Micro Optical Viscosity Sensor for *in situ* Measurement Based on a Laser-Induced Capillary Wave*

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Abstract

In this article, we demonstrate a novel micro optical viscosity sensor (MOVS) based on a laser-induced capillary wave with a focus control system that enables *in situ* monitoring of viscosity and surface tension changes in microliter-order liquid samples such as body fluids, polymer coating materials, lubricants, heavy oils and so on. The microfabricated sensor consists of two deep trenches (depth of 273 µm) holding photonic crystal fibers (PCFs), and three shallow trenches (depth of 125 µm) holding collimating lensed fibers (CLFs) for the probing laser. The capillary wave is excited by two pulsed laser beams generating optical interference, and the rapid motion of the capillary wave, which contains information regarding the viscosity and surface tension of the sample, is monitored by detecting the first-order diffracted beam of the probing laser irradiated onto the sample surface. In order to apply this sensor in manufacturing and clinical settings, the distance between the liquid level and the sensor must be properly adjusted because the sample surface is strongly influenced by evaporation and outside vibration disturbances under such conditions. In the MOVS, the specular reflection of the probing laser is detected by a symmetrically placed collimating lensed fiber. Maximizing the signal of specular reflection by using a piezo stage connected to the MOVS and PID controller, the focal points of the fibers (PCFs and CLFs) are adjusted on the sample surface. The high-reproducible measurement results under evaporation and outside disturbance indicate the validity of MOVS for *in situ* application.

*Key words: in-situ Monitoring, Laser-Induced Capillary Wave, Optical Interference, Optical Viscometer Chip, Surface Tension, Viscosity*

1. Introduction

The viscosity of a liquid is an essential physical property in numerous industrial fields (e.g. the polymer industry(1), the petroleum industry(2), the food industry(3), and so on) and material science for thermal design of liquid flow and its system. For example, in the polymer industry, real-time monitoring and *in situ* scanning of viscosity changes due to the formation and modification of polymers enables process control of polymerization, which can enhance the quality of products as well as the productivity of new polymer materials. In contrast, in the medical field, on-site monitoring of viscosity provides a fast and relatively noninvasive means of measuring small sample volumes of bodily fluids such as blood to provide information related to circulatory system disease (e.g. thrombosis(4)). This technique could potentially reduce the treatment burden for patients and thus improve their
quality of life (QOL). Furthermore, in this area of research and development, the massively parallel sensing of different materials, so-called "combinatorial synthesis"\(^5\), allows to promote the advanced research and development of material. However, the conventional viscosity measurement techniques (e.g. the capillary method, the falling-body method, and the vibrating method\(^6,\, 7\)), well known as standard bulk methods, require a large sample volume (a few tens of milliliters) and a long measurement time (a few minutes), and thus these techniques cannot fundamentally suit the demands mentioned above.

Several groups have developed miniaturized viscometers using microelectromechanical systems (MEMS) that can satisfy some of the above needs. For example, cantilever-type micro viscometric devices have been monolithically fabricated on a single-crystal silicon wafer\(^8\)-\(^10\). The resonant frequency of an oscillated cantilever provides the viscosity of a micro-liter order sample in which the device is immersed. Zhao et al\(^10\) have demonstrated a MEMS viscometric glucose sensor for monitoring glucose levels in diabetics. For the measurements carried out over a broad range of viscosities, temperatures, and shear rates, micro channel/capillary viscometers have been proposed\(^11,\, 12\). Chevalier et al\(^12\) have measured the viscosities of oil- and ethanol-based nanofluids up to \(10^{-5}\) s\(^{-1}\) using micromachined capillaries on chip rheometers. Despite the considerable amount of research in this field, a non-contact viscosity sensor applicable to in situ, as deposit or in process measurement where the viscosity changes rapidly, has not been proposed, because almost all of the devices are required to come in contact with the sample, thus introducing a risk of contamination.

We have developed a novel micro optical viscosity sensor (MOVS) based on a laser-induced capillary wave that enables in situ real-time monitoring of viscosity and surface tension change in micro-liter order liquids. The signal change due to the viscosity change has been successfully observed\(^13\). In order to apply this sensor in manufacturing and clinical settings, the distance between the liquid level and the sensor needs to be adjusted appropriately. In the present study, the applicability of MOVS with a focus control system for in situ monitoring was investigated using liquid samples, which are strongly influenced by evaporation and outside vibrational disturbances.

