Performance Evaluation of Interior Permanent Magnet Motors Using Thin Electrical Steels

Thanh Anh Huynh  Non-member,  Min-Fu Hsieh∗ Non-member

(Manuscript received Jan. 21, 2017, revised July 11, 2017)

This work investigates the impact of thin electrical steel laminations on the performance of interior permanent magnet (IPM) motors for electric vehicle tractions. Three different electrical steel grades are used in IPM motor designs and the performance is evaluated by simulation. It is found that thin laminations can improve the efficiency of the IPM motor, but the output torque could be slightly reduced due to low saturation flux density. Therefore, direct replacement of core materials for the same motor design may not be suitable. This paper presents the considerations for the design of IPM motors using thin laminations. The motor performance, including torque, efficiency, and constant power speed range is evaluated. A process is developed for the design of high performance IPM motors using thin laminations. Experimental studies are conducted to validate the simulations and designs.

Keywords: traction motor, IPM motor, thin lamination, field-weakening control

1. Introduction

Interior permanent magnet (IPM) motors are considered to be an excellent candidate for tractions of electric vehicle (EV) due to their high efficiency, high torque/power density and wide constant power speed range (CPSR). The requirements of lightweight and compactness for EV powertrains lead to high speed design of traction motors and this would require the iron loss to be minimized to maintain the efficiency. Therefore, thin electric steel laminations are gaining more and more popularity for high speed traction motors. However, thin laminations (e.g., 0.2 mm or thinner) usually possess lower saturation flux density than common ones (e.g., 0.5 or 0.35 mm). This may bring the output torque slightly lower and this is disadvantageous for high torque operation of EVs at low speed. Therefore, the effect of such materials used for traction motors should be carefully evaluated.

Many studies have analyzed the applications of different electrical steels to electric motors but mainly focused on core loss and efficiency [2–7]. The torque characteristics and efficiency of IPM motors using high-strength non-oriented electrical steel were enhanced compared to those using other materials [8]. Grain oriented electrical steel was used to replace conventional non-oriented electrical steel for axial flux switched reluctance motors in [9] and the result revealed an over 20% torque improvement. Four electrical steel grades were employed in [10] for synchronous reluctance motors and their d-q axis inductance were investigated.

From above discussions, two major research trends regarding electrical steels for electric motors can be observed: (a) high flux density materials to increase the torque or performance, and (b) high-strength and low-iron-loss materials to increase the efficiency at high speed or rotor strength. However, few studies have reported design and analysis to achieve both high torque and high efficiency using thin laminations. Note that thin laminations are still costly. Hence, using different materials for stator and rotor may satisfy the targets of high torque, high efficiency at high speed and low material cost.

This paper first presents the performance evaluation of IPM motors using thin laminations. The benefits of combining different materials, i.e., high saturation flux density and low iron loss to improve the motor performance and reduce the material cost are also investigated. This would be an alternative solution to designs with low material cost and high performance if motor production with stator and rotor having different materials can be easily fulfilled. Three materials are employed in this study: one thin lamination and two high-strength and low-iron-loss materials. A 10 kW IPM motor is designed as the case study. The motor performance is evaluated based on torque output, efficiency, and flux-weakening ability for constant power speed range (CPSR), which is an important performance index for EV application. Finite element method (FEM) is used for analysis. A prototype is fabricated and the designs and simulations are validated by experiments. Note that the mechanical strength of thin laminations for high speed applications is not discussed in this paper.

2. Analysis of IPM Motor

The main specifications and parameters of the target 10 kW IPM traction motor are given in Table 1. Five different motor designs based on two configurations are studied, as shown in Fig. 1, where the permanent magnet (PM) are arranged to be double-layer and triangular. These configurations are commonly employed in electric vehicles with a decent flux weakening capability and therefore their performances using different electrical steels (including thin laminations) may be

a) Correspondence to: Min-Fu Hsieh. E-mail: mfsieh@mail.ncku.edu.tw
∗ Department of Systems and Naval Mechatronic Engineering, National Cheng Kung University
1, University Road, Tainan, Taiwan

© 2017 The Institute of Electrical Engineers of Japan.
Performance Evaluation of Thin Laminations for IPM Motor

Thanh Anh Huynh et al.

