Characterization and Modeling of Manganese Effect on Strength and Strain Hardening of Martensitic Carbon Steels

Artem ARLAZAROV,1,3)* Olivier BOUAZIZ,1,2) Alain HAZOTTE,3) Mohamed GOUNÉ4) and Sébastien ALLAIN1)

1) ArcelorMittal Global Research and Development, Voie Romaine-BP30320, 57283 Maizières-lès-Metz Cedex France. 2) Centre des Matériaux, Ecole des Mines de Paris, CNRS UMR 7633, B.P. 87, 91003 Evry Cedex, France. 3) Laboratoire d’Étude des Microstructures et de Mécanique des Matériaux (LEM3), CNRS UMR 7239, Université de Lorraine, 57012 Metz Cedex, France. 4) Institut de Chimie de la Matière Condensée de Bordeaux (ICMCB), CNRS UPR 9048, 87 avenue du Docteur Schweitzer, 33609 Pessac, France.

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Carbon and manganese combined effect on the mechanical behavior of martensite was characterized and analyzed using literature and new experimental data of various carbon-manganese steels. A synergy effect of carbon and manganese on the martensite strength and strain hardening was detected and was then taken into account in a specific way in the simplified model, based on a Continuous Composite Approach. Model was adjusted with only one fitting parameter and the obtained results are in good agreement with experimental stress-strain curves.

KEY WORDS: martensite; carbon; medium Mn; strain-hardening; modeling.

1. Introduction

Martensite is one of the hardest phases in the steel and also one of the most complex due to its “natural” nanostructure. Development of almost all very high strength steels for automotive or industry market is hardly possible without use of this constituent. Dual-Phase steel is a common example of martensite use, when its strength is combined with the ductility of ferrite to offer a large range of strength-ductility balances for different applications. A lot of studies concerning martensite structure and strength are already done and the obtained scientific knowledge is synthesized in form of reviews.1,2)

Mechanical behavior of martensitic steel seems to be mainly controlled by one major factor – its initial carbon content. The evolution of martensite hardness related to its carbon content3) is probably the most generally acknowledged correlation between a mechanical and a metallurgical parameter. Influence of other microstructural characteristics like sizes of laths, packets or prior austenite grains is still widely discussed in the literature.3–5)

Surprisingly, the amount of considerations in the literature about strain-hardening mechanisms of martensitic steels is quite low, probably related to their poor uniform elongation (i.e. necking strain). Principally, the mechanical behavior of martensite is described either with phenomenological polynomial law6) or it is reduced to an elastic or an elastic-perfectly plastic law.7) However, recently a Continuous Composite Approach (CCA) was proposed to predict the complete tensile curves of as-quenched martensitic steels.8) The general idea of this approach is to consider martensite as a composite of elastic-perfectly plastic phases in interaction. All the phases have the same Young modulus, and the density of probability to find a phase with a given yield strength defines the so-called “stress spectrum”. This permits to describe the tensile behavior of martensite in a univocal way.

Although, there is an important quantity of data about different alloying elements influence on the martensite hardness,9,10) a few data are found about the substitutional elements influence on the strain hardening of martensitic steels.11) In the present work, Mn effect on the strain hardening of martensitic steels is characterized. Based on CCA a simplified model to describe the mechanical behavior of martensite is proposed and a special manner to introduce the influence of Mn addition is suggested.

2. Experimental Procedure

Four steels with different combinations of carbon (C) and manganese (Mn) contents were prepared using vacuum induction melting. The chemical compositions of these steels, as well as of some selected C–Mn steels from previously published studies are shown in Table 1. The slabs were hot rolled, and then cold rolled to 1.2 mm thickness. Cold rolled specimens were austenitized 1000°C above Ac1 temperature (the temperature is indicated in Table 1) for 30 minutes, and then water quenched (~1 000°C/s). For each steel two tensile tests at a constant strain rate of 0.008 s−1 were performed on the samples with gauge length 50 mm and width 12.5 mm, according to the ISO procedure. Table
Fig. 1. (a) and (b) are the microstructures of two medium Mn steels revealed with Dino etching and observed with optical microscope, (c) and (d) are their respective X-ray spectra: (a) and (c) – 0.1C–5Mn, (b) and (d) – 0.15C–5Mn.

Table 1. Chemical composition of studied and previously published steels (wt.%), holding temperature for the studied steels and corresponding references. For each steel first column gives the reference (Steel) that will be used further in the article.

