1. Introduction

In the MnCoGe alloy, the structural transformation from a Ni$_3$In-type hexagonal structure (space group P6$_3$/mmc, No. 194) to a TiNiSi-type orthorhombic structure (space group Pnnm, No. 62) at 375–620 K ($T_m$) is followed by the magnetic transformation from a paramagnetic state to a ferromagnetic state at 327–355 K ($T_c$). The two crystal structures were shown in Fig. 1. When the crystal structure changes from a hexagonal phase to an orthorhombic one, a large volume change and a large increase in magnetic moment occur. If the $T_m$ is lowered below the $T_c$, two transitions, i.e., structural and magnetic, can occur simultaneously and can cause an improvement of the magnetocaloric effect. Accordingly, several experimental studies have been conducted such as introducing a vacancy and fourth elements in MnCoGe. Recently, several experimental studies on (Mn,Fe)CoGe and Mn(Fe,Co)Ge have shown that the Fe substitution produces a decrease in the $T_m$ below the $T_c$. Thus, these materials can be used as a magnetic functional material in a magnetic-field-driven actuator or a magnetic refrigeration material.

In this study, we have investigated the structural transformation from a hexagonal ferromagnetic structure to an orthorhombic ferromagnetic one. We have performed first-principles calculations for the (Co,Fe)MnGe and Co(Mn,Fe)Ge systems. We will discuss the structural transformation from the point of view of an activation energy (barrier) between two structures, which is estimated from first-principles calculations.

2. Approach

We used a 2 × 2 × 1 (2 × 2 × 2) supercell to simulate a one-quarter (one-eighth) substituted hexagonal system with the lattice vectors $a_h$, $b_h$, and $c_h$. We used a 1 × 2 × 2 (2 × 2 × 2) supercell to simulate a one-quarter (one-eighth) substituted orthorhombic system with the lattice vectors $a_o$, $b_o$, and $c_o$. We optimized the lattice constants of the hexagonal and orthorhombic structures by minimizing the total energy. The atomic positions of the hexagonal and orthorhombic structures were optimized by minimizing the forces acting on the atoms. The results are listed in Table 1, where we only show the atomic positions in the orthorhombic structures, we optimized the atomic positions of the atoms in the orthorhombic and hexagonal phases in the paramagnetic and ferromagnetic states, for which the optimal lattice constants and atomic positions are listed in Table 1. This figure shows that a ferromagnetic orthorhombic phase is the most stable state. The values changes by 2.8% and 5.2% between the two structures in paramagnetic and ferromagnetic states, respectively. These values are close to the values reported previously for a paramagnetic state (4.1%) and for a ferromagnetic state (5.5% and 4.4%).

3. Results and Discussions

3.1 Preliminary results

Figure 2 shows the total energy as a function of the volume for the hexagonal and orthorhombic phases in the paramagnetic (non-magnetic) and ferromagnetic states, for which the optimal lattice constants and atomic positions are listed in Table 1. This figure shows that a ferromagnetic orthorhombic phase is the most stable state. The values changes by 2.8% and 5.2% between the two structures in paramagnetic and ferromagnetic states, respectively. These values are close to the values reported previously for a paramagnetic state (4.1%) and for a ferromagnetic state (5.5% and 4.4%).

3.2 Activation energy

We prepared other nine structures with the following lattice constants: $x_1 = x_0 + j(x_{10} - x_0)/10$; $j = 0, 1, 2, \ldots, 10$; $x_{10} = a_o, b_o, c_o$; $x_{11} = c_o, a_o, a_o + 2b_h$ to estimate the activation energy (barrier) between the two structures. For these nine structures, we optimized the atomic positions of the atoms in the cell. The total energies obtained for the 11 structures are shown in Fig. 3(a). The energy difference between each
structure and the orthorhombic one is maximum at a step 7 \((j = 7)\). We regard this value as the activation energy from an orthorhombic phase to a hexagonal one. This figure shows that the activation energy decreases with Fe substitution and that the amount of change is larger in Mn(Co0.75Fe0.25)Ge than in (Mn0.75Fe0.25)CoGe.

