Energy-on-Demand System Based on Combinatorial Optimization of Appliance Power Consumptions

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Received: June 30, 2016, Accepted: October 31, 2016

Abstract: In this paper, the author proposes an Energy-on-Demand (EoD) system based on combinatorial optimization of appliance power consumptions, and describes its implementation and evaluation. EoD is a novel power network architecture of demand-side power management, whose objective is to intelligently manage power flows among power generations under the limitation of available power resource. In an EoD system, when total power consumption exceeds the limit of power resource, a power allocation manager deployed in the system decides the optimal power allocation to all the appliances based on their importance and power consumptions, and controls the amount of power supplied to the appliances in a way that causes minimum undesired effect to quality-of-life of users. Therefore, one of the most crucial factors in an EoD system is the strategy for deciding the optimal power allocation. From a mathematical viewpoint, the power allocation management in an EoD system can be considered as an optimization problem of appliance operation modes. In the developed system, power allocation is based on the multiple-choice knapsack problem (MCKP), a kind of combinatorial optimization problem. The system measures power consumption of appliances, computes the optimal power allocation based on an algorithm for the MCKP, and realizes computed power allocation by controlling IR-controllable appliances and mechanical relays. Through experiments, the developed system is confirmed to work properly as an EoD system by observing system behaviors when the total power consumption exceeds the upper limit of the available power resource.

Keywords: Energy-on-Demand, power allocation management, multiple-choice knapsack problem

1. Introduction

In recent years, efficient usage of limited amount of electrical energy has been an important issue. For example, in the so-called “demand-response” system, consumers are requested to save electricity usage to balance the amount of power demand and supply for improving power network stability. Consequently, it is crucial to utilize the limited amount of available power in an efficient manner. Various approaches have been taken to support consumers to do their power-saving activities. Typically, the “energy usage visualization” system, which collects power consumption data of appliances in a home and visualizes them to consumers in some graphical ways, has certain helpful effect for consumers [1]. On the other hand, even if visualized data are presented, actual power-saving activities still require manual operations by users, which makes it not always easy to keep the activity in daily life. Though decision-making on controlling the amount of power to appliances is crucial to power-saving in user’s daily life [2], [3], it is not always properly done by ordinary users since their awareness on the amount of power consumption of appliances or their electricity bills is not necessarily high [4], [5]. If users do not have sufficient knowledge on the amount of power consumption of appliances they use, there is no guarantee to achieve their power-saving goals.

Energy-on-Demand (EoD) [6] is a recently-proposed novel power network architecture of demand-side power management, whose objective is to intelligently manage power flows among power generations under the limitation of the amount of available power resource. In an EoD system, the importance of each appliance is explicitly parameterized, and the amount of power consumption of appliances is measured by power sensors; then, if total amount of power consumption exceeds the limitation of power resource, a power allocation manager deployed in a home makes a decision on power allocation for appliances based on the parameters, capacity of the power source and various factors such as users lifestyles etc., and controls the amount of power supplied to the appliances in a way that minimizes undesired effect on quality-of-life (QoL) of users. Therefore, one of the most crucial factors in an EoD system is the strategy for deciding the optimal power allocation to appliances [7]. For optimizing power allocation, the power management system optimizes power allocation (e.g., up to 200 W for a TV, 30 W for a fan) considering user’s QoL, and when total power consumption exceeds a threshold value the system automatically controls power allocation based on control policies suited for users, assuming situations where total usable power is limited in demand-response scheme or for reducing peak load. Figure 1 shows the concept of optimal power allocation.

From a mathematical viewpoint, the power allocation management in an EoD system can be considered as an optimization problem; the problem where the goal is to choose the power allocation to appliances optimized for users from various possible combinations of appliance statuses, keeping total consumed power under the limitation. In real environments, many appli-
Ance have various operational modes in addition to simple on/off states, and it is not easy to find the most optimized combination of operation modes from many possible candidates. Moreover, the problem cannot be easily solved by linear programming methods since the importance of an appliance for users is not in proportion to the amount of power consumption, and since the amount of power consumption of many appliances varies in a step-wise manner with the change of operation modes. Hence the system should be able to flexibly and properly change operational modes of appliances for realizing the decided power allocation, since most appliances do not work properly if the system simply reduces the amount of power supplied to them.