<table>
<thead>
<tr>
<th>Steel</th>
<th>Composition (wt.%)</th>
<th>Thold (°C)</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C</td>
<td>Mn</td>
<td>Si</td>
</tr>
<tr>
<td>0.3C</td>
<td>0.29</td>
<td>1.20</td>
<td>0.25</td>
</tr>
<tr>
<td>0.36C</td>
<td>0.36</td>
<td>1.22</td>
<td>0.23</td>
</tr>
<tr>
<td>0.1C–5Mn</td>
<td>0.10</td>
<td>4.74</td>
<td>–</td>
</tr>
<tr>
<td>0.15C–5Mn</td>
<td>0.15</td>
<td>4.73</td>
<td>–</td>
</tr>
<tr>
<td>0.01C–3Mn</td>
<td>0.01</td>
<td>2.92</td>
<td>0.01</td>
</tr>
<tr>
<td>0.09C</td>
<td>0.09</td>
<td>1.90</td>
<td>0.15</td>
</tr>
<tr>
<td>0.15C</td>
<td>0.15</td>
<td>1.90</td>
<td>0.22</td>
</tr>
<tr>
<td>0.22C</td>
<td>0.22</td>
<td>1.18</td>
<td>0.27</td>
</tr>
</tbody>
</table>

“–” means less than 0.01 wt.% for Si and Cr and less than 0.001 wt.% for Ti.

Table 2. Measured mechanical properties of studied steels: yield strength (YS₀.₂), ultimate tensile strength (UTS), uniform (Uel) and total (TE) elongation, respectively.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>YS₀.₂ [MPa]</th>
<th>UTS [MPa]</th>
<th>Uel [%]</th>
<th>TE [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.3C</td>
<td>1333</td>
<td>1875</td>
<td>3.3</td>
<td>4.6</td>
</tr>
<tr>
<td>0.36C</td>
<td>1439</td>
<td>2150</td>
<td>4.0</td>
<td>6.3</td>
</tr>
<tr>
<td>0.1C–5Mn</td>
<td>1049</td>
<td>1387</td>
<td>3.0</td>
<td>5.2</td>
</tr>
<tr>
<td>0.15C–5Mn</td>
<td>1258</td>
<td>1663</td>
<td>3.7</td>
<td>3.7</td>
</tr>
</tbody>
</table>
retained austenite. The X-ray spectra (Figs. 1(c) and 1(d)) demonstrate only ferritic peaks: (220)\(_{\alpha}\), (211)\(_{\alpha}\) and (200)\(_{\alpha}\). Hence it is concluded that the structure is fully martensitic.

3. Results and Discussion

Figure 2 presents the results of experimental tensile tests performed in the present study along with the results collected from the previous works.\(^{8,12,13}\) The true stress evolution as a function of true strain is shown in Fig. 2(a), meanwhile Fig. 2(b) shows the related strain hardening rate evolution as a function of true stress (so-called Kocks-Mecking plot\(^{14,15}\)). For all studied martensitic steels some general highlights can be stated:

- Conventional yield stress seems to be a function of martensite carbon and manganese contents.
- High work-hardening rate is observed and it increases up to necking strain in accordance with the carbon and manganese contents.

From Fig. 2(a) it can be seen that the true stress-true strain curve of 0.1C–5Mn is almost the same as for 0.15C, and that the true stress-true strain curve of 0.15C–5Mn is in between the curves of 0.22C and 0.3C. The same conclusion can be deduced from Fig. 2(b) which demonstrates the strain hardening evolution. The solid solution hardening of Mn cannot explain this difference in the behavior of martensitic steels with high Mn content. Modification of solid solution hardening only shifts the curves to higher stress levels, but in the case of medium Mn steels a clear change in strain hardening of martensite can be found. According to F.B. Pickering and T. Gladman\(^{16}\) the solid solution hardening of Mn can be evaluated using following relation: \(S_{\text{Mn}}^* = \text{Mn wt.\%}, \) where \(S_{\text{Mn}} = 32\). This means that each percent of Mn increases strength on 32 MPa and for 4.7 wt.% of Mn the strength should increase on about 150 MPa. Figure 2(c) shows the experimental curves of 0.15C and 0.15C–5Mn, but also 0.15C curve shifted up at 150 MPa. This figure proves that such shift is not sufficient to match with 0.15C–5Mn; there are still about 125 MPa missing. But also the strain hardening rate, which is depicted in Fig. 2(b) is not the same. Thus it is considered that simple solid solution hardening cannot explain the behavior of martensite with medium content of Mn. It can be also observed from the Figs. 2(a) and 2(b) that the influence of Mn on stress and on strain hardening in the case of small carbon content (0.01C–3Mn) is rather limited.

All these facts suggest that Mn content influences the martensite strength and strain hardening in obvious synergy with the carbon content of martensite.

Based on the CCA approach,\(^{8}\) a simplified behavior law for martensitic steels is proposed. In order to describe the stress-strain curve of martensite as a large elasto-plastic transition the strain hardening can be expressed as the prod-

![Fig. 2](image-url)
uct of Young modulus \((E)\) by the fraction of elastic zones \((1 - F)\):

\[
\frac{d\sigma}{d\varepsilon} = (1 - F) \cdot E \quad \ldots \ldots (1)
\]

where \(\sigma\) and \(\varepsilon\) are respectively the macroscopic stress and strain of the material.

