Melting Separation Process of High Chromium Vanadium-bearing Titanomagnetite Metallized Pellet and its Optimization by Multi-Index Synthetic Weighted Scoring Method

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Based on the gas-based direct reduction followed by melting separation process, the melting separation process of high chromium vanadium-bearing titanomagnetite metallized pellet and its optimization by multi-index synthetic weighted scoring method are studied in the present work. The optimal melting separation parameters include a melting temperature of 1,650°C, a melting time of 45 min, and a basicity of 1.10. Under these conditions, the recoveries of Fe, V, Cr, and TiO₂ reach 99.87%, 98.26%, 95.32%, and 95.04% respectively; the mass fraction of Fe, V, Cr, and TiO₂ are 94.16%, 0.94%, 0.76%, and 38.21% respectively. The basicity has the strongest effect and its effect on the melting separation kinetic is more significant than thermodynamic. As increased basicity from 0.6 to 1.1, the slag viscosity decreases and surface tension increases, which are both attributed to smooth melting separation and improved indexes.

At present, VT is smelt in blast furnace (BF) but the recovery rate of Fe, V, and TiO₂ is only reach 70%, 39%, and 13% respectively. Recently, the technology of direct reduction followed by melting separation applying to disperse special metallurgical resources has attracted increasing attention. Based on the gas-based direct reduction followed by melting separation applying to disperse special metallurgical resources has attracted increasing attention. Based on the gas-based direct reduction followed by melting separation, the multi-index synthetic weighted scoring method is one of scientific evaluation methods used to optimize parameters for multi-index system. It contains three parts: (1) the weight of each factor is determined by its importance and subjective cognition (experience) on the factor importance; (2) the multi-index results is changed to a final single result that is synthetic scoring value; (3) the synthetic scoring value is analyzed by the normal single index analysis method. Here, the weight of each factor is a key point. To ensure a true and effective result, both the subjective cognition (experience) on the factor importance by tester and the objective information from test results are considered in this method. Finally the optimization model of synthetic scoring value is established based on the optimization theory, and its exact solution is given. So the

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1. Introduction

Vanadium-bearing titanomagnetite (VT) is a polymetallic intergrowth iron ore that owns a wide distribution throughout the world such as Russia, China, North Africa, and America etc. In VT, there are various valuable elements including iron, titanium, vanadium, and chromium which are typical strategic resources due to its extensive application in metallurgy, chemical industry, and aerospace etc. Based on the mass fraction of Cr₂O₃, VT is classified into two categories: ordinary VT and high chromium vanadium-bearing titanomagnetite (HCVT), and HCVT has a higher comprehensive utilization value. At present, VT is smelt in blast furnace (BF) but the recovery rate of Fe, V, TiO₂ is only reach 70%, 39%, and 13% respectively. Recently, the technology of direct reduction followed by melting separation applying to disperse special metallurgical resources has attracted increasing attention. Jun et al.'s study of carbothermal reduction-melting separation process for copper slag. In Guang et al.'s study, both the boron-bearing nugget and boron-rich slag were obtained from ludwigite through carbon bearing pellet reduction-melting technology. No matter BF process and present coal based direct reduction-melting separation process, it should be noted that the reduction by carbon is relatively slow and consumes large amounts of energy. But the gas-based reduction seems to be a novel and effective method to process VT due to its rapid reduction and clean production.

The multi-index synthetic weighted scoring method is one of scientific evaluation methods used to optimize parameters for multi-index system. It contains three parts: (1) the weight of each factor is determined by its importance for the whole test; (2) the multi-index results is changed to a final single result that is synthetic scoring value; (3) the synthetic scoring value is analyzed by the normal single index analysis method. Here, the weight of each factor is a key point. To ensure a true and effective result, both the subjective cognition (experience) on the factor importance by tester and the objective information from test results are considered in this method. Finally the optimization model of synthetic scoring value is established based on the optimization theory, and its exact solution is given. So the
analyses are reasonable and credible, and it has been widely applied in lots of fields such as agriculture, pharmacy, and manufacturing industry.\textsuperscript{18,19)}

Due to the previously discussed low recovery rate, high energy consumption, and slag pollution by solid reductant during BF or coal-based direct process, a new gas based reduction-melting process for HCVT has been proposed and researched by authors’ team.\textsuperscript{2,20,21)} From the previous work by author,\textsuperscript{21)} it has been proved that the iron containing V and Cr together with the slag bearing Ti can be obtained by the new process. Also, the effect rules of key parameters on high chromium vanadium-bearing titanomagnetite metalized pellet (HCVTMP) melting separation are investigated by the single index test. However, for a multi-index evaluation system, the optimal parameters obtained from single index test are not enough and imprecise, the scientific test should be designed and carried out. Subsequently, the proper and credible data analysis method is also distinctly necessary. In addition, till now there is no clear description on the detailed HCVTMP melting separation process, such as the behaviors on the aggregation, growth, and separation of reduced metals. Therefore in this work, firstly the orthogonal test is conducted and the key HCVTMP melting separation parameters are optimized by multi-index synthetic weighted scoring method. And then the detailed process of HCVTMP melting separation is discussed with the help of \textit{in-situ} confocal laser-scanning microscope (CLSM) observation.