In this research work, we propose power allocation management is considered as combinatorial optimization of appliance power consumptions as an alternative approach than the priority-based ones, and discuss the design, implementation and evaluation of an EoD system based on the combinatorial optimization. Power allocation schemes in existing EoD systems are priority-based, not based on the combinatorial optimization, where priority parameter is associated with each appliance, and the power allocation manager reduces the amount of power allocated to the appliance with lowest priority among the appliances [6], [8], [9], [10]. We formulate the power allocation as the multiple-choice knapsack problem (MCKP) [11], a kind of combinatorial optimization problem. The MCKP is an extended version of the simple knapsack problem; in the MCKP, class (an appliance) is a set of items (operation modes). Each item has parameters of size (power consumption) and profit (the importance to user’s life). A knapsack corresponds to a power source, and its capacity is the limit of available power resource. The objective of the problem is to find the optimal set of items packed into the knapsack that maximizes total obtained profit. Here exactly one item should be chosen from a class and should be packed into the knapsack in a way that the total size of packed items does not exceed capacity of the knapsack. The system is implemented utilizing a smart outlet network, where the power consumption of all the appliances is frequently (every one second) measured by power sensors. When the total amount of consumed power exceeds the upper limit, the power allocation manager deployed in the system computes the new optimal allocation using an algorithm for the MCKP, and sends control messages to appliances.

To control ordinary IR-controllable appliances with various operation modes other than simple on/off states, we have adopted a programmable IR control unit controllable from the manager via Wi-Fi, which enables the system to flexibly control the operation modes of IR-controllable appliances by sending pre-recorded IR signal patterns. Through experiments, the developed system is confirmed to work properly as an EoD system by observing system behaviors when the total power consumption exceeds the upper limit of the available power resource.

This paper is consists as follows; Section 2 refers related work. Section 3 presents a basic concept of EoD and formulation of power allocation as a combinatorial optimization problem. In Section 4, we discuss our implementation of the developed power allocation system. Section 5 describes experiments and considerations. Section 6 concludes this paper. This paper is an extended version of our preliminary work [12]; we have enhanced it by adding evaluations on the system behavior, descriptions of problem formulation including the assumed method for setting parameters, and considerations on important topics such as feasibility of the system in real-life environments.

2. Related Work

As described in the previous section, power allocation schemes in existing EoD systems are priority-based, not based on the combinatorial optimization, where priority parameter is associated with each appliance, and the power allocation manager reduces the amount of power allocated to the appliance with lowest priority among the appliances [6], [8], [9], [10]. The major difference between the combinatorial optimization based approach and the priority-based approach lays in their power reduction schemes, especially when the total amount of power consumption exceeds an upper limit; a fundamental scheme of the priority-based algorithms is to repeatedly reduce the amount of supplied power for an appliance with lowest priority until total power consumption becomes less than the limit. The beneficial aspect of the combinatorial optimization based algorithm is that the power allocation can be done based on specific measures by setting an appropriate objective function, and the decision of the optimal modes of multiple appliances is completed by a single calculation. On the other hand, in the priority-based approach, configuring parameters might be relatively straightforward since only one appliance is controlled in a single operation. In general schemes of power management in Automated Demand Response or Home Energy Management System, priority-based methods are commonly used [13]. There have been other research work where optimization problems are considered in diverse formulation, and various simulational and theoretical studies have been conducted [14]. For example, the research work by Lee et al. [15] considered combinatorial optimization of power consumption patterns of appliances to reduce peak load of total power consumption. Adika and Wang investigated a method for autonomous scheduling of electrical appliances in a grid connected household with photovoltaic energy [16]. Kumaraguruparan et al. formulated a scheduling problem based on the multiple knapsack problem, in which daily power-consuming tasks are allocated to time slots with different electricity bills to minimize total elec-
tricity bills, and made a simulation-based evaluation [17].

There have been noteworthy studies on optimizing power consumption in homes by quantifying the relationship between the importance of an appliance and the amount of power consumption. Sianaki et al. formulated the optimal power allocation as the knapsack problem, proposed a method for parameterizing the importance of each appliance by applying the analytic hierarchy process (AHP), and presented results obtained by numerical simulations [18]. Kempton and Montgomery proposed a “folk quantification” method [19] to quantify the importance of appliance use in homes.