The plasticized zones fraction \(F\) is chosen as a logistic law:

\[
F = 1 - \exp \left( -\left( \frac{\sigma - \sigma_{\min}}{\sigma_0} \right)^p \right) \quad \ldots \ldots (2)
\]

where \(\sigma_{\min}\) is the minimum stress necessary to start to plasticize and, \(p\) and \(\sigma_0\) are the parameters that control the shape of \(F(\sigma)\) curve (Fig. 3(a)). In the first stage of tensile test, the macroscopic stress is lower than the elastic threshold \((\sigma<\sigma_{\min})\), hence \(F = 0\) and the material exhibits completely elastic behavior. When the applied stress \((\sigma)\) became more important than \(\sigma_{\min}\), then \(F\) starts to increase, meaning that the plasticized zones fraction increases.

Model adjustment with the experimental and literature data shows that \(\sigma_{\min}\) and \(p\) can be taken as constants for all considered steels, and the following values are found to be optimal: \(\sigma_{\min} = 450\) MPa and \(p = 2.5\). Thus, only one variable parameter, \(\sigma_0\), is used to obtain the best fitting results between model and experiments. It is found that both \(C\) and \(Mn\) have an important influence on \(\sigma_0\). A linear dependence between \(\sigma_0\) and \(C_{eq}\) is established in the form of subsequent equation:

\[
\sigma_0 = 130 + 1997 \cdot C_{eq} \quad \ldots \ldots (3)
\]

where \(C_{eq}\) is the parameter that considers the concomitant influence of \(C\) and \(Mn\). It is proposed to take into account this synergy of \(C\) and \(Mn\) in the following way:

\[
C_{eq} = C \left( 1 + \frac{Mn}{K_{Mn}} \right) \quad \ldots \ldots (4)
\]

where \(C\) and \(Mn\) represent initial \(C\) and \(Mn\) (wt.%) contents, and \(K_{Mn}\) is the coefficient of the \(Mn\) influence. Finally, from the collected experimental data (Tables 1, 2 and Fig. 2) it is possible to find the optimum value for \(K_{Mn} = 3.5\).

The \(\sigma_0\) evolution with \(C_{eq}\) is shown in Fig. 3(b): experimentally adjusted points are compared to the ones predicted with Eq. (3).

The final results of the model are presented and compared to the experimental data in Fig. 4. The results of stress-strain curves prediction are separated into two graphs (Figs. 4(a) and 4(b)) to have a better vision of medium \(Mn\) steels curves. As it can be seen, this simple model accurately predicts the whole stress-strain curves of different martensitic steels with varied \(C\) and \(Mn\) contents. On the other hand, it can be noticed that the simulated curves are not perfect and there are some mismatches. However, the maximum difference between model and experimental curves in terms of stress is less than 60 MPa and this represent less than 5% of the maximum flow stress.

Figures 4(c) and 4(d) present the evolution of strain hardening rate as a function of stress and as a function of strain, respectively. Taking into account that modeling of derivative is more complex than modeling of a function itself; the proposed model gives very satisfactory results of strain hardening rate evolution. These figures also shows that the model accounts well the synergy influence of \(C\) and \(Mn\) on the strain hardening rate evolution.

Even though the results are satisfactory, it is evident that the proposed model is a simplified version of CCA published previously, hence the global description of stress-strain curves is less precise, especially elasto-plastic transition. This can be clearly seen on the stress-strain curves of 0.22C, 0.15C and in particular 0.01C–3Mn steels. The discrepancy of the model is also related to the fact that only one fitting parameter is considered. This is done deliberately in order to simplify the understanding of the observed phenomenon of \(C\)–\(Mn\) synergy. Model response can be easily improved by relaxing the constraints on \(\sigma_{\min}\) making it variable and not constant. Nevertheless, to obtain good correlation between \(\sigma_{\min}\) and some metallurgical or microstructural parameters more data and studies are needed.

Future works are also necessary to understand physical mechanism of this \(C\)–\(Mn\) synergy and its relation with the microstructure. The outputs of these further investigations will be probably very helpful for further model improvement.
4. Conclusions

Mechanical behavior of martensite was studied using literature and new experimental data obtained on two medium carbon and two medium manganese steels. It was found that manganese increases strength and strain hardening of martensite in synergy with its carbon content. This synergy between carbon and manganese was taken into account in a specific way and the coefficient of the manganese influence was adjusted. More pragmatic model to describe mechanical response of martensitic steels was proposed based on Continuous Composite Approach developed previously. The results of adjusted model with only one fitting parameter showed very satisfactory agreement with the experimental data.

As the understanding of physical mechanism explaining the reported synergy between manganese and carbon on the behavior of martensite is not available, future investigations are planned in order to link the macroscopic martensite behavior and the related microstructure in presence of carbon and manganese.

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