2. Experimental

The HCVTMP with a metallization rate of about 95\% obtained from gas-based furnace direct reduction is applied in the work and the chemical composition analyzed by ICP-OES is listed in Table 1. The amount of HCVTMP sample is 100 g. The analytically pure activated carbon, CaO, and CaF\textsubscript{2} with the particle size less than 0.074 mm are used in the work. The C/O is defined as the mole ratio of carbon to reducible oxygen in iron, vanadium, chromium, and titanium oxides. According to the early work by author,\textsuperscript{21)} the amount of carbon in the work is based on C/O of 1.20 for sufficient deep reduction and carburization. The basicity defined as CaO/SiO\textsubscript{2} is the mass fraction ratio of CaO to SiO\textsubscript{2} in raw material. Through adjusting the mass of CaO, a series of basicity in designed tests is obtained. The basicity of 1.10 as an example, if the basicity is adjusted to 1.10, the mass of addition CaO is 3.08 g (0.34 of 1.10 as an example, if the basicity is adjusted to 1.10, the basicity in designed tests is obtained. Taking the basicity of 1.10 as an example, if the basicity is adjusted to 1.10, the mass of addition CaO is 3.08 g ((0.34+\times)/3.11 = 1.10, \(x=3.08\) g). And considering the slag with good fluidity and the erosion to brusque by early work based on people, the addition of CaF\textsubscript{2} in the work is 2\% (100 g HCVTMP, 2 g CaF\textsubscript{2}).

The melting separation of HCVTMP is carried out in a medium frequency induction furnace (XZ-40B), and the sketch map is shown as Fig. 1. The temperature is measured by an infrared thermometer (DT-8869b) with a measure range of \(-50\text{ to } 200\)\textdegree C and an accuracy of 0.1\textdegree C. The HCVTMP is crushed to below 1 mm. Then the materials including powder samples, activated carbon, CaO, and CaF\textsubscript{2} are weighted, mixed homogeneously, and loaded in a high pure graphite crucible. Next, the crucible is placed in the effective temperature section of furnace and heated at high temperatures to realize the iron and slag separation. Argon atmosphere is keeping throughout the process. After melting separation, the furnace is shut down and the sample is rapidly cooled down in argon atmosphere. To ensure the significance of result, each test is checked for three times and the mean is taken as the final result.

The samples are analyzed by ICP-OES, SEM-EDS, and Factsage 7.0. In all calculations by Factsage, the system pressure is \(1.01\times 10^5\text{ Pa}\), and the atmosphere is in Ar. And the equilibrium calculations are assumptive to explain the reactions and behaviors occurring during the experiment (non-equilibrium). The recovery rates of elements are calculated according to the mass balance and defined as:

\[ R_{TiO_2} = \frac{W_2 \times M_{i}}{W_{i} \times M_P} \times 100\% \quad \quad \quad \quad \quad \quad \quad \quad \quad (1) \]

Where, \(R_{TiO_2}\) is the recovery rate of TiO\textsubscript{2} in slag, \%, \(W_1\) and \(W_2\) is the mass fraction of TiO\textsubscript{2} in HCVTMP and slag respectively, \%, \(M_P\) and \(M_s\) is the mass of HCVTMP and slag respectively, g.

\[ R_i = \frac{W_i \times M_{i}}{W_s \times M_P} \times 100\% \quad \quad \quad \quad \quad \quad \quad \quad \quad (2) \]

Where, \(R_i\) is the recovery rates of elements (Fe, V and Cr) in iron, \%, \(W_3\) and \(W_4\) is the mass fraction of element in HCVTMP and iron respectively, \%. \(M_i\) is the mass of iron, g.

CLSM is help for \textit{in-situ} observation of HCVTMP melting separation behavior. A pressed pellet with the mixed material (crushed HCVTMP, C, CaO, and CaF\textsubscript{2}) is put in a platinum crucible and placed to the heating range just under the laser microscope. The inner chamber is sealed and purged with high purity Ar flow of 200 mL/min during observation. The sample is rapidly heated up to 1 050\textdegree C at the heating rate of 150\textdegree C/min, and then maintained for 30 s at 1 050\textdegree C. After stabilization, the sample is heated to 1 600\textdegree C with the heating rate of 24\textdegree C/min, and then maintained for 40 min at 1 600\textdegree C. After the test, the sample is

<p>| Table 1. Chemical composition of HCVTMP (wt%). |</p>
<table>
<thead>
<tr>
<th>TFe</th>
<th>MFe</th>
<th>V\textsubscript{2}O\textsubscript{5}</th>
<th>TiO\textsubscript{2}</th>
<th>Cr\textsubscript{2}O\textsubscript{3}</th>
<th>CaO</th>
<th>SiO\textsubscript{2}</th>
<th>MgO</th>
<th>Al\textsubscript{2}O\textsubscript{3}</th>
</tr>
</thead>
<tbody>
<tr>
<td>76.62</td>
<td>73.09</td>
<td>1.387</td>
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<td>0.947</td>
<td>0.34</td>
<td>3.16</td>
<td>1.55</td>
<td>4.28</td>
</tr>
</tbody>
</table>

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2
cooled down.

3. Results and Discussion

3.1. Orthogonal Test

From the previous single index test, the rough ranges of HCVTMP melting separation parameters are obtained: melting temperature (the set temperature of melting separation test) is around 1625°C, melting time (the holing time under the set melting temperature) is about 40–50 min, and basicity (CaO/SiO2) is approximately kept at 1.10. But for a multi-index evaluation system, the optimal parameters gotten from single index test are not enough and imprecise, the scientific test should be designed and carried out. So based on these results, the scheme of orthogonal test is detailed in Table 2. Three key process factors and three varying levels are used, including a melting temperature of 1600–1650°C, a melting time of 45–55 min, and a basicity from 1.0 to 1.2. In the test, the recovery rate of Fe, V, and Cr in iron ($R_{Fe}$, $RV$, $RCr$) together with the recovery rate of TiO2 in separation slag ($RTiO2$) is considered as the four evaluation indexes. The results including index data and morphologies of iron and separation slag are given in Table 2 and Fig. 2, respectively. The considered indexes show relatively good values, meanwhile, the surface of iron is smooth which indicates that the separation proceeds successfully. In other words, the optimization in the given range is reasonable and credible.