Table 1. Specifications of 10 kW IPM motor

<table>
<thead>
<tr>
<th>Parameters/Specifications</th>
<th>Value (Unit)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum torque</td>
<td>54 Nm</td>
</tr>
<tr>
<td>Maximum speed</td>
<td>9000 RPM</td>
</tr>
<tr>
<td>Maximum current</td>
<td>110 A</td>
</tr>
<tr>
<td>Maximum voltage</td>
<td>220 Vrms</td>
</tr>
<tr>
<td>Number of phase</td>
<td>3</td>
</tr>
<tr>
<td>Number of poles</td>
<td>8</td>
</tr>
<tr>
<td>Number of slot</td>
<td>36</td>
</tr>
<tr>
<td>Stator diameter</td>
<td>160 mm</td>
</tr>
<tr>
<td>Stack length</td>
<td>86 mm</td>
</tr>
<tr>
<td>Air-gap length</td>
<td>0.5 mm</td>
</tr>
</tbody>
</table>

Fig. 1. Two rotor configurations of 10 kW IPM motor

Table 2. Design parameters of five IPM motor designs

<table>
<thead>
<tr>
<th>Items</th>
<th>Double PM layers</th>
<th>Triangular PM</th>
</tr>
</thead>
<tbody>
<tr>
<td>X1 (mm)</td>
<td>2.3</td>
<td>3.3</td>
</tr>
<tr>
<td>X2 (mm)</td>
<td>4.47</td>
<td>4.47</td>
</tr>
<tr>
<td>Number of slots</td>
<td>36</td>
<td>36</td>
</tr>
<tr>
<td>Rotor size (mm)</td>
<td>94</td>
<td></td>
</tr>
<tr>
<td>Stator size (mm)</td>
<td>160</td>
<td></td>
</tr>
<tr>
<td>PM volume (mm³)</td>
<td>7740</td>
<td></td>
</tr>
<tr>
<td>PM Material</td>
<td>N55H (NdFeB, B=1.19 T, Hc=915 kA/m at 20 °C)</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 2. The stator flux linkage in the d-q reference frame

2.1 Mathematical Model of IPM Motor

The phasor diagram in the d-q reference frame as shown in Fig. 2 is used to analyze the IPM motor characteristics.

The d- and q-axis currents \(I_d\) and \(I_q\) can be given as

\[ I_d = -I_s \sin \beta, \quad I_q = I_s \cos \beta \]  \hspace{1cm} (1)

where \(\beta\) is current angle and \(I_s = \sqrt{I_d^2 + I_q^2}\).

The d- and q-axis voltages can be expressed as

\[ V_d = R_d I_d - \omega \Phi_q = R_d I_d - \omega L_q I_q \]  \hspace{1cm} (2)

\[ V_q = R_q I_q + \omega \Phi_d = R_q I_q + \omega L_d I_d + \omega \Phi_m \]  \hspace{1cm} (3)

where \(\Phi_d\) and \(\Phi_q\) are the d-q-axis flux linkages respectively; \(L_d\) and \(L_q\) are the d-q-axis inductances, respectively; \(\Phi_m\) is the PM flux linkage; \(R_d\) is the phase resistance; \(\omega\) is the electrical angular speed, and \(V_s\) is the voltage in the stator winding.

\[ V_s = \sqrt{V_d^2 + V_q^2} \] \hspace{1cm} (5)

Note that the excitation current \(I_s\) should not exceed the maximum allowable current (the current limit to produce the peak torque). The electromagnetic torque \(T_e\) of IPM motors consists of two components: the mutual torque and reluctance torque and can be calculated by

\[ T_e = \frac{3}{2} P \left( \Phi_m I_q - (L_d - L_q) I_d I_q \right) \] \hspace{1cm} (6)

where \(P\) is the number of poles.

Note that the torque in (6) does not consider the influence of iron losses and mechanical loss. To evaluate the effect of electrical steels on the motor performance, iron losses are computed here using FEM based on the iron loss models of the materials employed without considering the effect of pulse-width modulation (PWM) switching.

