A Novel Control Method in Flux-weakening Region for Efficient Operation of Interior Permanent Magnet Synchronous Motor

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(Manuscript received Aug. 8, 2014, revised May 18, 2015)

This paper proposes a novel control method in the flux-weakening region. The proposed method utilizes a maximum torque per flux (MTPF) control at full load, and an efficient flux-weakening control at light load. In order to simplify the MTPF control, the approximate method of MTPF curve is proposed. In the flux-weakening control, a more efficient control obtained by minimizing the armature current at light load is applied. In the flux-weakening region, it is possible to operate at the maximum torque by applying the MTPF control. In addition, if the load torque is light, operation along a constant voltage ellipse is more efficient compared to the operation of the MTPF control along the MTPF curve owing to the decrease in copper loss with decreasing armature current. In the proposed efficient flux-weakening control, a current command generation method in which the armature current ampere is adopted for operation along the constant voltage ellipse is also proposed. The validity of the proposed control method is verified by simulation and experimental results.

Keywords: IPMSM, Flux-weakening control, High efficiency, MTPF control

1. Introduction

The interior permanent magnet synchronous motor (IPMSM) is capable of variable speed operation over a wide speed region compared to a surface permanent magnet synchronous motor (SPMSM). This operation is made possible by the flux-weakening control which controls the induced voltage to the induced voltage limit by the negative d-axis current in the high-speed region. The output capability of PMSM depends on the machine parameters and the control method. The maximum output power can be obtained under the voltage and current constraints by the maximum output control, in which the current vector is operated at the optimal operating condition. The profile of the speed versus torque and power characteristics as well as the optimal control method in the high-speed region are dependent on \( \Psi_{dmin} = \Psi_u - L_d I_{an} \) \(^{(13)}\), where \( \Psi_u \) is the stator flux linkage due to the permanent magnet, \( L_d \) is the d-axis inductance, and \( I_{an} \) is the armature current limit. If \( \Psi_{dmin} \) is negative, maximum torque can be obtained in the high-speed flux-weakening region by applying maximum torque per flux (MTPF) control.

The parameter of \( \Psi_{dmin} \) is usually positive in the conventional PMSMs. For such PMSMs, in which it is not necessary to apply MTPF control, a lot of flux-weakening strategies including MTPF control were proposed. However, the method of generating the current command value in the MTPF region is complex. The MTPF control strategies were discussed in some papers. In Ref. (11), the flux-weakening control for non-salient pole PMSM having large winding inductance was proposed, however, the control method at the high-speed and light-load condition and the application to the IPMSM drive were not discussed. In general, the control of IPMSM becomes difficult compared with SPMSM. The flux-weakening control strategies including MTPF control for IPMSM were proposed in Refs. (12) and (13). In the control system of Ref. (12), many lookup tables and PI controllers are used for generating the d- and q-axis current commands, and the design method of the PI gains is unclear and it will be necessary to adjust those gains appropriately. Therefore, the system configuration and the design of controller seem to be complex. Although the complex control algorithm can be easily implemented with recent high-performance processors, the composition of an easier control system is more preferable to the viewpoint of the easy adjustment of the controller. The direct-flux field-oriented vector control was applied for the MTPF control in Ref. (13). In this system, the current feedback control loop does not exist and voltage commands are generated based on the flux and q-axis current. The control method and efficiency characteristics at the high-speed and light-load condition were not discussed in both papers.

The purpose of this paper is to develop a novel control method in the flux-weakening region for IPMSM with negative \( \Psi_{dmin} \) in order to achieve a high-efficiency operation. The proposed IPMSM drive system is based on the conventional current feedback control, and thus there is

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not additional controller. This paper proposes a generation method of current vector command (d- and q-axis current commands) for improving efficiency and simplifying control system. Because the expression of relations between d- and q-axis currents for the MTPF control is complicated\(^{(1)}\), a straight-line approximation of the MTPF curve is used in order to simplify the control algorithm of the MTPF in the proposed method. In order to achieve high-efficiency operation in the high-speed flux-weakening region, two methods are discussed, and the current vector is operated along a constant-voltage ellipse under the high-speed, light-load condition in the proposed system. The generation method of current vector command is proposed in order to achieve a stable and efficient operation at high speeds. The performances of the proposed control method are evaluated by simulations and experiments, and the validity of the proposed method is verified.