**Nomenclature**

- \(C_p\) : specific heat capacity, kJ/kg K
- \(I_h\) : pulsed heating laser energy, J/m\(^2\)
- \(T_0\) : mean of temperature distribution, K
- \(T_1\) : amplitude of temperature distribution, K
- \(u_0\) : spatially uniform displacement, m
- \(u_1\) : amplitude of the laser-induced capillary wave, m
- \(V_L\) : sound velocity of liquid, m/s
- \(V_i\) : visibility of interference fringe, -
- \(V_{BP}\) : visibility detected by the beam profiler, -
- \(\Delta z_d\) : focal depth, m

**Greek**

- \(\alpha\) : absorption coefficient, 1/m
- \(\beta\) : thermal expansion coefficient, 1/K
- \(\Lambda\) : interference fringe space, m
- \(\delta_{BP}\) : half-pixel size of the beam profiler, m
- \(\phi\) : incident angle of probing beam, deg
- \(\eta\) : viscosity, Pa s
- \(\lambda\) : thermal conductivity, W/m K
- \(\lambda_h\) : wavelength of heating laser, m
2. Measurement Principle

2.1 Laser-induced Capillary Wave Method

A schematic of the measurement principle of MOVS is shown in Fig. 1. The laser-induced capillary wave method was utilized for the optical viscometry. Terazima et al.\(^{(14)}\) first demonstrated the laser-induced capillary wave method for the investigation of surface interactions of a gas/liquid interface, and Nagasaka et al.\(^{(15)}\) have developed a bench-top-type \textit{in situ} viscometer using a nano-second pulsed carbon dioxide laser for the control of industrial materials such as food. The sample surface is heated by two pulsed laser beams, which intersect and generate an optical interference fringe pattern on the surface. The optical intensity distribution \(I(x)\) on the surface can be written as,

\[
I(x) = I_h \left\{ 1 + \cos \left( \frac{2\pi x}{\Lambda} \right) \right\}, \quad (1)
\]

\[
\Lambda = \frac{\lambda_h}{2\sin(\theta/2)}, \quad (2)
\]

where \(I_h\) is the intensity of the heating laser, \(\Lambda\) is the fringe space, \(\lambda_h\) is the wavelength of the excitation laser, and \(\theta\) is the beam intersecting angle. The sample surface is instantaneously heated by optical interference, and the temperature distribution \(T(x)\) is then expressed by the following expression.

\[
T(x) = T_h + T_1 \cos \left( \frac{2\pi x}{\Lambda} \right), \quad (3)
\]

![Fig. 1 Measurement principle of a micro optical viscosity sensor (MOVS). The sample surface is heated by the interference pattern of pulsed laser beams that are delivered through photonic crystal fibers (PCFs). The probing laser beam is irradiated onto the laser-induced capillary wave, and the first-order diffracted beam and specular reflected beam are detected via collimating lensed fibers (CLFs).](image)
where $T_0$ and $T_1$ are the mean and the amplitude of the temperature distribution, respectively. The spatially periodic temperature distribution generates a capillary wave (nanometer order of amplitude, and micro-meter order of wavelength) due to thermal expansion and the temperature dependence of the sample's surface tension. The surface displacement $u(x)$ due to the capillary wave is expressed as,

$$u(x) = u_0 + u_1 \cos \left( \frac{2\pi x}{A} \right),$$  \hspace{1cm} (4)

where $u_0$ is the spatially uniform displacement and $u_1$ is the amplitude of the laser-induced capillary wave. The geometric behavior of the laser-induced capillary wave is described by three phenomenological equations with the appropriate boundary conditions. First, the continuity equation is written as,

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0,$$  \hspace{1cm} (5)

where $\rho$ is the density and $\mathbf{V}$ is the velocity of the liquid. Second, the Navier-Stokes equation is expressed by,

$$\frac{\partial^2 \mathbf{u}}{\partial t^2} - \nu \nabla^2 \mathbf{u} - \frac{1}{c_L^2} \nabla \cdot \mathbf{u} - \beta T = -\beta V_s^2 \nabla \mathbf{u} ,$$  \hspace{1cm} (6)

where $\mathbf{u}$ is the displacement, $\beta$ is the thermal expansion coefficient, $c_L$ is the sound velocity in the liquid, and $\nu = \eta/\rho$ is the kinematic viscosity as a constant of viscosity $\eta$ divided by the density $\rho$. Third, the heat conduction equation is given by the following expression,

$$\frac{\rho C_p}{\partial t} \left( \frac{\partial T}{\partial t} \right) - \lambda \nabla^2 T = I_0 A \left( \frac{\cos \left( \frac{2\pi x}{A} \right)}{\exp \left( \frac{2\pi x}{A} \right)} \right) \exp (\alpha z) \delta(t) ,$$  \hspace{1cm} (7)