3. Concept and Formulation

This section describes the EoD concept and problem formulation of power allocation in EoD.

3.1 EoD Concept

In a conventional power network in homes, power consuming devices (appliances) can be supplied with power if only they are connected to power sockets and are turned on. Therefore, to achieve power-saving goals, users are required to have sufficient knowledge on how much power is consumed by each appliance, and should take careful and manual work to save electricity. In an EoD system, the importance of each appliance is explicitly parameterized, which corresponds to the strength of “power demand” from each appliance, and the amount of power consumption of appliances are measured by power sensors; then, if the total amount of power consumption exceeds the limitation of power resource, a power allocation manager deployed in the system makes a decision on power allocation for appliances based on the parameters, the amount of power consumption, varying capacity of the power source and various factors such as users lifestyles etc., and controls the amount of power supplied to the appliances in a way that causes minimum undesired effect to QoL of users and total power consumption does not exceed the limit. Figure 2 presents an overview of an EoD concept. In this example, there are two power-requiring appliances (a cleaner and a light). The power allocation manager decides the power allocation optimized to users life, based on parameters (power consumption and importance of appliances, upper limit of available power, etc.), and controls the amount of power supplied to the appliances (in this example, the light is supplied with power, while the cleaner is not).

3.2 Formulation as a Combinatorial Optimization Problem

Setting an objective function is a crucial factor in the formulation of an optimization problem, and there are many reasonable candidates of the objective function in modeling power allocation in an EoD system. In this research work, we have defined the objective function as maximization of user’s total benefit gained by being able to use appliances, based on a similar approach in former research work by Sianaki et al. [18].

Figure 3 shows an example situation where each appliance has its operational modes such as “high”, “mid” or “low”, each of which is associated with parameters of profit (determined with some quantification methods [18], [19]) and power consumption measured by power sensors. The task of the power allocation manager is to decide the optimal combination of the operational modes of the appliances, which maximizes total profit gained by selected modes. The most crucial constraint is that total power consumption of all appliances should not exceed the upper limit. Considering this constraint in home environments has become realistic, since recently some utility companies (e.g., Arizona Public Service [20] and TEPCO Energy Partner, Inc. [21]) has begun to offer price menus based on power consumption for residential customers, not only for corporate customers. In addition to that, there has been a proposal of the method to determine the upper limit of total power consumption in each time in a day based on energy-saving goal [6]; with this method, the upper limit of total power consumption in each time period is determined in a way that the energy saving goal is consequently achieved even if total power consumption is not always less than the limit. Therefore, the objective in the formulation is to determine the power allocation under the limitation which is properly determined.

In the simple knapsack problem, we are given a knapsack with capacity and set of items with profit and size, and our objective is to find a subset of items that maximizes total profit of items and total size does not exceed the capacity of the knapsack. The multiple-choice knapsack problem (MCKP) [11] is a natural extension of the knapsack problem; the items are classified into class, and the constraint is added that exactly one item must be packed into the knapsack from each class. The objective is the same as the simple knapsack problem. Here we define some mathematical symbols for problem formulation; the number of classes (appliances) is denoted by m, and a class $i (1 \leq i \leq m)$ is a...
set consisted of $n_i$ items (operational modes) $j(1 \leq j \leq n_i)$. For each item $j$, profit (importance for its user) $p_{ij}$ and size (power consumption) $w_{ij}$ are associated. A knapsack (a power source) has capacity (upper limit of total power usage) $c$. Exactly one item must be packed into the knapsack, which means that an appliance cannot work with multiple modes at the same time (here operational modes contain the “off” status). A decision variable $x_{ij} \in \{0, 1\}$ means whether item $j$ is chosen from class $i$; namely, if $x_{ij} = 1$, appliance $i$ works with operational mode $j$, and $x_{ij} = 0$ means $i$ works with some other mode than $j$.

The profit parameters of each operation mode of power consuming devices should be decided properly reflecting user’s preferences. The most straightforward method is that user manually determine them, and it seems reasonable to prepare some preset patterns of parameters for dealing with some major or typical situations. On the other hand, it is difficult for users to manually determine the profit parameters in a way that properly reflects their preference, especially when the number of appliance operation modes are large and fixing parameter is a complicated task. It is therefore helpful for users that some scheme is available to determine the parameters in a systemized manner. One possible candidate method for deciding the profit parameters systematically is analytic hierarchy process (AHP), which is the powerful technique to quantify importance of each choice in decision-making process by utilizing questionnaire for users, and has been applied in the quantification of user’s preferences in power allocation to appliances [18].