The orthogonal range analysis is listed in Table 3. The change rule of HCVTMP melting separation indexes under series factor level is described in Fig. 3. These results quantitatively indicate the significance of each key process factor.

![Fig. 2. Morphology of the separation iron and slag for each orthogonal test.](image)

![Fig. 3. Change rule of HCVTMP melting separation indexes under series factor level.](image)

### Table 2. Scheme and result of the orthogonal test.

<table>
<thead>
<tr>
<th>No</th>
<th>Factor Results</th>
<th>A/°C</th>
<th>B/min</th>
<th>C/−</th>
<th>$R_{Fe}/%$</th>
<th>$RV/%$</th>
<th>$RCr/%$</th>
<th>$RTiO2/%$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td>1600</td>
<td>45</td>
<td>1.0</td>
<td>99.58</td>
<td>95.13</td>
<td>89.71</td>
<td>91.61</td>
</tr>
<tr>
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<td></td>
<td>1600</td>
<td>50</td>
<td>1.1</td>
<td>99.14</td>
<td>94.82</td>
<td>87.8</td>
<td>95.91</td>
</tr>
<tr>
<td>3</td>
<td></td>
<td>1600</td>
<td>55</td>
<td>1.2</td>
<td>99.58</td>
<td>94.96</td>
<td>90.74</td>
<td>93.97</td>
</tr>
<tr>
<td>4</td>
<td></td>
<td>1625</td>
<td>45</td>
<td>1.1</td>
<td>99.96</td>
<td>96.37</td>
<td>92.50</td>
<td>94.74</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>1625</td>
<td>50</td>
<td>1.2</td>
<td>97.79</td>
<td>96.89</td>
<td>91.75</td>
<td>94.29</td>
</tr>
<tr>
<td>6</td>
<td></td>
<td>1625</td>
<td>55</td>
<td>1.0</td>
<td>98.83</td>
<td>93.16</td>
<td>87.84</td>
<td>95.55</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td>1650</td>
<td>45</td>
<td>1.2</td>
<td>99.86</td>
<td>96.27</td>
<td>90.46</td>
<td>91.89</td>
</tr>
<tr>
<td>8</td>
<td></td>
<td>1650</td>
<td>50</td>
<td>1.0</td>
<td>99.04</td>
<td>95.67</td>
<td>90.02</td>
<td>90.91</td>
</tr>
<tr>
<td>9</td>
<td></td>
<td>1650</td>
<td>55</td>
<td>1.1</td>
<td>98.28</td>
<td>97.22</td>
<td>94.38</td>
<td>93.65</td>
</tr>
</tbody>
</table>

Note: A-Melting temperature, B-Melting time, C-Basicity

### Table 3. Range analysis of orthogonal test.

<table>
<thead>
<tr>
<th>Index</th>
<th>$R_{Fe}/%$</th>
<th>$R_{RV}/%$</th>
<th>$R_{RCr}/%$</th>
<th>$R_{RTiO2}/%$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_1$</td>
<td>A 99.43</td>
<td>B 99.80</td>
<td>C 99.15</td>
<td>94.97</td>
</tr>
<tr>
<td>$k_2$</td>
<td>A 98.86</td>
<td>B 98.66</td>
<td>C 99.13</td>
<td>95.47</td>
</tr>
<tr>
<td>$k_3$</td>
<td>A 99.06</td>
<td>B 98.90</td>
<td>C 99.08</td>
<td>96.39</td>
</tr>
<tr>
<td>$R$</td>
<td>A 0.57</td>
<td>B 1.14</td>
<td>C 0.07</td>
<td>1.42</td>
</tr>
</tbody>
</table>

Significance $R_B>R_A>R_C$ $R_C>R_A>R_B$ $R_C>R_A>R_B$ $R_C>R_A>R_B$

Optimum A1 B1 C1 A2 B2 C2 A3 B3 C3 A4 B4 C4

Note: A-Melting temperature, B-Melting time, C-Basicity
on the HCVTMP melting separation indexes and the optimal conditions for different factors. The factor affecting $R_{Fe}$ in descending order of significance is melting time > melting temperature > basicity; the optimal condition for better $R_{Fe}$ is 1 600°C, 45 min, and basicity of 1.0. The order of each factor affecting $R_{Fe}$ is basicity > melting temperature > melting time; the optimal condition for higher $R_{Fe}$ is 1 650°C, 45 min, and basicity of 1.1. The order of each factor affecting $R_{Cr}$ is basicity > melting temperature > melting time; the optimal condition for higher $R_{Cr}$ is 1 650°C, 55 min, and basicity of 1.1.

3.2. Optimization of HCVTMP Melting Separation by Synthetic Weighted Scoring Method

The multi-index synthetic weighted scoring method is used to determine the optimal HCVTMP melting separation parameters. Considering the importance of subjective cognizance and making the most use of objective test results, the weight value of indexes should accomplish the unification of the subject and object, then the scoring is objective, true, and effective.