2.2 Characteristics of Electrical Steels

The B-H curves of the three electrical steels (produced by China Steel Corp., Taiwan) are given in Fig. 3(a). As can be seen, 50CS1300 possesses the highest saturation flux density in comparison with the other two. One drawback of thin electrical steel material (20CS1500HF) is the low saturation flux density despite its low iron loss [Fig. 3(b)]. This makes it suitable for high speed operation (if mechanical strength is not considered) but disadvantageous for high torque output.

2.3 Material Combinations for IPM Motors

The core loss of IPM motors is calculated using FEM with the data shown in Fig. 3(b). From the three materials, seven material combinations for the stator and rotor are considered, as...
Table 3. Material combinations (based on Motor 1)

<table>
<thead>
<tr>
<th>Model No.</th>
<th>Materials</th>
<th>Denoted</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>50CS1300 (R + S)</td>
<td>T1</td>
</tr>
<tr>
<td>Case 2</td>
<td>35CS550 (R + S)</td>
<td>T2</td>
</tr>
<tr>
<td>Case 3</td>
<td>20CS1500HF (R + S)</td>
<td>T3</td>
</tr>
<tr>
<td>Case 4</td>
<td>20CS1500HF (R) + 35CS550 (S)</td>
<td>T4</td>
</tr>
<tr>
<td>Case 5</td>
<td>20CS1500HF (R) + 50CS1300 (S)</td>
<td>T5</td>
</tr>
<tr>
<td>Case 6</td>
<td>35CS550 (R) + 20CS1500HF (S)</td>
<td>T6</td>
</tr>
<tr>
<td>Case 7</td>
<td>50CS1300 (R) + 20CS1500HF (S)</td>
<td>T7</td>
</tr>
</tbody>
</table>

Note: R is rotor and S is stator.

Fig. 4. Torque comparison of three electrical steel materials (@110 A current)

Fig. 5. Torque characteristics of the combining electrical steel materials (@110 A current)

listed in Table 3. For a fair and direct comparison, the geometry, meshes, nodes and elements are constructed in the same condition for all the cases, which are all based on the same motor, i.e., "Motor 1", as shown in Fig. 1(a) and Table 2.

2.4 Results and Discussion—Torque Output

To evaluate the effect of the combined materials, the operating condition at the peak torque (and the peak current 110 A) and a speed of 1800 rpm is first considered, where the output power is maximum and saturation could occur. Therefore, Fig. 4 shows the torque characteristics of cases T1, T2, and T3 at the peak current with varying current angles ($\beta$). Each of these three cases employs the same material for its stator and rotor but the materials are different for one case from another. As can be seen, the torque of models T1 (50CS1300) and T2 (35CS550) is respectively 2.6% and 1.5% higher than that of T3 (20CS1500HF). This is mainly due to different material saturation flux densities.

In the cases of using different materials for the stator and rotor, the simulation in Fig. 5 shows that the condition is similar to the previously discussed cases, around 2% difference between the highest and lowest cases. Model T7, with a 20CS1500 stator and 50CS1300 rotor, produces the highest torque. The torque is higher than that of T2 and T3 and very close to T1. Note that the excitation currents are the same for all the models.

Discussion:
The above results invoke some discussions regarding the material effect, as listed in the following.

(a) The stator is subject to alternating flux and using thin lamination is advantageous for high efficiency design.
(b) The rotor is used to produce field and the majority of flux does not alternate (disregarding armature reaction and PWM switching). Thus, the rotor seems to be less sensitive to iron loss.
(c) The use of materials with high saturation flux density for the rotor can indeed improve torque output but the stator with a lower saturation flux density may bring the flux level and torque down slightly.
(d) Employing thin laminations for both stator and rotor to improve efficiency at high speed, the slightly reduced torque may be recovered by proper design.
(e) As shown in Figs. 4 and 5, for all the models, the peak torque occurs at a current angle of around 43°E under maximum voltage operation.

Figure 6 shows the variation of $d$-$q$-axis inductances with different currents at 43°E current angle.