The formulation of the MCKP is presented below (here $N_i$ is a set of items in class $i$). The first constraint means that the total size of packed items should not exceed capacity of the knapsack. The second and third constraints mean that exactly one item should be chosen from each class and packed into the knapsack.

$$\max \sum_{i=1}^{m} \sum_{j \in N_i} p_{ij} x_{ij}$$

subject to

$$\sum_{i=1}^{m} \sum_{j \in N_i} w_{ij} x_{ij} \leq c,$$

$$\sum_{j \in N_i} x_{ij} = 1, \quad i = 1, \ldots, m,$$

$$x_{ij} \in \{0, 1\}, \quad i = 1, \ldots, m, \quad j \in N_i.$$

4. System Design and Implementation

The design of the system is an extension of the former prototype system [22], which was based on an algorithm for the simple knapsack problem and was capable of on/off control utilizing smart outlets, which are the power strips with functions of power measurement, communications and power control with mechanical relays. Figure 4 presents the overview of the developed system, which we assume is suitable for ordinary homes. The system architecture is designed in a centralized manner, where the power allocation manager takes all the crucial decisions. The manager stores data of possible operational modes of each appliance, values of parameters (profit and size) of each mode, control methods available for each appliance (IR-controllable or relay-only). The manager also collects real-time data of power consumption of each appliance (every one second), and when the total amount exceeds the upper limit it calculates optimal power allocation utilizing a dynamic-programming algorithm for the MCKP. Finally, the manager sends control messages to realize calculated power allocation; if the appliance to be controlled is IR-controllable, the manager first sends the corresponding control message to the Wi-Fi capable IR remote control, then the control sends IR signals to the appliance. Otherwise i.e., the appliance is not IR-controllable hence no direct mode control method is available, the manager sends a control message to the smart outlet to which the appliance is connected, and the outlet turns on or off the corresponding socket. Table 1 shows the list of data stored and maintained by the manager.

Table 1 Data stored and maintained by the manager.

<table>
<thead>
<tr>
<th>Items</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Appliance IDs</td>
<td>Name of appliances</td>
</tr>
<tr>
<td>Operational modes</td>
<td>Possible operational modes</td>
</tr>
<tr>
<td>Available control methods</td>
<td>IR-controllable or relay-only</td>
</tr>
<tr>
<td>IR control messages</td>
<td>For IR-controllable appliances</td>
</tr>
<tr>
<td>Relay control messages</td>
<td>For relay-only appliances</td>
</tr>
<tr>
<td>Parameters of each operation mode</td>
<td>Profit and power consumption</td>
</tr>
<tr>
<td>Current power consumption</td>
<td>Measured by smart outlets</td>
</tr>
<tr>
<td>Capacity of the power source</td>
<td>Current upper limit</td>
</tr>
<tr>
<td>Current modes of appliances</td>
<td>For proper control of the system</td>
</tr>
</tbody>
</table>

4.1 Design and Implementation of Hardware and Software

4.1.1 Power Allocation Manager

In hardware aspects, the system consists of the power allocation manager, the smart outlets and the IR remote control, all of which are deployed in an IEEE802.11n Wi-Fi network. We assumed that, in realistic environments, the power allocation manager is not expected to have rich computational resources compared with personal computers such as laptop/desktop PCs, and it likely has similar specifications as embedded computers such as home controllers. Therefore, we adopted Raspberry Pi 2 model B\(^{1}\), a microcomputer with sufficient specifications and programmability, as the hardware of the power allocation manager. Table 2 shows its specifications.

Fig. 4 System overview.

Table 2 shows its specifications.

4.1.2 Smart Outlet

The smart outlet used on the developed system is the extended version of the one formerly developed [23]; we have improved the outlet to be more compact and practically designed, and have extended computational resources. Figure 5 is an outward ap-
Table 2 Specifications of the power allocation manager.