2. Maximum Output Control

This section examines the current vector control method used to obtain the maximum output under the limiting voltage and current conditions given as follows:

\[
V_o = \omega \sqrt{(\Psi_a + L_d i_d)^2 + (L_q i_q)^2} \leq V_{om} \quad \cdots \cdots \cdots \cdots (1)
\]

\[
I_o = \sqrt{i_d^2 + i_q^2} \leq I_{om} \quad \cdots \cdots \cdots \cdots (2)
\]

where \(V_o\) is the induced voltage, \(\omega\) is the electrical rotor angular velocity, \(\Psi_a\) is the armature flux linkage due to permanent magnet, \(i_d\) and \(i_q\) are the armature currents in the d-q frame, \(L_d\) and \(L_q\) are the d- and q-axis inductances, \(V_{om}\) is the induced voltage limit, \(I_{om}\) is the armature current, \(I_{am}\) is the armature current limit.

Figure 1 shows the characteristic curves on a current vector plane at 2,000 r/min, where the machine parameters of the tested IPMSM listed in Table 1 are used. The maximum speed of tested IPMSM is limited by 2,000 r/min as shown in Table 1. In this situation, the ratio of voltage drop due to the resistance among the voltage becomes relatively higher. In the proposed current command generation method, however, the armature current limit \(I_{am}\) and the induced voltage limit \(V_{om}\) are considered. Therefore, the voltage drop due to the resistance does not affect the current command generation. The voltage limit due to winding resistance \(R_a\) is considered when the induced voltage limit \(V_{om}\) is set from the voltage limit \(V_{am}\); \(V_{am} = V_{om} - R_a I_{am}\). In this case, armature voltage \(V_a\) becomes less than \(V_{am}\) in the control that keeps \(V_{am}\) to \(V_o\), and there is voltage margin. Although this voltage margin is large in this study because of setting the induced voltage limit to low value as mentioned above, the voltage drop by armature resistance \((R_a I_{am})\) is 10% or less of the voltage limit \((V_{am})\) in general. Thus the voltage margin is not too large and it is thought that the influence of the voltage margin is a little.

The maximum torque per ampere (MTPA) curve and the MTPF curve indicate the current vector trajectory when MTPA control and MTPF control are applied. In Fig. 1, the constant-current limit circle indicates the armature current limit. The constant voltage ellipse indicates the corresponding induced voltage limit at a rotor speed of 2,000 r/min. Figure 2 shows a close-up of the area inside the broken-line rectangle in Fig. 1. Points A is the intersection of the MTPF curve and the constant voltage ellipse. The q-axis current on the constant voltage ellipse is maximum at Point B. Points C and D are located at the intersection of the constant-torque curve and the characteristic curves, respectively.

2.1 Maximum Torque per Ampere Control

Maximum torque per ampere (MTPA) control is performed at the intersection of the current limit circle and the MTPA curve. The MTPA curve is given by the following equation\(^{(6)}\).

\[
\frac{\psi}{\phi} = \frac{L_d}{L_q} \quad \text{at} \quad I_m = \frac{V_m}{L_d}
\]

Table 1. Parameters of the IPMSM and the controller

<table>
<thead>
<tr>
<th>Item [Unit]</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of pole pairs</td>
<td>2</td>
</tr>
<tr>
<td>Armature flux linkage (\Psi_a) [Wb]</td>
<td>0.078</td>
</tr>
<tr>
<td>d-axis inductance (L_d) [mH]</td>
<td>72.2</td>
</tr>
<tr>
<td>q-axis inductance (L_q) [mH]</td>
<td>568</td>
</tr>
<tr>
<td>Current limit (I_{am}) [A]</td>
<td>2.4</td>
</tr>
<tr>
<td>Armature voltage limit (V_{am}) [V]</td>
<td>91.85</td>
</tr>
<tr>
<td>Base speed [r/min]</td>
<td>200</td>
</tr>
</tbody>
</table>

Fig. 1. Characteristic curves on the current vector plane (2,000 r/min)

Fig. 2. Close-up of area indicated by the broken line in Fig. 1
This control method is applied in the speed region in which the induced voltage \( V_o \) does not exceed the induced voltage limit \( V_{om} \). In this case, point I in Fig. 1 is the operating point generating maximum torque by MTPA control considering the current limit. In this control region, the armature current \( I_a \) is equal to the current limit \( I_{am} \), and the induced voltage \( V_o \) is less than the induced voltage limit \( V_{om} \).

2.2 Flux-weakening Control for Maximizing Torque

The induced voltage increases with increasing rotor speed. When the motor speed reaches the base speed, the induced voltage becomes equal to the induced voltage limit \( V_{om} \). Hence, the induced voltage is controlled to the induced voltage limit \( V_{om} \) by flux-weakening (FW) control above the base speed, and the \( d \)-axis current is given by the following equation (3).

\[
I_d = \frac{\psi_a}{2(L_q - L_d)} - \frac{\psi_a^2}{4(L_q - L_d)} + \frac{V_o}{L_d} \quad \cdots \cdots \cdots \cdots \cdots (3)
\]

Fig. 3 shows the torque versus speed characteristics based on several control methods. Figure 4 shows the armature current corresponding to Method A and Method B at 2,000 r/min.