where $C_p$ is the heat capacity, $\lambda$ is the thermal conductivity, and $\alpha$ is the absorption coefficient of light. The boundary conditions are expressed as follows,

$$\sigma \left( \frac{\partial s}{\partial x} - \frac{\partial s}{\partial z} \right) + \rho V_s^2 \left( T - \frac{\partial s}{\partial x} - \frac{\partial s}{\partial z} \right) = 0 ,$$  \hspace{1cm} (8)

$$\eta \left( \frac{\partial u_s}{\partial z} + \frac{\partial u_s}{\partial x} \right) - \left( \frac{\partial \sigma}{\partial T} \right) \frac{\partial T}{\partial x} = 0 .$$  \hspace{1cm} (9)

$\sigma$ denotes the surface tension, and the temperature dependence of the surface tension that is sinusoidally distributed on the sample surface is considered in the second term of Eq. (9). The amplitude of the laser-induced capillary wave $u_1$ can be derived from the above expressions as a function of the physical properties of the liquid and the experimental condition written in Laplace domain. The detail of the Laplace transformed amplitude is written in the reference (16). Consequently, by observing the motion of the laser-induced capillary wave, the viscosity in the near surface and surface tension are numerically analyzed from the experimental data of the damped oscillating signal by inverse problem analysis. In order to measure the geometric behavior in the relaxation process of the laser-induced capillary wave after pulsed heating, which contains the information regarding viscosity and surface tension, a probing beam is irradiated onto the laser-induced capillary
wave, and the first-order diffracted beam is detected since the laser-induced capillary wave acts as a dynamic reflection grating. The intensity of the first-order diffracted beam $I_{\text{sig}}(t)$ is proportional to the square of the amplitude of the laser-induced capillary wave.

$$I_{\text{sig}}(t) \propto u_i^2(t).$$  (10)

Hence, by detecting the first-order diffracted beam, the dumping oscillation behavior of the laser-induced capillary wave can be observed. In the MOVS, all laser beams are delivered, irradiated and collected by photonic crystal fibers (PCFs) and collimating lensed fibers (CLFs) whose focal points and optical axes intersect with each other.

### 2.2 Focus Control Principle

For the *in situ* measurement of viscosity, the focus control system is required to reduce the negative effects of liquid level reduction and fluctuations due to evaporation of the sample and external vibrations, which are dominant factors in the control of the production process such as polymer coating process. In this research, specular reflection of the probing beam was utilized as a control signal of liquid levels. The probing beam delivered via CLF1 is irradiated onto the sample surface, and the first-order diffracted beam is detected through CLF2 as the signal of the laser-induced capillary wave, as previously mentioned in section 2.1. Meanwhile, the specular reflection of the probing beam is detected by CLF3 as the reference signal for the focus control feedback. The dual-axes configuration consisting of two CLFs is shown in Fig. 2. The point spread function (PSF) of the dual-axes configuration is the product of individual PSFs of CLF1 and CLF3, and the focal depth $\Delta z_d$ is described as:

$$\Delta z_d = \frac{0.37 \lambda_p}{N A \sin \phi},$$  (11)

where $\lambda_p$ is the wavelength of the probing beam, NA is the numerical aperture of the CLFs, and $\phi$ is the incident angle of the probing beam of CLF1 and the detection port of CLF3. The focal depth of MOVS is estimated to be 12.6 $\mu$m by Eq. (11) in the case of $\phi=60^\circ$. Maximizing the signal of the specular reflection by using a PID controller and a piezo stage (PZT, cutoff frequency of 600 Hz) connecting to the MOVS chip, the focal points of CLFs and the intersecting points of PCFs are adjusted on the sample surface.

![Fig. 2  Schematic diagram of the dual-axes configuration.](image-url)
3. Device Configuration and Experimental Setup

3.1 Design and Fabrication of the Micro Optical Viscosity Sensor (MOVS)

Fig. 3 Overall view of MOVS consisting of two wide and deep trenches holding PCFs and three narrow and shallow trenches holding CLFs.