<table>
<thead>
<tr>
<th>Items</th>
<th>Specs</th>
</tr>
</thead>
<tbody>
<tr>
<td>CPU</td>
<td>ARM Cortex-A7 700 MHz Quad-Core</td>
</tr>
<tr>
<td>RAM</td>
<td>1 GB</td>
</tr>
<tr>
<td>Communication media</td>
<td>IEEE802.11n Wi-Fi</td>
</tr>
<tr>
<td>Interface</td>
<td>USB 2.0</td>
</tr>
<tr>
<td>OS</td>
<td>Raspbian (Debian-based Linux)</td>
</tr>
</tbody>
</table>

The software in the system has been developed using the standard C language. Since there is no straightforward method to grasp current operation modes and statuses of ordinary appliances from outer devices, the system has to keep the current operation modes of appliances by tracking the variation of modes from the initial state. The manager also stores data of IR control messages for changing modes of IR-controllable appliances, relay-control messages for controlling non IR-controllable appliances, and values of (pre-measured) power consumption and profit parameters associated to each operation mode of appliances. The communication in the Wi-Fi network among the manager, smart outlets and the IR control is done via standard TCP/IP socket protocols.

4.2 Network

The Wi-Fi used in the network is IEEE 802.11n with maximum bandwidth of 300 Mbps using 2.4 GHz of frequency and is protected with WPA encryption for easier coordination with ordinary information devices such as PC, tablets or smartphones. As a transport layer protocol, we have chosen TCP for reliability, dependability and safety, because the system does control electricity actively, not only gathering data on power consumption.

4.3 Data Formats

Measured power consumption data and relay control messages are formatted in XML-like manners as follows, considering the extendibility, versatility and easier handling [23].

- **Measured Power Consumption Data:**
  The below is an example of notice_wattmeter, which is used for sending measured power consumption data (approximately 540 bytes). This example means that integrated power on socket #2 is 64 Wh, instantaneous voltage is 100.585 V, current is 0.831 A, instantaneous effective power is 48.8 W, and the relay at the socket has been turned on.

```xml
<root><info>
  <kind>notice_wattmeter</kind>
  <time>20160509213008175</time>
</info><data>
  <socket1><wh>100.519</wh><volt>100.568</volt><current>0.002</current><watt>0.8</watt><state>OFF</state></socket1>
  <socket2><wh>100.585</wh><volt>100.585</volt><current>0.831</current><watt>48.8</watt><state>ON</state></socket2>
  <socket3><wh>100.568</wh><volt>100.568</volt><current>0.511</current><watt>33.7</watt><state>ON</state></socket3>
  <socket4><wh>100.568</wh><volt>100.568</volt><current>0.511</current><watt>33.7</watt><state>ON</state></socket4>
</data></root>
```

- **Relay Control Message:** The below is an example of allocation manager. When the manager takes control of an IR-controllable appliance as a result of calculation, the manager first sends a text-based control message to the IRKit via Wi-Fi, then the IRKit transforms the message into IR signals and sends it to the appliance, realizing the decision made by the manager.