2.5 Results and Discussion—Iron Loss and Efficiency

The simulations shown in Fig. 7 are conducted based on the iron loss models given by the material provider for various speeds and frequencies. The influence of PWM harmonics is not considered in the analysis. Therefore, in practice, the iron loss in the rotor may be greater than predicted due to the PWM harmonics effect. It can be seen from Fig. 7 that the iron loss in the stator is larger than that in the rotor. This is expected due to the alternating flux in the stator.
Also expectedly, the rotors or stators using thin lamination have much less iron loss than that of the thick one. The stator iron loss drops after 2400 RPM are due to the introduction of flux weakening. In Fig. 8, T1 has the highest iron loss while T3 has the lowest (the efficiency of T3 is 2.5% higher than T1). Both T6 [35CS550(R) + 20CS1500HF(S)] and T7 [50CS1300(R) + 20CS1500HF(S)] have lower iron loss than T4 [20CS1500HF(R) + 35CS550(S)] and T5 [20CS1500HF(R) + 50CS1300(S)]. The efficiency of T6 and T7 is slightly higher than that of T4 and T5. The results shown in Figs. 7 and 8 are calculated at the peak current of 110 A, whose current angles vary from low speed up to the maximum speed (9000 rpm). It can also be observed that the iron loss in the stator using different materials has the larger difference than that in the rotor and therefore low-iron-loss materials should be used for the stator.

**Discussion**

From the above results, it can be observed that:

(a) Although material combinations can hardly enhance motor torque but improve iron loss and efficiency. It also leads to reducing the material cost.

(b) The iron loss and efficiency of all the models can be categorized into three groups, i.e., T1-T6-T7, T2-T4, and T3-T5. It can be observed that the stators in the same group used the same lamination materials and the small deviation is caused by the rotor materials used. This indicates that stators have a much more significant effect on efficiency than rotors.

(c) From Eq. (6), it can be seen that the torque of IPM motors can be improved by increasing the PM flux linkage \( \Phi_m \) or current (note: materials do not affect the inductance much). However, increasing the current might lead to low efficiency. Therefore, enhancing air gap flux would be the most influential way but the stator and rotor require a redesign.

### 2.6 Brief Summary

It can be observed from the above analysis that, using different materials in the stator and rotor can achieve an equivalent performance to those cases with the stator and rotor having the same materials. Model T1 may have the highest torque but the lowest efficiency and material cost. Model T3 has the lowest torque based on the same current but the highest efficiency and material cost. With a modest material cost and excellent performance, T7 is considered as a tradeoff design and should be a decent choice. Therefore, T7 [50CS1300(R) + 20CS1500HF(S)] is chosen for further investigation as will be discussed in the following sections.

For the iron losses at the peak torque (@110 A, 43°E) operation, Table 4 summarizes the simulation results for the seven models investigated. As expected, T1 and T6 have the greatest iron losses. Generally, the iron losses at this condition are smaller than those at high speed.

### 3. Performance Analysis with Selected Materials

Recalling the motor designs shown in Fig. 1 and Table 2, the material combination T7 will be applied to these five motors. In addition to torque and efficiency, the five IPM motors are also evaluated based on two important performance indices: the flux-weakening ability and saliency ratio, as expressed by (11):

\[
\max(k_{CPSR}) = \max \left( \frac{\Phi_m + L_q I_{lim}}{\Phi_m - L_d I_{lim}} \right) \quad {{\text{max}}} \quad \text{max}(\xi)
\]

\[
\xi = \frac{L_q}{L_d} \quad \text{max}(\xi)
\]

where \( k_{CPSR} \), defined to be the ratio of maximum speed to base speed, indicates the capability to achieve constant power speed range (CPSR) due to the weakened field by d-axis current. \( \max(k_{CPSR}) \) is maximum \( k_{CPSR} \), \( I_{lim} \) is current limit \( \xi \) and is saliency ratio, indicating the reluctance torque capability. The smaller the term \( \xi \), the larger the flux-weakening capability can be (12). To accurately evaluate the CPSR, accurate calculation of inductance variation is necessary, which is not a straightforward task, especially when saturation occurs. In this paper, the inductance is computed by the FEM package JMAG and the CPSR can be determined.