The magnetization per formula unit is shown in Fig. 3(b). This figure shows the following aspects. The magnetization, \(M\), decreases from step 0 (orthorhombic phase) to step 10 (hexagonal phase). The \(M\) of Mn(Co0.75Fe0.25)Ge is almost same as that of MnCoGe, but the \(M\) of (Mn0.75Fe0.25)CoGe is lower than that of MnCoGe. Larger magnetocaloric effects are expected for Mn(Co,Fe)Ge than for (Mn,Fe)CoGe because the change in \(M\) from orthorhombic to hexagonal phases is larger for Mn(Co,Fe)Ge than for (Mn,Fe)CoGe.

We show the atomic arrangements of steps 0, 8, and 10 from the view of the \(b_0\) axis in Fig. 4. This figure indicates that the movement of Co (Mn) is remarkable from steps 10 to 8 (8 to 0). To verify this, we estimate an amount of movement of Mn, Co, and Ge and the results are listed in Table 2. Here, we listed the first three atoms with the largest movement. The amount of movement of Ge is smaller than the amounts of movement of Co and Mn, and hence, it is not shown. This table validates the arrangement shown in Fig. 4. However, the result for steps 0 to 6 shows that the amount of movement is almost the same in both Co and Mn. This is also observed in steps 6 to 10. Thus, the activation energy is closely related to the movements of both Co and Mn, and the contribution of the movement of Ge is small.

To investigate the relationship between Fe concentration and the stability of the structure, we have prepared an additional structure Mn(Co0.625Fe0.375)Ge, whose lattice constants and atomic positions are fixed to the corresponding values of hexagonal and orthorhombic MnCoGe. The result

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Table 1 Optimized lattice constants (Å) of (Mn1-xFe0)(Co1-yFey)Ge. Optimized atomic positions of orthorhombic Mn, Co, and Ge are listed at 3rd, 4th and 5th columns. Optimized atomic positions in other materials are not listed.

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<th>(a)</th>
<th>(b)</th>
<th>(c)</th>
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Fig. 2 Total energy of MnCoGe as a function of the volume per two formula units. The solid and dotted lines show the orthorhombic and hexagonal phases. White (black) triangle and diamond symbols show the paramagnetic (ferromagnetic) state.

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**Fig. 1** Hexagonal (a) and orthorhombic (b) structures.
are shown in Fig. 5. The energy difference between the hexagonal and orthorhombic phases almost disappears in Mn(Co$_{0.875}$Fe$_{0.125}$)Ge. Our results indicate that, for $x = 0.375$, the hexagonal structure is more stable than the orthorhombic one. This value of $x_c$ is larger than those estimated from the experimental results such as 0.25 or 0.08. Thus, we conducted a trial calculation of (Mn$_{0.375}$Fe$_{0.125}$)(Co$_{0.375}$Fe$_{0.625}$)Ge, whose lattice constants and atomic positions are fixed to the corresponding values of hexagonal and orthorhombic Mn(Co$_{0.875}$Fe$_{0.125}$)Ge. In this case, the hexagonal phase is lower in energy than the orthorhombic phase. This result indicates a random occupation of Fe at both Mn and Co sites.

4. Summary

We investigated the structural transformation from the point of view of the activation energy (barrier) between the hexagonal and orthorhombic structures, which is estimated from the first-principles calculations. We showed that the Fe substitution decreases the activation energy. We discussed the relationship between the activation energy and the atomic movement. We indicated the possibility that Fe atoms randomly occupy Mn and Co sites.

Acknowledgments

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REFERENCES

20) For this material, we do not show such data as optimized lattice constants and atomic positions in this paper. The data will appear in an upcoming paper.