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4.1.3 Software

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  <socket3><wh>100.568</wh><volt>100.568</volt><current>0.511</current><watt>33.7</watt><state>ON</state></socket3>
  <socket4><wh>100.568</wh><volt>100.568</volt><current>0.511</current><watt>33.7</watt><state>ON</state></socket4>
</data></root>
```

- **Relay Control Message:** The below is an example of
the number of operation modes of appliance defined before, the number of appliances is denoted by the system. Algorithm 1 presents its formal description. As Choice Knapsack Problem [25]

\[ P(i, d) = \max \{ P(i, d - w_j) + p_j | j = 1, \ldots, n \} \]

4.4 Dynamic-programming Algorithm for MCKP

When all the classes have only one item, the MCKP corresponds to simple knapsack problem. Therefore the MCKP is NP-hard, since it includes the knapsack problem as a special case and the knapsack problem is NP-hard [24]. However, it has been shown that there is a dynamic-programming algorithm for the MCKP that obtains an optimal solution in pseudo-polynomial time [25]. Hereafter, we treat the power capacity and the amount of power consumption as integers (note that the smart outlet is able to measure the power consumptions to one decimal place and the algorithm is able to handle real numbers by increasing the number of digits, though there is trade-off between accuracy and computational time).

We have implemented the dynamic-programming algorithm in the system. Algorithm 1 presents its formal description. As defined before, the number of appliances is denoted by \( m \), and the number of operation modes of appliance \( i \) is denoted by \( n_i \). \( P(i, d) \) denotes an optimal solution of the subproblem with classes of \( 1, \ldots, i \) (1 \( \leq \) \( i \) \( \leq \) \( m \)) and a knapsack with capacity of \( d \) (1 \( \leq \) \( d \) \( \leq \) \( c \)). Generally, a dynamic-programming algorithm is based on principle of optimality; the algorithm first obtains the optimal solution of an instance with smaller size, then constructs the optimal solution for a larger instance in a step-by-step manner. In the case of the MCKP, the dynamic-programming based algorithm first treats the instance with limited capacity and a subset of items. Then, by using solutions for smaller instances and the recursions \( P(j, d) = P(i - 1, d - w_j) + p_j \) or \( P(j, d) = P(i - 1, d) \), we can obtain the optimal solution of the instance with classes \( 1, \ldots, i \) and the knapsack with capacity \( d \), based on the optimal solutions of the smaller instance with limited classes \( 1, \ldots, i - 1 \) and the knapsack with capacity smaller than \( d \). Through the algorithm execution, the system records the set of selected appliance modes that achieves the optimal profit \( P(i, d) \) for each subproblem so that it is able to control the modes in a way that realizes the final optimal solution.

5. Experiments and Considerations

This section describes observations of the system behavior when the upper limit of an available power resource is dynamically changed, shows required time for communication/calculation of power allocation/power control, and presents some considerations.

5.1 Experiments

For presenting the result clearly, here we describe behavior of the system with a small number of appliances. Figure 6 presents an example configuration of the developed system, which includes an IR-controllable fan (with modes of “off”, “low” and “high”, an IR-controllable light (with modes of “off” and “on”), a laptop (not IR-controllable) and a battery charger (not IR-controllable). In this example configuration, the profit parameters of appliances are manually set based on user’s preference. The power consumption parameters of the appliances are set as 50 W for the laptop, 18 W for the fan with “low mode” and 35 W for “high” mode, 3 W for the light and 5 W for the battery charger, based on pre-measured power consumption of each appliance. The power allocation manager checks whether the total power consumption exceeds the limit every one second, and when exceeding the limit it calculates the new power allocation based on the pre-measured power consumption values. The profit values of the appliances are set manually as 200 for “on” mode of the laptop, 50 and 100 for “low” and “high” modes of the fan respectively, 30 for “on” mode of light, and 10 for “on” mode of the battery charger. Also, “off” mode of each appliance has profit of 0.

We have observed how the developed system controls appliance operation modes by recalculating the optimal power allo-
The first power control taken by the system can be observed from the zeroth second to around 150th seconds, the upper limit is set to be 100 W; therefore, the fan works with its “high” mode and the other appliances are turned on with no limitation. Total profit obtained is $340 (\approx 200 + 100 + 30 + 10)$. 

The first power control taken by the system can be observed around 150th seconds when the upper limit is set as 80 W. Since the total power consumption exceeds the limit, the power allocation manager computes the new optimal power allocation. As a result, the fan is set to be “low” mode by a control message sent by the manager, and total power consumption became less than the limit. Hereafter, the upper limit changes periodically (every 30 seconds). Total profit obtained is $290 (\approx 200 + 50 + 30 + 10)$.

The second power control is observed around 180th seconds when the upper limit is set as 60 W. At the result of the new optimal power allocation, the fan is turned off, while the allocation to other appliances are unchanged. (The power consumption of the fan temporarily increased and immediately dropped at around the 180th seconds, because the manager must control the fan to be turned off via temporal “high” mode due to its hardware specification.) Total profit is $240 (\approx 200 + 30 + 10)$; here we can observe that system chooses the fan to be turned off, since the profit of the laptop is higher than that of the fan.