3.2.1. Determination of Standardized Evaluation Matrix

In a multi-index test, there are $n$ schemes marked as $I = \{1, 2, 3, \ldots, n\}$ and $m$ indexes marked as $J = \{1, 2, \ldots, m\}$. The corresponding experimental data are $x_{ij}$ ($i = 1, 2, 3, \ldots, n; j = 1, 2, 3, \ldots, m$) which make up an evaluation matrix marked as $X = (x_{ij})_{n \times m}$.

To unify the tendency requirement of each index and remove its incommensurability, the evaluation matrix should be standardized. Assuming $I_1 = \{\text{the indexes with “the lower, the better”}\}$, $I_2 = \{\text{the indexes with “the higher, the better”}\}$, $I_3 = \{\text{the indexes with a stable and desired value}\}$, $I_1 \cup I_2 \cup I_3 = I$. When the judgment standard of the weight scoring is “the lower, the better” or “the high, the better”, the different forms of $y_{ij}$ are given as Eqs. (3) and (4), respectively. Where, $x_{ij}^*(j \in I_3)$ is the desired value for index; $x_{jmax} = \max_{1 \leq i \leq n} \{x_{ij}\}$.

For unifying the index’s magnitude order and removing its dimension, the $z_{ij}$ value is commanded as Eq. (5). Where, $y_{min} = \min \{y_{ij}|i = 1, 2, 3, \ldots, n\}$; $y_{max} = \max \{y_{ij}|i = 1, 2, 3, \ldots, n\}$. $Z = (z_{ij})$ is the final standardized evaluation matrix.

$$y_{ij} = \begin{cases} x_{ij} & j \in I_1 \\ x_{jmax} - x_{ij} & j \in I_2 \\ x_{ij} - x_{jmin} & j \in I_3 \end{cases} \quad \text{.........(3)}$$

$$y_{ij} = \begin{cases} x_{jmin} - x_{ij} & j \in I_1 \\ -x_{ij} & j \in I_2 \\ -x_{jmin} & j \in I_3 \end{cases} \quad \text{.........(4)}$$

$$z_{ij} = 100 \times \frac{(y_{ij} - y_{min})}{(y_{max} - y_{min}),} \quad i = 1, 2, 3, \ldots, m; j = 1, 2, 3, \ldots, m \quad \text{.........(5)}$$

In the present HCVTMP melting separation process, the recovery rates of Fe, V, Cr, and TiO$_2$ are the four evaluation indexes which are all expected to be higher as much as possible. The evaluation matrix $X = (x_{ij})$ can be gained from experimental data listed in Table 2. According to the judgment standard that “the higher, the better” as Eq. (4), the final standardized evaluation matrix $Z(z_{ij})$ is obtained.

$$X = (x_{ij}) = \begin{bmatrix} 99.58 & 95.13 & 89.71 & 91.61 \\ 99.14 & 94.82 & 87.80 & 95.91 \\ 99.58 & 94.96 & 90.74 & 93.97 \\ 99.96 & 96.37 & 92.50 & 94.74 \\ 97.79 & 96.89 & 91.75 & 94.29 \\ 98.83 & 93.16 & 87.84 & 95.55 \\ 99.86 & 96.27 & 90.46 & 91.89 \\ 99.04 & 95.67 & 90.02 & 90.91 \\ 98.28 & 97.22 & 94.38 & 93.65 \end{bmatrix}$$

$$Z = (z_{ij}) = \begin{bmatrix} \frac{83.26}{82.49} & 48.52 & 29.03 & 14.00 \\ 62.21 & 40.89 & 0.00 & 100.00 \\ 82.49 & 44.33 & 44.68 & 61.20 \\ 100.00 & 79.06 & 71.43 & 76.60 \\ 0.00 & 91.87 & 60.03 & 67.60 \\ 47.93 & 0.00 & 0.61 & 92.80 \\ 95.39 & 76.60 & 40.43 & 19.60 \\ 57.60 & 61.82 & 33.74 & 0.00 \\ 22.58 & 100.00 & 100.00 & 54.80 \end{bmatrix}$$

3.2.2. Determination of Synthetic Weight of Each Index

The HCVTMP used in the work is imported from Russia, and it is a remnant after the iron ore beneficiation titanium. The content of TiO$_2$ is relatively low. On the premise of ensuring the relatively high recovery of Ti, the main aim for comprehensively utilizing this HCVTMP is to improve the recoveries of Fe, V, and Cr as much as possible. As a result, firstly based on the previous experience and requirement during the optimization of HCVTMP melting separation process, the expert investigating method is used to obtain the subjective weight for each index.$^{15,16}$ The subjective weight of Fe, V, Cr, and TiO$_2$ recovery rate in this work is $\alpha_1 = 0.3$, $\alpha_2 = 0.3$, $\alpha_3 = 0.3$, and $\alpha_4 = 0.1$, respectively. It means that the matrix of subjective weight is $\alpha = [0.3, 0.3, 0.3, 0.1]^T$.

Secondly, from the entropy evaluation method,$^{16,22}$

$$\beta = (1 - h_j) / \sum_{k=1}^n (1 - h_k) \quad (j = 1, 2, 3, \ldots, m; k \leq j),$$

where,

$$h_j = (\ln n)^{-1} \sum_{i=1}^m p_{ij} \ln p_{ij}, \quad \text{and} \quad p_{ij} = z_{ij} / \sum_{k=1}^m z_{ik}. \text{Notes, } p_{ij} \ln p_{ij} = 0 \quad (i = 1, 2, 3, \ldots, n; j = 1, 2, 3, \ldots, m) \text{ when } p_{ij} = 0. \text{ Then the objective weights are also given as } \beta = [0.31, 0.27, 0.24, 0.18]^T. $$

Finally, in order to achieve the unity of the subjective and objective, the optimization decision model is established as Eq. (6). Where, $\mu (0 \leq \mu \leq 1)$ is the inclination coefficient that reflects the preference degree for the subjective and objective weights. Here, $\mu = 0.5$. The final synthetic weight for each index is obtained as $w = [0.30, 0.28, 0.27, 0.14]^T$. 