3. Control Method in Flux-weakening Region

3.1 Current Vector Generation Method in Flux-weakening Region

In a high-speed region in which the MTPF control should be applied to obtain the maximum output, we discuss the current vector generation method under a light-load.

In the first method, the operation of the current vector along the MTPF approximation inside the constant-voltage ellipse is considered. This method is referred to herein as Method A. Hence, the operating point is present inside a constant-voltage ellipse. This method is referred to here as Method B. In this method, the current vector is operated at the intersection of the constant-voltage ellipse and the constant-torque curve. Point C in Fig. 2 corresponds to the operating point at a load torque of 0.1 Nm. In the second method, the operation of current vector along the constant-voltage ellipse is considered. This method is referred to here as Method B. In this method, the current vector is operated at the intersection of the constant-voltage ellipse and the constant-torque curve. Point C in Fig. 2 corresponds to the operating point at a load torque of 0.1 Nm. Method B appears to be more efficient compared to Method A because the copper loss decreases with decreasing current. Figure 4 shows the armature current versus torque characteristics at 2,000 r/min under the control of Method A and Method B. This figure shows that Method B can reduce the armature current compared to Method A. Therefore, Method B is applied as the current vector generation method in the proposed IPMSM control system.

3.2 Generation of Current Commands

Figure 5(a) shows the general method for generating the \( d \) - and \( q \)-axis current commands. In this method, \( q \)-axis current command \( i_{q}^* \) is determined by the speed error \( \Delta \omega \). Then, the \( d \)-axis current command \( i_{d}^* \) is determined using the current vector control algorithms given by (3), (4) and (5). The \( i_{q \text{lim}} \) in Fig. 5(a)
represents a limit value of the q-axis current command \( i_q^* \). The value of \( i_{\text{lim}} \) is determined based on the q-axis current during the maximum output control shown in Fig. 1. The current limit \( i_{\text{lim}} \) is decreased with increasing rotor speed in order to control the induced voltage \( V_o \), and the armature current \( I_a \) to the induced voltage limit \( V_{\text{om}} \) and the armature current limit \( I_{\text{am}} \), respectively.

In the proposed current vector generation method (Method_B), the current vector moves from point A toward B and C at 2000 r/min as the load torque decreases, as shown in Fig. 2. In this case, the q-axis current must increase from point A to point B. Figure 5(b) shows the q-axis current vs. torque characteristics. Points A, B, and C correspond to operating points A, B, and C in Fig. 2. The MTPF control is switched to operation along the constant-voltage ellipse at point A. Point C is the operating point at a load torque of 0.1 Nm. This figure shows that the q-axis current hardly changes for a change of the torque, and thus torque control by the q-axis current seems difficult. Moreover, the q-axis current must increase in order to decrease the torque in the region from point A to point B. In the conventional system shown in Fig. 5(a), however, the q-axis current command decreases when the output of PI controller decreases. Therefore, stable operation cannot be achieved by the conventional method shown in Fig. 5(a).

The proposed current command generation method based on armature current command is shown in Fig. 6(a). In the proposed method, an armature current command \( I_{a}^* \) is first generated from \( \Delta \omega \), and the current phase angle \( \beta' \) corresponding to the current command \( I_{a}^* \) is then determined using Eqs. (6) and (7). Equation (6) is used to achieve the MTPA control (3), and Eq. (7) was derived from condition of \( \Psi_a = V_{\text{om}} \) and Eqs. (1), (8) and (9). Equation (7) is used in the speed range above the base speed including MTPF control region. Based on \( I_{a}^* \) and \( \beta' \), the d- and q-axis current commands are determined using Eqs. (8) and (9).

\[
\beta'_{\text{MTPA}} = \sin^{-1} \left( \frac{-\Psi_a + \sqrt{\Psi_a^2 + 8 (L_q - L_d)^2 I_{a}^*} \Psi_a^2}{4 (L_q - L_d) I_{a}^*} \right) \tag{6}
\]

\[
i_q^* = I_a^* \cos \beta' \tag{8}
\]

\[
i_q^* = -I_a^* \sin \beta' \tag{9}
\]

