2 mm is found at 8 mm for all three current ratios. The maximum of the electromagnetic force on the rails depends on the current ratio. The best ratio of the force on the projectile and the forces on the rails is found at b = 8 mm for the current ratios 600 kA/511 kA and 500 kA/833 kA and at b = 2 mm for 400 kA/1267 kA. Another point of interest are the electromagnetic forces on the inner rail. If the width b is chosen too small, we will need a high current in the inner rail to avoid negative electromagnetic forces in the inner rails. We have chosen b = 8 mm to optimize the electromagnetic force on the projectile.

5. 3D transient Analysis of the Theoretical Solution

5.1 Determination of the Current Ratios

We first have to optimize the current ratios needed to obtain the desired impulses for the best theoretical geometry. For an impulse of 200 Ns we vary the inner current between 300 and 600 kA and calculated the corresponding outer current. For these current ratios a 2D transient analysis was carried out to determine the corresponding electromagnetic forces on the rails. The results of these calculations are listed in Table 3.

The electromagnetic forces on the rails decrease with an increasing current in the inner rails. Since limiting the current in the inner rails is the main reason why we want to design an augmented railgun, we choose the current ratio with the lowest inner current wherefore the electromagnetic force on the rails is smaller than 8 MN/m. But for the current ratio 400 kA/1030 kA there is a significant negative force on the inner rails. The results for 450 kA/857 kA show only a low negative electromagnetic force on the inner rail at the very beginning of the analysis and this current ratio is chosen as solution.

For an impulse of 400 Ns the inner current is varied between 550 kA and 850 kA and the corresponding outer currents are calculated. The electromagnetic forces on the rails are again simulated with a 2D transient analysis (Table 4). The limit of 8MN/m is not achieved for a reasonable inner current.

5.2 Electromagnetic Force and Impulse on the Projectile

A 3D transient analysis was carried out for the best theoretical geometry for the current ratio 450 kA/857 kA. The electromagnetic force on the projectile obtained with this analysis is compared with the results of the analytical method (Fig. 6) and a good agreement is found. The difference between the electromagnetic forces on the projectile calculated with both methods is within 2%. The current ratio 450 kA/857 kA was optimized to obtain an impulse of 200 Ns. The impulse based on the results of the 3D transient analysis, calculated as control, is 202.
6. Discussions

For the construction of an augmented railgun the influence of the geometry of the outer rail on the magnetic forces on the projectile was studied. The objective is a muzzle velocity of 1-2 km/s for a projectile with a mass of 100-200 g and electromagnetic forces on the rails lower than 8 MN/m.

A 2D transient analysis was carried out for the determination of the electromagnetic force on the rails. The total electromagnetic force on the rails decreases with increasing height h and distance a. The lowest overall maximum is found for the current ratio with the highest inner rail current. The width b where the overall maxima are found is depending on the current ratio.

The electromagnetic force on the projectile was analytically calculated with the force-equation. The coefficients of this force-equation \( L' \) and \( M' \) were determined with 3D AC analyses at 10 Hz and 1 kHz. The force on the projectile decreases with increasing height h and distance a. The overall maxima were found at \( b = 8 \) mm. The electromagnetic force on the projectile is increasing with decreasing current ratio.

To determine the theoretically best geometry a balance between the electromagnetic forces on the rails and on the projectile has to be found. The electromagnetic force on the projectile is faster decreasing with the distance a and the height h than the electromagnetic force on the rails. The width b was optimized to obtain a maximum force on the projectile. The theoretically best geometry is then \( a = 2 \) mm, \( h = 2 \) mm and \( b = 8 \) mm.

Then we determined the best current ratio for this geometry to obtain an impulse of 200Ns. A 3D transient analysis was carried out for the theoretically best geometry. The difference between the directly determined and the analytically calculated force on the projectile is within 2 % and the determined impulse is 202 Ns. The maximum total electromagnetic force on the rails is 6.3 MN/m for this configuration.

For an impulse of 400 Ns the limit of 8 MN/m for the electromagnetic force on the rails was not achieved for an acceptable inner current.

The obtained solution for an impulse of 200 Ns is a theoretical solution based upon the electromagnetic forces on the rails and on the projectile. Other criteria have to be considered for the final construction, like the mechanical feasibility and the maximal current density.

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References


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