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of slag and metal are listed in Table 6. The mass fraction of Fe, V, Cr, and TiO₂ reach 94.16%, 0.94%, 0.76%, and 38.21%, respectively. And the recovery of Fe, V, Cr, and TiO₂ is high to 99.87%, 98.26%, 95.32%, and 95.04%, respectively. Compared with the single index test results, all the recoveries and mass fraction are improved obviously. The cross section of separation slag and iron (rapidly cooled down in argon atmosphere) under the optimum are analyzed by SEM-EDS, shown in Fig. 4. In (a) and (c), the

3.2.3. Calculation of Synthetic Weighted Score

From the formula described as Eq. (7), the synthetic weighted score for each index is calculated as:

$$f = [w_1, w_2, \ldots, w_n] \cdot [x_1, x_2, \ldots, x_n]$$

3.2.4. Single Index Analysis Evaluation

Subsequently, the optimization of HCVTMP melting separation is investigated by the single index analysis evaluation and the results are listed in Table 4. Through the whole multi-index synthetic weighted scoring method, the optimal HCVTMP melting separation parameters are obtained as follows: a melting temperature of 1 650°C, a melting time of 45 min, and a basicity of 1.1. The basicity most strongly affects the HCVTMP melting separation, followed successively by the melting temperature and melting time. In addition, the effect of inclination coefficient (μ) on the optimization is also discussed in Table 5. All the significance order and optimum are the same under any inclination coefficient. The basicity still has the most significant effect on HCVTMP melting separation.

The HCVTMP melting separation is applied under the optimal conditions. The recovery amount and compositions

![Table 4](image)

<table>
<thead>
<tr>
<th>No.</th>
<th>Index Factor</th>
<th>$f$</th>
</tr>
</thead>
<tbody>
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<td>$A^{\circ}C$</td>
<td>$B/\text{min}$</td>
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<td>45</td>
</tr>
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<tr>
<td>9</td>
<td>1 650</td>
<td>55</td>
</tr>
</tbody>
</table>

K₁, 93.21 94.51 93.09 $w_1=0.30, w_2=0.28, w_3=0.27, w_4=0.14$

K₂, 94.53 93.98 94.95 Significance $C>A>B$

K₃, 94.91 94.15 94.61 Level $C_2, A_2, B_2$

R, 1.70 0.53 1.86 Optimum $A_2, B_2, C_2$

Table 5. Optimal parameters under different inclination coefficient μ.

<table>
<thead>
<tr>
<th>μ</th>
<th>$w_1$</th>
<th>$w_2$</th>
<th>$w_3$</th>
<th>$w_4$</th>
<th>Significance</th>
<th>Optimum</th>
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<tr>
<td>0.4</td>
<td>0.30</td>
<td>0.28</td>
<td>0.26</td>
<td>0.15</td>
<td>C&gt;A&gt;B</td>
<td>A₃B₂C₂</td>
</tr>
<tr>
<td>0.5</td>
<td>0.30</td>
<td>0.28</td>
<td>0.27</td>
<td>0.14</td>
<td>C&gt;A&gt;B</td>
<td>A₃B₂C₂</td>
</tr>
<tr>
<td>0.6</td>
<td>0.30</td>
<td>0.29</td>
<td>0.28</td>
<td>0.13</td>
<td>C&gt;A&gt;B</td>
<td>A₃B₂C₂</td>
</tr>
<tr>
<td>0.8</td>
<td>0.30</td>
<td>0.30</td>
<td>0.29</td>
<td>0.12</td>
<td>C&gt;A&gt;B</td>
<td>A₃B₂C₂</td>
</tr>
<tr>
<td>1.0</td>
<td>0.30</td>
<td>0.30</td>
<td>0.30</td>
<td>0.10</td>
<td>C&gt;A&gt;B</td>
<td>A₃B₂C₂</td>
</tr>
</tbody>
</table>

Note: A-Melting temperature, B-Melting time, C-Basicity

Table 6. Recovery amount and compositions of slag and metal under the optimal conditions.

<table>
<thead>
<tr>
<th>$M_t/g$</th>
<th>$C_{%&lt;/}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>81.26</td>
<td>94.16 94.04 94.30 94.30 94.04</td>
</tr>
<tr>
<td>23.05</td>
<td>38.21 21.19 13.44 6.72 18.55</td>
</tr>
</tbody>
</table>

Note: $M_t, M_s, M_p$-Mass of HCVTMP, Iron, Slag; $C_{</%}$-Composition of iron, slag

![Fig. 4](image)
two phases that the light gray (Point A) has more calcium while the dark gray (Point B) contains more titanium. Seen from (b) and (d), there are also two phases in iron, the bright white of pure metallic iron (Point C) and the gray white of metallic iron containing V and Cr (Point D).