Figure 3 shows an overall view of the MOVS without fibers. The MOVS (chip size of 12.6 mm × 6 mm × 800 µm) consists of two wide and deep trenches for the fibers of the excitation laser placed in the center at an intersecting angle of θ corresponding to the fringe space of interference, and three narrow and shallow trenches for the fibers of the irradiating and collecting probing laser placed in the side of the center trenches at an angle φ and the first-order diffraction angle ϕ1 that is described as,

\[ \phi_1 = \sin^{-1} \left( \frac{\lambda_p}{A - \sin \phi} \right) \]  

The five trenches with springs can precisely hold the fibers within ±1 µm because the MOVS chip is fabricated using MEMS technology. The PCFs (core diameter of 25.2 µm, mode-field diameter of 19.8 µm, ultra small NA of 0.04 at a wavelength of 1064 nm, clad diameter of 268 µm) can deliver the high-power short pulsed laser beam onto the sample surface to generate the laser-induced capillary wave. For the probing and detecting fibers, collimated lensed fibers are utilized in which the index-grating multi-mode fibers (clad diameter of 125 µm, length of 935 µm, and the spot size of 16.7 µm at the working distance of 3 mm) are fusion-spliced with single mode fibers.

The diameter of the PCF is approximately twice the size of the CLF; therefore, depth control of the CLF is required in the fabrication process. The MOVS is fabricated on a silicon-on-insulator (SOI) wafer by timed-etch deep reactive ion etching (DRIE) with an inductively coupled plasma (ICP) creating the fiber grooves, springs for holding the fibers, the dummy trenches, and the alignment edge for the fiber end face, according to a process flow schematically drawn in Fig. 4. First, a thermal oxide layer (thickness of 400 nm) and an aluminum layer of 300 nm are grown and sputtered on the SOI wafer (the device layer of 269 µm, the buried oxide layer of 4 µm, and the substrate of 525 µm) as photomask layers, as shown in Fig. 4(a). In order to form the grooves on the SOI wafer for the PCFs and CLFs that lead the heating and probing lasers, the photomask layers are patterned by a photolithography technique followed by etching of the layers using phosphoric acid aluminum etchant and reactive ion etching (RIE). The 8-µm photoresist is spin-coated and patterned to obtain the mask for the timed-etch DRIE process in order for the center of the fiber cores of the PCF and CLF to be aligned at the same height (Fig. 4(b)). Because the aspect ratio dependent etching (ARDE) effect and the micro loading effect in the grooves may occur in the case that wide and narrow trenches are patterned in the same wafer, the dummy trenches are patterned in the grooves of the PCF (Fig. 4(c)). The first and second etches were carried out by using timed-etch DRIE until the depth of the trenches for the CLFs reached the appropriate position (Fig. 4(d)). For the back-side etching, which shaped the outline of the tip of MOVS in order to control the working distance of the chip, a silicon
dummy wafer was bonded to the foreside of the processed wafer by photoresist, and the two windows were etched to access the foreside alignment mark for the backside alignment (Fig. 4(e)). After backside etching, the dummy trenches and springs were released by etching the sacrificial oxide layer using buffered hydrofluoric acid, and finally the fibers were packaged in the trenches by a micromanipulator (Fig. 4(f-h)).

A scanning electron microscope image of the MOVS in which the fibers are packaged and glued by UV resin is shown in Fig. 5. Although ion bombardment of the sidewall and the “mousebite effect” occurred to some extent during DRIE process, undercutting was not observed in the fabricated structures. Therefore, the trenches of the PCFs and CLFs can precisely hold the fibers with springs, and the centers of the two different fibers are aligned at the same height.

![Fig. 4 Process flow of the fabrication of the MOVS.](image)

![Fig. 5 A scanning electron microscope (SEM) image of microfabricated MOVS.](image)

### 3.2 Measurement Apparatus

Figure 6 shows a schematic diagram of the optical system of a MOVS. We utilize a Nd:YAG laser (wavelength of 1064 nm, power of 3 mJ, and a pulse width of 6 ns) to generate the capillary wave on the sample surface. The pulsed laser beam is first shaped by lenses 1 and 2 (L1 and L2) to achieve an optimal beam diameter, and then divided into two beams of equal intensity by a nonpolarized beam splitter (NPBS). The two beams are coupled into PCFs by using the objective lens (OBJ) with a single-mode fiber coupler, and are then intersected on the sample surface, generating the interference fringe pattern. The sample surface is interferometrically excited, and the laser-induced capillary wave is generated. The probing laser beam (wavelength of 641 nm, and maximum power of 20
mW) is led to the sample surface via CLF1. The first-order diffracted beam is collected by CLF2, and is detected by a cooled photomultiplier tube (PMT) with a low-noise high-speed current amplifier. The specular reflection of the probing beam for the focus control signal of the MOVs chip is simultaneously detected by a Si-PIN photodetector (PD). The cutoff frequency of the photodetector (up to 200 kHz) is much lower than that of the dumping oscillation of the laser-induced capillary wave, and the intensity of the first-order diffracted beam is significantly lower than that of the specular reflection; the diffraction beam can therefore be assumed to not affect the focal depth control signal.