Next, we set a new upper limit of 40 W around 210th seconds. The decision by the manager is that the laptop and the battery charger should be turned off since 40 W of available power is not sufficient to supply power to them, instead the fan is controlled to be “high” mode since there is sufficient available power to supply the fan as the laptop and the battery charger are turned off. Total profit obtained is $130 (\approx 100 + 30)$; here we can observe that system chooses the battery charger to be turned off, since the profit of the light is higher than that of the charger.

Similarly, when the limit is changed to 20 W at the 240th seconds and 10 W at the 270th seconds, the new power allocation is recalculated as optimized for each new setting. In particular, at the 240th seconds, it is observed that the system choose the fan to be its “low” mode, since it has profit of 50 which is higher than the sum of the profit of the battery charger and the light (40+10+30).

When the limit is recovered to 100 W around 300th seconds, the power resource is sufficient and all the appliances are fully allocated with power, i.e. the fan works with “high” mode and all the other appliances are turned on.

These observations through the experiment indicate that the system works properly as an EoD system. By deploying the system in a real-life environment and changing the upper limit, we also have confirmed that the system is able to handle other ordinary appliances such as an IR-controllable air conditioner, a TV, audio systems, a coffee maker or a hair dryer, etc., some of which consume the larger amount of power than the appliances used in the example configuration.

We have measured time required to compute the optimal power allocation by using the algorithm for the MCKP. The calculation of the optimal allocation is completed less than one second on the power allocation manager (Raspberry Pi 2) when example instances have 24 appliances with five modes and the upper limit is set as 3000 W, and less than 100 milliseconds when four appliances with three modes. Therefore, the time needed for the calculation is sufficiently short. In the experimental environment, to control an appliance required at most around six seconds when multiple IR signals should be sent to an IR-controllable fan. It is shown that relay control by the smart outlet can be done in averagely 29.3 milliseconds after receiving a relay control message, using Wi-Fi 802.11n as a communication media and the standard TCP/IP socket communication [22]. Hence, in a real-world environment, the implemented system is also expected to work as a circuit breaker and is beneficial for avoiding damage caused by overcurrent, overload or short circuit, though the main purpose of the system is optimizing power allocation.

5.2 Considerations

Full installation of the proposed system in real-life environment requires users additional cost, knowledge and effort to construct and maintain the system properly. On the other hand, the proposed system is able to be installed partially in exchange for precision and capability of control; for example, if we admit the system to use approximate power consumption values in the calculation of total power consumption instead of real-time measured values, power sensors are not necessary though the precision of power control is inevitably limited as trade-off. Similarly, if a user decides that it is sufficient for the system to control only IR-controllable appliances, mechanical relays installed in the smart outlet is also unnecessary.

In the experiments, sending IR-control messages requires marginal time, since IR-controllable appliances sometimes failed to receive the control signals if they are sent fast and continuously. Also, since the calculation of power allocation is done using pre-measured power consumption of each appliance, sometimes there appears some unintentional deference between assumed power consumption, with the upper limit being changed over time. Figure 7 shows the variations of total power consumption and power consumption by each appliance over time, where the X axis represents time (second), and the Y axis represents power consumption (W). The experiment was conducted in the following scenario.

(1) From the zeroth second to around 150th seconds, the power consumption by each appliance over time, where the X axis represents time (second), and the Y axis represents power consumption (W). The experiment was conducted in the following scenario;

(2) When the battery charger to be turned off, since the profit of the laptop is higher than that of the charger. Total profit obtained is 340 ($=200+100+30+10$).

(3) When the limit is recovered to 100 W around 300th seconds, the power resource is sufficient and all the appliances are fully allocated with power, i.e. the fan works with “high” mode and all the other appliances are turned on.
consumption and actual power consumption, which causes inefficiency in utilizing available power resources. In addition to that, as long as the power allocation and control is done in periodically, it is inevitable that sometimes total power consumption temporally exceeds the upper limit, which is a common issue in EoD systems [6]. Frequency of data collection and power control should be optimized for real-life situations, considering various factors such as the variation of appliances’ power consumption, trade-off between control precision and computational load, etc.

Some of the limitations of the developed system depend on functional restrictions of today’s ordinary appliances; there is no straightforward method to grasp their current operation modes or internal statuses from outer devices such as the power allocation manager. The system therefore should properly manage statuses of all the appliances, which is not always possible in a real-life environment since the appliance operation modes can be manually changed by users and it is not easy for the system to precisely detect or handle manual mode changes. After the system fails to detect the manual operation, the control by the system does not work properly since the actual modes differ from the modes assumed in the system.