3.3. Function Mechanism of Basicity on the HCVTMP Melting Separation

From the optimization by multi-index synthetic weighted scoring method, it is evident that basicity is really the most significant factor that affects HCVTMP melting separation, it is quite necessary to further confirm its function mechanism. Therefore the detailed single index tests are supplemented and shown in Fig. 5. When holding the HCVTMP original basicity of 0.13, the melting can’t be achieved at all. Slightly increasing basicity to 0.60, the relatively big iron is gathered at the bottom of crucible, but the separation is still not done successfully. So the data under the two basicity are inaccurate and not given. Further increasing basicity continuously, all the indexes show the tendency of first increase and then decrease, and have the highest value at the basicity of 1.10.

Effect of basicity on the thermodynamic equilibrium of HCVTMP melting is evaluated by the Equilib module in FACTSAGE 7.0 package. The databases including FactPS, FToxid, FTstel, and Fe₂VO₄ 23) (established by author) are applied. The system pressure is 1.01 × 10⁵ Pa, and the initial atmosphere is in Ar. The possible products are considered: liquid metal, metal carbide, metal oxide, liquid carbon, solid carbon, spinel, anosovite, monoxide, clinopyroxene, wollastonite, anorthite, cordierite, mullite, cordum, pseudobrookite, ulvaespinel, rutile, and perovskite etc. 100 g HCVTMP samples with C, CaO, and CaF₂ are analyzed with the temperature range of 1 000–1 700°C and the basicity range of 0.13–1.20. The possible liquid products including Fe (l), V (l), Cr (l), and Ti (l) are emphasized in Fig. 6. As increased basicity, the amount of Ti (l) has a slight decrease which is good for titanium oxide enrichment in slag. Beyond that, the major liquids of Fe (l), V (Cr), and V (l) are almost the same despite of the obvious increase of basicity. However, the result from experiment (Fig. 5) shows that all the indexes are sensitive to basicity. It is speculated that the influences of basicity on melting separation kinetic are greater than thermodynamic.

Viscosity of the slag formed in HCVTMP melting separation with different basicity is calculated by Viscosity module in FACTSAGE 7.0 package. The Melts database is applied. The evaluated temperature range is 1 350–1 700°C. The viscosity calculation results are described in Fig. 7. It’s obvious that the viscosity decreases gradually as increased basicity. Generally, the slag with a low viscosity is of great benefit to good diffusion and mass transfer due to its good fluidity. So by rising basicity, the melting separation kinetic is enhanced due to the decreasing slag viscosity, the successful separation of iron and slag is promoted.

Besides viscosity, the surface tension of slag is another key point in melting separation process for controlling various surface and interfacial phenomena. The bigger surface tension of molten slag will lead to the decreasing adhesion work between iron and slag which makes the slag difficult to
be brought to iron, and then the separation of iron and slag is improved. Therefore, the effect of basicity on HCVTMP melting separation is considered from the aspect of slag surface tension. According to the prediction model derived by Tanaka et al. and the research on the surface tension of molten blast furnace slag bearing TiO₂, the surface tension of HCVTMP melting separation slag (CaO–SiO₂–MgO–Al₂O₃–TiO₂–CaF₂) is evaluated based on the Butler’s equation. The surface tension is calculated by Eqs. (8)–(10).

\[ \sigma = \sigma_{\text{Pure}} + \frac{RT}{A_i} \ln \frac{M_i^{\text{Surf}}}{M_i^{\text{Bulk}}} \] ..............................(8)

\[ A_i = N_0^{1/13} \cdot V_i^{2/13} \] ........................................(9)

\[ M_i^{p} = \frac{N_i^{p}}{\sum_i \frac{R_i^{\text{cation}}}{R_i^{\text{Anion}}} \cdot N_i^{p}} \] ........................................(10)

Where, \( \sigma \) is the surface tension of molten slag, mN/m; \( i \) refers to the following components: CaO, SiO₂, MgO, Al₂O₃, TiO₂, CaF₂; \( \sigma_{\text{Pure}} \) is the surface tension of pure molten component \( i \), mN/m; \( R \) is the gas constant, \( - \); \( T \) is the absolute temperature, K; \( A_i \) is the molar volume of pure molten component \( i \), m³/mol; \( N_0 \) is Avogadro number; \( - \); \( V_i \) is the molar volume of pure molten component \( i \), m³/mol; \( R_i^{\text{cation}} \) and \( R_i^{\text{Anion}} \) is the radium of cation and anion respectively, m; \( N_i^{p} \) is the mole fraction of component \( i \) in phase \( P \); \( - \); \( P \) is Surf (surface) or Bulk (bulk). In addition, SO₄²⁻ is thought to be the minimum anionic unit in SiO₂ and the ratio of \( R_{\text{Si}^{4+}} \) to \( R_{\text{so}^{4-}} \) is 0.5³,²⁷,²⁸

The data including the ionic radii together with the temperature dependences of molar volume and surface tension for pure component used in the present evaluation are obtained from previous works²⁶–³¹ and listed in Tables 6 and 7. The calculated surface tension with different basicity at 1 650°C is given in Table 8. Meanwhile, the detection test is carried out by using RTW-10 melt physical property comprehensive testing instrument (deigned by Northeastern University, CHINA), and the data is also added into Fig. 8. The calculated values based on the present model are in good agreement with the experimental. As basicity increased, the surface tension goes up resulting in decreasing adhesion work between iron and slag, then the separation of iron and slag is enhanced and all the indexes are improved.