### 3.1 Result Analysis—Saturation Effect

The original design is Motor 1, as previously mentioned. Motors 2 and 3 are modified designs based on Motor 1 by changing the distance from the PM center to rotor surface [as the “X1” indicated in Fig. 1(a)] and the stator tooth width [as the “X2” indicated in Fig. 1(a)]. Motor 4 changes the rotor structure of Motor 1, as can be seen in Fig. 1(b) while Motor 5 modifies the number of slots for Motor 4, as indicated in Table 2. The rotor design of Motors 4 and 5 remains the same, as shown in Fig. 1(b). The performance is evaluated by keeping the same number of turns per coil in the windings and the current density of all the motors. The slot fill factor is modified from 45% (for Motors 1, 2 and 4) to 42.5% for Motor 3 because of the larger slot area with narrower teeth. The slot fill factor

![Fig. 7. The iron loss of IPM motor in rotor and stator](image)

![Fig. 8. The efficiency with different electric steel materials](image)

---

**Table 4. Comparison of motor characteristics (110 A, 43°E)**

<table>
<thead>
<tr>
<th>Model</th>
<th>Torque (Nm)</th>
<th>Ld (mH)</th>
<th>Lq (mH)</th>
<th>Iron Loss (W)</th>
<th>Eff (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>T1</td>
<td>56</td>
<td>0.438</td>
<td>1.322</td>
<td>462</td>
<td>92.8</td>
</tr>
<tr>
<td>T2</td>
<td>55.4</td>
<td>0.436</td>
<td>1.307</td>
<td>252.6</td>
<td>94.2</td>
</tr>
<tr>
<td>T3</td>
<td>54.6</td>
<td>0.435</td>
<td>1.286</td>
<td>113.5</td>
<td>94.8</td>
</tr>
<tr>
<td>T4</td>
<td>54.9</td>
<td>0.438</td>
<td>1.289</td>
<td>234</td>
<td>94.1</td>
</tr>
<tr>
<td>T5</td>
<td>55.1</td>
<td>0.442</td>
<td>1.3</td>
<td>396.2</td>
<td>93.1</td>
</tr>
<tr>
<td>T6</td>
<td>55</td>
<td>0.432</td>
<td>1.303</td>
<td>138.1</td>
<td>94.7</td>
</tr>
<tr>
<td>T7</td>
<td>55.4</td>
<td>0.432</td>
<td>1.317</td>
<td>174.3</td>
<td>94.5</td>
</tr>
</tbody>
</table>
Table 5. Flux density of five IPM motors (@110 A, 43°E)

<table>
<thead>
<tr>
<th>Items</th>
<th>Motor 1</th>
<th>Motor 2</th>
<th>Motor 3</th>
<th>Motor 4</th>
<th>Motor 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>B_Stator (T)</td>
<td>1.56 T</td>
<td>1.57 T</td>
<td>1.6 T</td>
<td>1.55 T</td>
<td>1.56 T</td>
</tr>
<tr>
<td>B_Rotor (T)</td>
<td>2.06 T</td>
<td>2.04 T</td>
<td>2.0 T</td>
<td>1.96 T</td>
<td>2.07 T</td>
</tr>
<tr>
<td>B_Air-gap (T)</td>
<td>0.79 T</td>
<td>0.9 T</td>
<td>0.79 T</td>
<td>1.01 T</td>
<td>0.97 T</td>
</tr>
<tr>
<td>Torque (Nm)</td>
<td>55.4</td>
<td>56.2</td>
<td>52.1</td>
<td>59</td>
<td>56.8</td>
</tr>
</tbody>
</table>

for Motor 5 is 46% due to its smaller number of slots. Despite the smaller number of slots in Motor 5, the back EMF constant is kept the same as that for Motor 4 and the winding resistance is only 7% lower. Therefore, they would possess a similar flux weakening capacity under maximum voltage.

The flux density distributions of the five IPM motors at the peak load condition (110 A, 43°E phase advance) are shown in Fig. 9. It can be seen that the operating regions of the stator teeth of all the motors are around 1.6 T, also as listed in Table 5. This has not saturated the thin lamination (20CS1500HF), even with the rotor providing the highest air gap flux density (Motors 4 and 5) or the stator with the narrowest teeth (Motor 3). The modified designs, Motors 2, 4 and 5 can improve the torque due to their rotor configurations that produce higher air gap flux density (Table 5). The tooth flux density of Motor 3 is higher than Motor 1 but the torque reduces due to the reduction of tooth width with keeping the slot magnetomotive force. The torque and flux density of Motor 5 are slightly smaller than that of Motor 4 due to the modified number of slots. Figure 9 also shows that all the rotor bridges are saturated. Thus, high saturation flux density materials should be used for the rotor to increase the torque and reduce the saturation.