Fig. 6 Schematic of the optical system of the MOVs.

4. Results and Discussion

In order to verify the feasibility of the presented MOVs, a point spread function (PSF) was performed in the z-direction, and the interference fringe of the excitation laser delivered by PCFs was observed, as shown in Figs. 7 and 8. Figure 7 indicates the optical response of the specular reflection during the z-axis scanning of distilled water. The signal at the out-of-focus position (z=±5 µm) was significantly fluctuated, because the specular reflection signal in this region was sensitive to small variations in liquid level. The full-width of half-maximum of PSF was estimated to be 10.7 µm, which agreed with the theoretical value calculated in section 2.2. The deviation was caused by the uncertainty of positioning, which could be changed due to outside disturbance. The two short-pulsed beams successfully formed an interference pattern at a cross section of the two beams as shown in Fig. 8. The interference fringe was observed by a microscopic beam profiler (pixel

Fig. 7 PSF of dual-axes configuration of CLFs.   Fig. 8 Interference fringe generated by heating laser.
size of 4.65 µm, objective lens of fourfold magnification), and the fringe space was estimated to be 3.96 µm, which was in agreement with the designed value of 4 µm. The visibility of the interference fringe was calculated as 0.14. In fact, the pixel size of the beam profiler is close to the fringe space; therefore the image captured by the beam profiler is averaged. The actual visibility $V_i$ is described by the following expression,

$$V_i = \frac{A}{2\pi\delta_{BP}}V_{BP} \sin \left( \frac{2\pi\delta_{BP}}{A} \right), \quad (13)$$

where $\delta_{BP}$ is half the size of the pixel, and $V_{BP}$ is the visibility calculated from the image of the beam profiler. In the present setup, the actual visibility $V_i$ is estimated as 0.17, which is quite low due to the optical pass difference between the two pulsed laser beams. The coherent length of the pulsed YAG laser is around a few centimeters, thus there is still room for improvement in the visibility by adjusting the fiber length, which directly corresponds to the intensity of the first-order diffracted beam.

The specular reflected light signal of the probing beam and the displacement of the piezo stage are shown in Fig. 9. The MOVs tracked the reduction of liquid levels due to evaporation of the sample (Fig. 9(a)). The CLF1 was focused on the sample surface for a prolonged measurement period, even if the sample had evaporated; therefore, the fluctuation of the signal under control was dramatically decreased by using the control system. The deviation was calculated to be approximately \(\pm 0.7\) µm. Finally, to assess the validity of the focus control system for the in situ measurement of viscosity, we demonstrated the stability and reproducibility of the first-order diffracted beam of the
laser-induced capillary wave using a mechanically vibrated sample of distilled water with 0.01 % pigment (black carbon) at room temperature and atmospheric pressure. The oscillation (amplitude of 13 µm and frequency of up to 7 Hz) was applied to the sample, and the specular reflection was monitored, as shown in Fig. 9(b). The piezo stage was actuated to maintain the specular reflected signal against the microvibrational disturbance. The standard deviation without control was evaluated to be 30 µW; in contrast, the standard deviation under control was improved threefold (standard deviation of 10 µW). In Fig. 10, the first-order diffracted beams were averaged 256 times for 2 min while the vibration was applied. The signal-to-noise ratio (SNR) of the controlled laser-induced capillary wave signal (SNR=250) is dramatically improved over the uncontrolled signal (SNR=66, see Fig. (10(a)), and the high-speed damping oscillation (especially 2nd peak and 3rd peak of oscillation) within 1 µs was clearly observed, as shown in Fig. 10(b). The detected signal under control was highly reproducible and in good agreement with the theoretical curve. By analyzing the damping oscillation signal, the kinematic viscosity was estimated to be 0.61 mm²/s. Although there was an effect of dispersing media (low concentration of pigment), the estimated value was valuable compared with the reference value of the water. Consequently, the applicability of the MOVS for non-contact and disturbance-free viscometry, which was promising in situ measurement where the viscosity was drastically changed in short time such as polymer coating, was verified.

5. Conclusion

A novel micro optical viscosity sensor (MOVS) with a focus control system has been proposed for in situ applications. The laser-induced capillary wave was successfully generated on the sample surface where the evaporation and ambient vibration strongly affected the liquid level, and the highly reproducible damped oscillation signal of the laser-induced capillary wave was detected using a MOVS with a focus control system. The validity of a MOVS that can track sample evaporation within 1 µm and compensate for ambient vibrations, was confirmed. The measurement results using distilled water with 0.01 % pigment indicate the applicability of MOVS for in situ measurement.

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