The metal-separation temperature usually depends on the slag melting temperature. The effects of basicity on slag initial melting temperature and slag melting temperature are evaluated by Equilib module in FACTSAGE 7.0 package and presented in Fig. 9. The evaluated basicity range is 0.13–1.20. When calculating the slag initial melting temperature, the FToxid-Slag A is set as “F” (Formation target phase). And the FToxid-Slag A is set as “P” (Precipitate target phase) if calculating slag melting temperature. The other calculation conditions are the same to the conditions of Fig. 6. When the basicity rising from the original (0.13) to 0.60, it is obvious that the initial melting temperature has a slight decrease but the slag melting temperature dramatically decreases from 1 536°C to 1 353°C accordingly. That is a pivotal reason why the HCVTMP melting separation can’t be achieved successfully with the basicity below 0.6. Further increasing basicity, the slag initial melting tem-

![Fig. 8. Effect of basicity on the 6-component slag surface tension.](image)

| Table 8. Temperature dependences of surface tension and molar volume of pure oxide. |
|-----------------|-----------------|-----------------|
| Oxide          | Surface tension (mN/m) | Molar volume (m³/mol) |
| CaO            | 791±0.0935 T     | 20.7±[1±10⁻⁴(T−1 773)]10⁻⁶  |
| SiO₂           | 243.2±0.031 T    | 27.516±[1±10⁻⁴(T−1 773)]10⁻⁶  |
| MgO            | 1 770±0.636 T    | 16.1±[1±10⁻⁴(T−1 773)]10⁻⁶  |
| Al₂O₃          | 1 024±0.177 T    | 28.3±[1±10⁻⁴(T−1 773)]10⁻⁶  |
| TiO₂           | 1 384±0.6254 T   | 22.2±[1±4.689·10⁻³(T−1 023)]10⁻⁶  |
| CaF₂           | 1 604±0.72 T     | 31.3±[1±10⁻⁴(T−1 773)]10⁻⁶  |

![Fig. 9. Effect of basicity on initial melting separation temperature and melting temperature of the slag.](image)
perature has no obvious changes. Instead, the slag melting temperature shows an increasing tendency which will bring some disadvantages to the separation of iron and slag.

To better understand the effect of basicity on HCVTMP melting separation behavior, the phase fraction changes of the slag with different basicity as a function of temperature are calculated by Equilib module in FACTSAGE 7.0 package and shown in Fig. 10. 100 g HCVTMP samples with C, CaO, and CaF$_2$ are analyzed with the temperature range of 1 100–1 600°C and the basicity range of 0.13–1.20. The other calculation conditions are the same to the conditions of Fig. 6. When the basicity is 0.13 (Fig. 10(a)), TiO$_2$ is observed to be in the forms of less anosovite MgTi$_2$O$_5$ (1) and more TiO$_2$ (2); CaO is primitively combined with SiO$_2$ and Al$_2$O$_3$ to generate anorthite CaAl$_2$Si$_2$O$_8$ (3); Mg is mainly dissolved in cordierite Mg$_2$Al$_4$Si$_5$O$_18$ (4) and sapphire Mg$_4$Al$_10$Si$_2$O$_23$ (5); and a large amount of liquid phase slag (7) suddenly forms at around 1 400°C. Increasing basicity to 0.60 (Fig. 10(b)), part of CaO is still in CaAl$_2$Si$_2$O$_8$, but the excessive CaO is combined with TiO$_2$ and the perovskite CaTiO$_3$ (8) with a high point of 1 960°C appears; Mg is mainly combined with about half of TiO$_2$ to form MgTi$_2$O$_5$ and the new phase of MgTi$_2$O$_4$ is also observed; meanwhile, the temperature that much liquid phase will generate decreases substantially. Further rising the basicity (Figs. 10(c)–10(f)), the temperature generating much liquid slag has no obvious changes, but the amount of CaTiO$_3$ increases evidently resulting in the increasing of slag melting temperature that has been shown in Fig. 9. Directly, the smooth HCVTMP melting separation is hindered by excessive basicity and all the indexes decrease more or less.

For improving the HCVTMP melting separation indexes, the controlling of slag amount is another key step. The proper more liquid slag amount can supply a relatively good environment for iron-slag melting separation.9) But the excessive amount slag can prevent the agglomeration of iron. Then the melting separation can’t proceed perfectly. The un-agglomerate iron particle with little size may be wrapped by slag, which will decrease the recovery of Fe, V, and Cr in iron.32) As seen from the slag amount under different basicity in Fig. 11 (calculated by Equilib module in FACTSAGE 7.0 and the calculation conditions are the same to the conditions of Fig. 6), all the indexes decrease when the basicity is further more than 1.10. Therefore, from the aspect of slag amount, HCVTMP melting separation is enhanced by rising basicity should be applied in a proper range.

According to the above analyses, increasing basicity within a certain basicity range is attributed to decreasing viscosity, increasing surface tension, decreasing slag melting point, and improving melting separation kinetic. But the excessive basicity will result in rising slag melting temperature instead and generating a large amount of slag, which are bad for improving melting separation indexes. As a result, the proper basicity for HCVTMP melting separation should be maintained at a compromised value, and for the experimental conditions, the compromised value is around 1.10.

### 3.4. Process of HCVTMP Melting Separation

The observed HCVTMP melting separation behaviors with the basicity of 1.10 are seen in Fig. 12. The camera lens is focused on the slide. They show (a) Fe–C melt formation and Fe(l) generation for carburization, (b) slag melting initiation and slag(l) generation, (c) start of iron-slag separation (starting of aggregation of small iron droplets or slag droplets), (d) continuous aggregation and growth of iron or slag and then accomplishment of iron-slag separation (relatively big size iron droplets formation).