Figure 6(b) shows the armature current vs. torque characteristics at 2,000 r/min. In the operation along the constant-voltage ellipse, the output torque increases with increasing armature current. Therefore, stable operation can be achieved by the proposed method shown in Fig. 6(a). However, if the armature current becomes greater than the current at the intersection point of the constant-voltage ellipse and the MTPF curve (the point A in Fig. 2), the torque decreases with increasing armature current in the operation along the constant voltage ellipse. Thus, the limitation of the armature current is necessary. The \( I_{\text{lim}} \) in Fig. 6(a) represents a limit value of the armature current command \( I_{a}^* \), and is determined based on the armature current during the maximum output control. \( I_{\text{lim}} \) is set to \( I_{\text{am}} \) below the speed at which the current vector control method is changed from FW control to MTPF control under the maximum output control shown in Sect. 2. Above that speed, \( I_{\text{lim}} \) is determined by the current at the intersection point of the constant-voltage ellipse and the MTPF curve given by Eq. (5), and \( I_{\text{lim}} \) is decreased with the increasing rotor speed.

4. Analysis Results

The analysis is carried out using the parameters listed in Table 1. The analysis results show the acceleration characteristics, where the speed command steps up from 100 to 2,000 r/min under 0.1 Nm. Figure 7 shows the responses of the rotor speed, torque and armature current controlled by Method_A and Method_B. The rotor speed and torque of Method_A and Method_B are approximately the same. However, the armature current of Method_B is less than that of Method_A after the speed reaches the commanded speed. Figure 8 shows the current vector trajectory under
the operation shown in Fig. 7. Figure 8(a) shows that the operation along the straight-line approximation of the MTPF curve is possible using the Method_A. Figure 8(b) shows that operation along the constant-voltage ellipse is possible using the Method_B after the speed reaches the commanded speed. The current vector trajectory seems not to be along the MTPA curve in Fig. 8. This trajectory represents the momentary response of controlled current vector at step change of speed command, at which the current vector command also instantaneously changes to the operating point I in Fig. 8. Therefore, there is no necessity that current vector moves along the MTPA curve at this transient-state.

Figure 9 shows the torque controlled by the proposed method under the operation conditions shown in Fig. 7. Figure 9 also shows the theoretical value for each control method. The output torque was not observed to differ between the calculated value and the theoretical value in the region which is used in actual operation. Therefore, the good current vector control and speed control is achieved by the proposed control method.

Based on the analysis results, the following results were obtained. The MTPF control is possible using the straight-line approximation of the MTPF curve. Operation using Method_B is more efficient compared to that using Method_A under a light-load. The stable operation can be achieved by using the armature current value and current phase angle to generate the $d$- and $q$-axis current commands.
5. Experimental Results

5.1 Transient Characteristics
The experiment is carried out under same conditions as the analysis. The purpose of the experiment is to realize efficient operation along the constant-voltage ellipse and MTPF control in the high-speed region. Figure 10 shows the IPMSM drive system used in the experiment. The experimental results reveal the acceleration characteristics, where the speed command steps up from 100 to 2,000 r/min under 0.1 Nm. Figure 11 shows the measured current vector trajectory. The three control methods are confirmed to switch properly with increasing rotor speed. Figure 12 shows the speed response characteristic, and the desirable speed response is realized. The results of the experiment and analysis are confirmed to be similar.

5.2 Motor Losses
The motor losses of Method A and B under the high-speed, light-load condition are compared. Figure 13 shows characteristics of copper and iron losses at 2,000 r/min. This tested condition is the same as in Fig. 4. The magnetic saturation exists in the tested motor and thus the $q$-axis inductance increases in the high-speed flux weakening region because the $q$-axis current becomes small. As a result, the current to produce the same torque becomes less than Fig. 4 in the experiment because of increase of reluctance torque. The current of Method B becomes smaller than Method A at the torque of 0.17 Nm, and the copper loss has become small as shown in Fig. 13, even if the armature current is the same at torque of 0.16 Nm in Fig. 4. Additionally, the difference of copper loss increases with decreasing the load torque. On the other hand, iron loss of the Method A and B is almost same irrespective of torque value. It is confirmed that Method B is more efficient under the high-speed, light-load condition.

6. Conclusions
A novel control method for use in the flux-weakening re-
region for operation at optimal torque point has been proposed. The simulation and experimental results confirmed the possibility of expanding the operation region by applying the simplified control method using approximate MPF control algorithm. In addition, efficient operation is possible using Method B. The stable operation can be achieved by using the armature current value and current phase angle to generate the d- and q-axis current commands. Thus, wide, efficient and stable operation is possible by the proposed control method. In order to utilize the available voltage as much as possible and improve the control accuracy, the current vector control to keep \( V_a \) to \( V_{un} \) and the consideration of magnetic saturation are required. We will continue study for these improvements.

**References**


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