Discussion:

From Fig. 9 and Table 5, it is known that the thin laminations in the stator may not be saturated with a proper design. Thus, the rotor design becomes the key factor affecting the torque. This also indicates that the use of high flux density materials in the rotor is necessary to improve the torque performance. Therefore, this highlights the advantages of employing material combinations for IPM motors, i.e. low iron loss laminations for stators and high flux density laminations for rotors. Note that the efficiency is almost unaffected.

3.2 Result Analysis—CPSR and Saliency

The inductance of each motor is analyzed. Figures 10–14 show the inductance profile of the five motors, where the trends of $L_d$ and $L_q$ of Motors 1, 2, and 3 are different from that of Motors 4 and 5. This is due to the different rotor structures. Based on the inductance profiles, the d-axis inductances of Motors 1 and 2 are higher than that of Motors 3, 4 and 5. Therefore, it is predicted that the field weakening ability of Motors 1 and 2 are better than that of Motors 3, 4 and 5.

Figures 15 and 16 show the saliency ratios, which range from 2.5 to 5.5 at the condition below the current 77 Arms. The motor performance is not significantly affected by current over 77 Arms. This is due to the d-q axis inductance drops at the saturated condition although the saliency ratio increases. Therefore, it is predicted that $k_{CPSR}$ of the five
moters ranges from 4 to 6. Table 6 presents the analysis results for the motors operating at peak condition. The CPSRs calculated by Eq. (7) are compared with that of FEM and the two cases agree well for all the models. It can also be seen that Motor 1 achieves the highest CPSR. Since all the motors have satisfied the basic requirement of 10 kW output power, Motor 1 based on Model T1 is chosen for prototyping as it has the highest CPSR.

Figure 17 shows the characteristic of electromagnetic torque $T_e$ and the output power $P_{out}$ versus speed at the peak condition. As can be seen, the calculated CPSR using Eq. (7) fits well into the simulations. Therefore, the accurate calculation of inductances is extremely important to evaluate the IPM motor performance. Note that the applied current is the same as that in Figs. 7 and 8.

Based on the previous analysis, a design process to improve the motor performance is presented, as shown in Fig. 18. The rotor should be considered first in this process as its significant effect on torque output. Low iron loss laminations should be used for the stator.

4. Experimental Validation

As mentioned above, the prototype of IPM motor was fabricated based on Motor 1, as shown in Fig. 19. The comparisons between the simulation and tests for the torque-power versus speed is shown in Fig. 20. As can be seen, the simulation and experiment agree well. However, the current angle cannot be freely adjusted because a commercial driver was used. In the tests, the current angle was fixed at 43 degrees and the simulations were then re-conducted using this current angle for direct comparison. This indicates that the motor could not be controlled to reach the maximum speed as stated in the specifications. In addition, the test could not be conducted...
beyond 3600 rpm because of the limitation of the laboratory facilities. Nevertheless, the test results could still validate the reliability of FEM and indirectly validate the design and analysis in this paper.

5. Conclusions

This paper has investigated the effect of thin electrical steel laminations on the performance of IPM motors. It was found that the utilization of the high saturation flux density materials in rotor combining with the thin laminations in stator could improve the performance and reduce the cost. The performance of the IPM motors with different rotor structures has been evaluated and compared in terms of torque, efficiency, field weakening ability, and saliency ratio. A design process to improve the motor performance was then proposed based on the analysis. A prototype was fabricated and the experiment has verified the simulations.

Acknowledgment

This work was supported in part by NSPO of NAR Labs, Taiwan and the project co-funded by China Steel Corporation and Ministry of Science and Technology, Taiwan under contract 104-2622-8-006-001. The author would like to thank Electric Motor Technology Research Center of National Cheng Kung University for technically supporting this work. Mr. Thai Hao Nguyen and Hsiu-Fu Kuo are acknowledged for their assistance in experiments.

References