In order to observe the detailed behaviors of iron aggregation and growth, the camera lens is focused on the sample, and the observation results are given as Fig. 13. Firstly, in Fig. 13(a), it is spontaneous crystal nucleus formation of iron droplet at a certain point of low potential barrier, the carburization is relatively slow in this stage, with the increasing temperature, the carburization is accelerated and the amount of slag also increases; then the period for iron crystal nucleus formation is shortened and the spontaneous nucleation rate is enhanced. Secondly, in Figs. 13(b) and 13(c), it is reaction interface formation and enlarge-
formation, reaction interface formation and enlargement, and following reaction interface decrease and iron aggregation. Additionally, the ratio of $\sigma_{\text{metal-slag}}$ (interfacial tension between metal and slag) to $\eta_{\text{slag}}$ (slag viscosity) also has significant effects on the separation of iron and slag. If $\sigma_{\text{metal-slag}}/\eta_{\text{slag}}$ is large, the separation is accomplished smoothly.

At last, the several noticeable points during HCVTMP melting separation are illustrated in Fig. 14. The carburization phenomena is given in Fig. 14(1), there are about three possibilities for iron carburization during HCVTMP melting separation, including direct carburization, gas carburization, and molten slag carburization (during melting). As the carburization reaction, the melting point of reduced iron decreases, and the diffusion together with agglomeration is accelerated, therefore, the carburization is the prerequisite for HCVTMP melting separation. In addition, the molten slag also plays an important role in HCVTMP melting separation. Kim et al. have pointed that the molten slag has a good wetting with iron but bad wetting with carbon. This good wetting and slag spreading will introduce an attractive force between iron and slag so as to make them come into contact with each other. With the developing of carburization, the liquid iron will form between solid iron and carbon and its amount increases with time. These processes when molten slag carburization during melting are clearly illustrated in Fig. 14(2): (a) solid iron and carbon will come to close after molten slag formation, (b) and they contact with each other by the attractive force from good wetting between iron and molten slag, (c) then the liquid iron generates for carburization, (d) finally the contacting area between liquid iron and carbon is enlarged and the amount of liquid iron increases. Combining with the CLSM observation, the iron aggregation and growth process is simply described as Fig. 14(3), it contains (a) iron crystal nucleus formation, (b) reaction interface formation and enlargement, (c) and (d) reaction interface decrease together with iron droplets aggregation and growth.

After iron droplets of big size formation, the iron droplets sedimentate to the bottom but the slag rise to the surface for different density and surface tension, and then the separation of iron and slag is achieved naturally. It is worth noting that the reduction of the oxides bearing iron, vanadium, chromium, and titanium in HCVTMP is run through the whole deep reduction melting separation process, but the restrictive step of reduction is different during each stage.

4. Conclusions

(1) The optimal HCVTMP melting separation parameters are obtained by multi-index synthetic weighted scoring method and included a melting temperature of 1650°C, a melting time of 45 min, and a basicity of 1.10. Under these conditions, the recoveries of Fe, V, Cr, and TiO₂ reach 99.87%, 98.26%, 95.32%, and 95.04% respectively; the mass fraction of Fe, V, Cr, and TiO₂ are 94.16%, 0.94%, 0.76%, and 38.21% respectively. The basicity most strongly affects the HCVTMP melting separation, followed successively by the melting temperature and melting time. And the optimization is credible and valid.

(2) The effect of basicity on the HCVTMP melting separation based on the existed iron crystal nucleus, and the carburization is accelerated continuously. Thirdly, in Figs. 13(d)–13(f), it is reaction interface decrease, the reaction interfaces that formation from each crystal nucleus are assembled together, the reaction interface will decrease after the maximum generation, then iron droplets are combined and grown, the particle size of iron is becoming larger and the interfacial tension between iron and slag is bigger, and then the separation of iron and slag will be achieved.

During the HCVTMP melting separation, the excellent slag properties including less viscosity, good fluidity, and bigger surface tension are conductive to iron crystal nucleus
separation kinetic is more considerable than thermodynamic. As increased basicity from 0.6 to 1.1, slag viscosity decreases, surface tension increases, and melting temperature decreases, which are all attributed to smooth melting separation and improved indexes. But further increasing basicity to 1.2, the amount of CaTiO$_3$ increases and slag melting point rises instead, meanwhile, the amount of slag is relatively excessive, then all the HCVTMP melting separation indexes show a decrease tendency.

(3) HCVTMP melting separation process contains four key behaviors: Fe–C melt formation and Fe(l) generation, slag melting initiation and slag(l) generation, start of iron-slag separation, and continuous aggregation and growth of iron or slag and then accomplishment of iron slag melting initiation and slag(l) generation, start of iron-slag separation and improved indexes. But further increasing basicity to 1.2, slag viscosity decreases, surface tension increases, and melting temperature decreases, which are all attributed to smooth melting separation kinetic is more considerable than thermodynamic. As increased basicity from 0.6 to 1.1, slag viscosity decreases, surface tension increases, and melting temperature decreases, which are all attributed to smooth melting separation and improved indexes. But further increasing basicity to 1.2, the amount of CaTiO$_3$ increases and slag melting point rises instead, meanwhile, the amount of slag is relatively excessive, then all the HCVTMP melting separation indexes show a decrease tendency.

(3) HCVTMP melting separation process contains four key behaviors: Fe–C melt formation and Fe(l) generation, slag melting initiation and slag(l) generation, start of iron-slag separation, and continuous aggregation and growth of iron or slag and then accomplishment of iron-slag separation. As for iron aggregation and growth, it should go through iron crystal nucleus formation, reaction interface formation and enlargement, and following reaction interface decrease.

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