Though the estimation methods for recognizing operation modes of appliances from power consumption [26] should be useful, the complete solution for these technical problems can be achieved only by utilizing so-called smart appliances, which are capable of communicating the internal statuses with other devices based on communication standards for smart appliances such as ZigBee Smart Energy Profile [3], Apple HomeKit [4] or ECHONET Lite [5]. Therefore, we are considering to extend the developed system being capable of handling these protocols, and conduct real-life experiments. In this context, the noteworthy feature of USB Power Delivery (USB PD) [6] is its smart power supplying scheme; a USB PD ready power consuming device communicates with a power supplying device, negotiates about the amount of power it is allowed to consume, and is able to adapt its mode best suited for available power amount. For developing a more sophisticated and flexible EoD system, it is strongly desired that the appliances have similar smart functions.

### 6. Conclusion and Future Work

In this paper, we have considered the power allocation management in an EoD system as a combinatorial optimization of appliance power consumptions, and have discussed the design and implementation of an EoD system using the dynamic-programming algorithm for the multiple-choice knapsack problem. The system finds the optimal combination of appliance operation modes under the limitation of available amount of power, and controls the amount of power supplied to appliances using the IR control and mechanical relays in smart outlets. Time required for calculating the optimal allocation is sufficiently short when we consider instances with realistic size (24 appliances with five modes, upper limit set as 3000 W). We have confirmed that the developed system works properly as an EoD system by observing system behaviors when the total power consumption exceeds the upper limit of the available power resource.

In the developed system we focused on keeping restrictions on instantaneous power, however there are other reasonable factors to be considered as well; for example, assuming the Time-of-Use pricing in demand response systems, it is reasonable to control power consumption to minimize the electricity cost, not only considering restrictions of instantaneous power. Since the combinatorial-based approach we have taken can be extended to other objective functions (the total energy consumption, electricity cost, CO₂ emission, etc.), we are planning to additionally implement a scheduling scheme in the developed system, where the parameter setting is based on real-life power consumption data and patterns measured over one year [23]. In developing scheduling strategies, it should be of importance and interesting to consider uncertain factors such as price uncertainty [27].

Another future research direction is to make experimental comparisons of two power allocation approaches (the combinatorial optimization based approach and the priority-based approach) in real-life environments, since they have different characteristics; the combinatorial optimization based algorithm decides all the operation modes in a single calculation, while the priority-based algorithm repeats to select an appliance based on its priority parameter and reduce the amount of supplied power for it until total power consumption decreases to be less than the upper limit.

One of the important future work topics for applying the developed system in real-life situations is to pursue a method to decide the profit parameters of appliances. The methods for systematically parameterize the importance of appliances are the common challenging problem in EoD systems (e.g., Ref. [28]). The profit parameters of appliance modes should dynamically change over time, depending on various factors such as temperature value. We are considering to apply the methods for quantifying user’s preference such as the AHP [18] or folk quantification [19], based on patterns of user’s behavior and power consumption data in a real-life environment, which can be grasped by the smart outlet network for energy-aware services utilizing various sensor information (motion, temperature, humidity, etc.) [23]. In conducting the AHP in real-life environments, decision of criteria and the questionnaire setting should be crucial factors, and further investigation is needed to verify whether the criteria and questionnaire settings adopted in former work [18] are applicable to our system in real-life environments, since they possibly require modifications or adjustments. This investigation should require large experiments involving people with various power consumption preferences and lifestyles. Also, as pointed out by Kato et al. [6], it is crucial to develop user interfaces for updating parameters including user preferences and the upper limit, which helps the system to flexibly react to sudden changes of situations or user’s feeling.

We expect the developed system works as a test-bed for real-life application of the other optimization methods which have been studied in theoretical or simulational manners. Also we are considering to pursue more sophisticated system with a smart rule-based scheme which realizes EoD by determining the power requests from policies and the appliances specification [9], since

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*3 http://www.zigbee.org/
*4 http://www.apple.com/ios/homekit/
*5 http://www.echonet.jp/english/index.htm
*6 http://www.usb.org/developers/powerelementary/
the computational resource of the smart outlet and the power allocation manager is sufficient for the rule-based power management system [23].

Acknowledgments The author would like to thank anonymous reviewers for their helpful comments, and EneGa Co., Ltd. for their cooperation in developing the smart outlet. This work was supported by JSPS KAKENHI Grant Number 15K15979, JST Super Cluster Program, and NICT Advanced Telecommunication Research Fund.

References


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